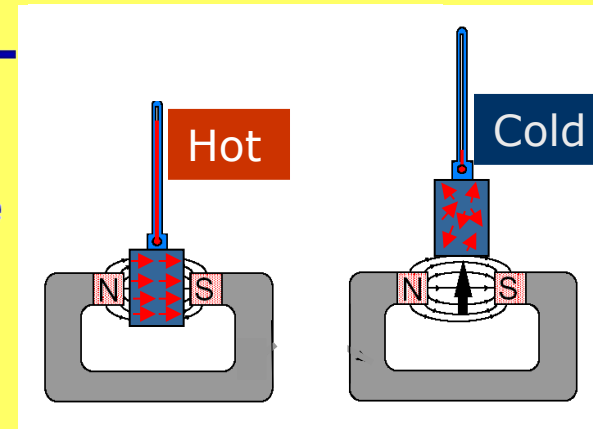




European School in Materials Science

$$\Delta S_{mag} + \Delta S_{lat} = 0$$



Electronic aspects of magnetocaloric refrigeration

$$G = G_0 + G_0 V G$$

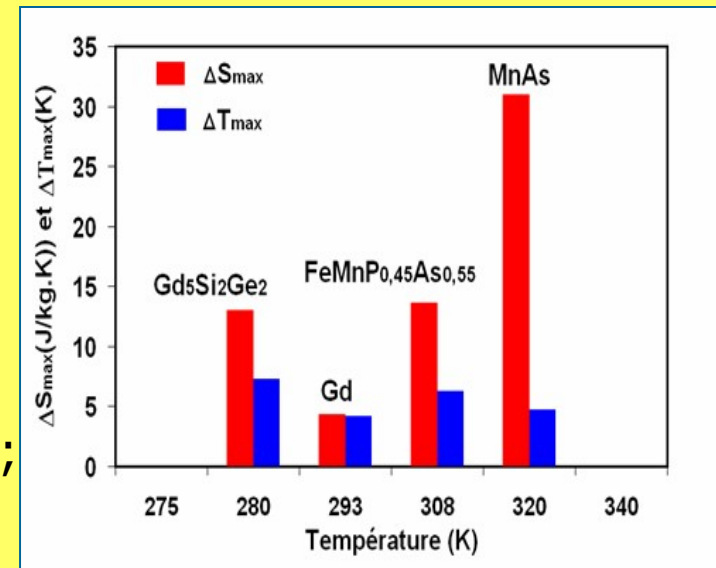
Janusz Tobola



Faculty of Physics and Applied Computer Science,
 AGH University of Science and Technology,
 Krakow, Poland
 email: tobola@ftj.agh.edu.pl

Outline

1. Magneto-caloric effect **MCE** (brief history and introduction), giant MCE.
2. Entropy contributions and concept of MCE cooling – analogy to thermodynamic cycle; how to measure MCE ?
3. Illustrative examples of MC materials & experimental results
 - $\text{Gd}_5\text{Si}_2\text{Ge}_2$ - RE alloys,
 - MnAs, MnFe(As-P), Fe_2P , Mn_3Sn_2 – TM alloys.
4. Electronic structure of intermetallic MC compounds (MnAs, MnFeAs-P, ...)
5. Concept of DLM (*disordered local moments*)- simulation of paramagnetic state within DFT methods.
5. Estimation of entropy jump: mean field approach for magnetic entropy.
6. Estimation of lattice entropy from phonon calculations.
7. Summary



Brief history of **MCE** discovery

1881 E. Warburg, iron heats up in magnetic field $\sim 0.5\text{--}2\text{ K/1T}$, *Ann. Phys.* (1881)

1926 P. Debye (Nobel 1936, chemistry)

1927 W. Giauque (Nobel 1949, chemistry)

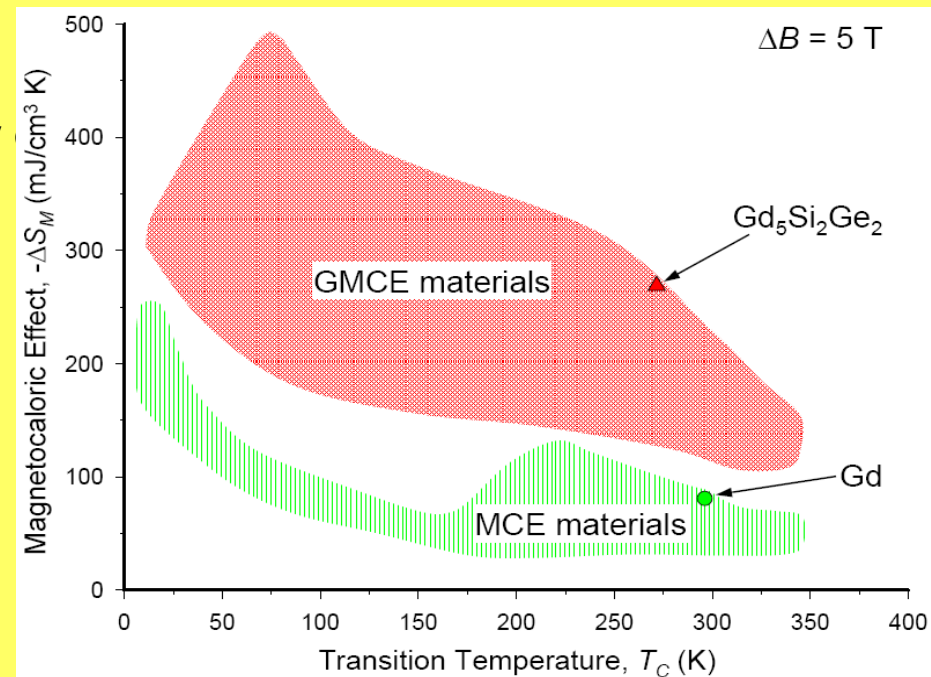
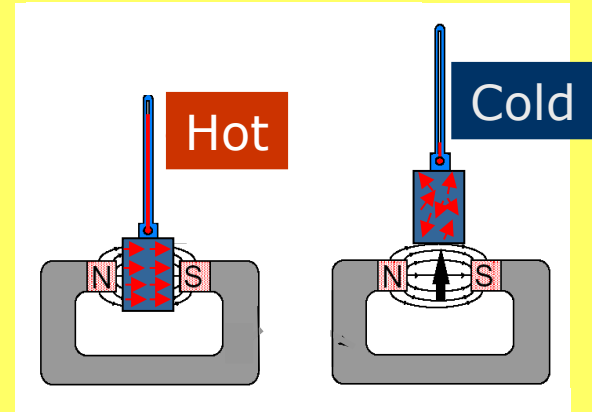
cooling via adiabatic demagnetization (order-disorder transition of magnetic moments in presence (or not) of magnetic field; for cryogenic purposes, down to 0.25 K (MacDougall, 1933).

1997 K. A. Gschneider & V. Pecharsky (Ames Lab., USA), PRL (1997) - discovery giant magnetocaloric effect :

MCE: an intrinsic property of magnetic materials;

MCE : the largest at the transition temperature, e.g. ferro-para

Adiabatic magnetization / demagnetisation



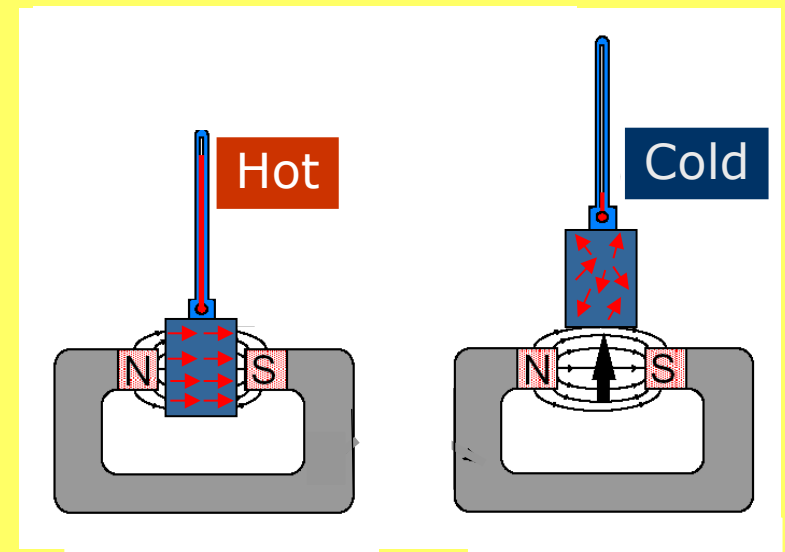
Introduction

MCE

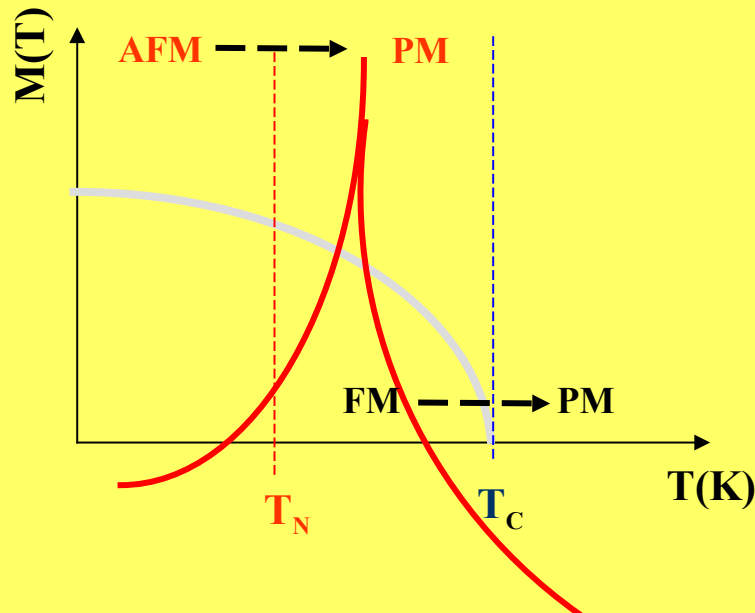
Intrinsic property of a material

Maximal at the transition temperature

$$\Delta S_{mag} + \Delta S_{lat} = 0$$



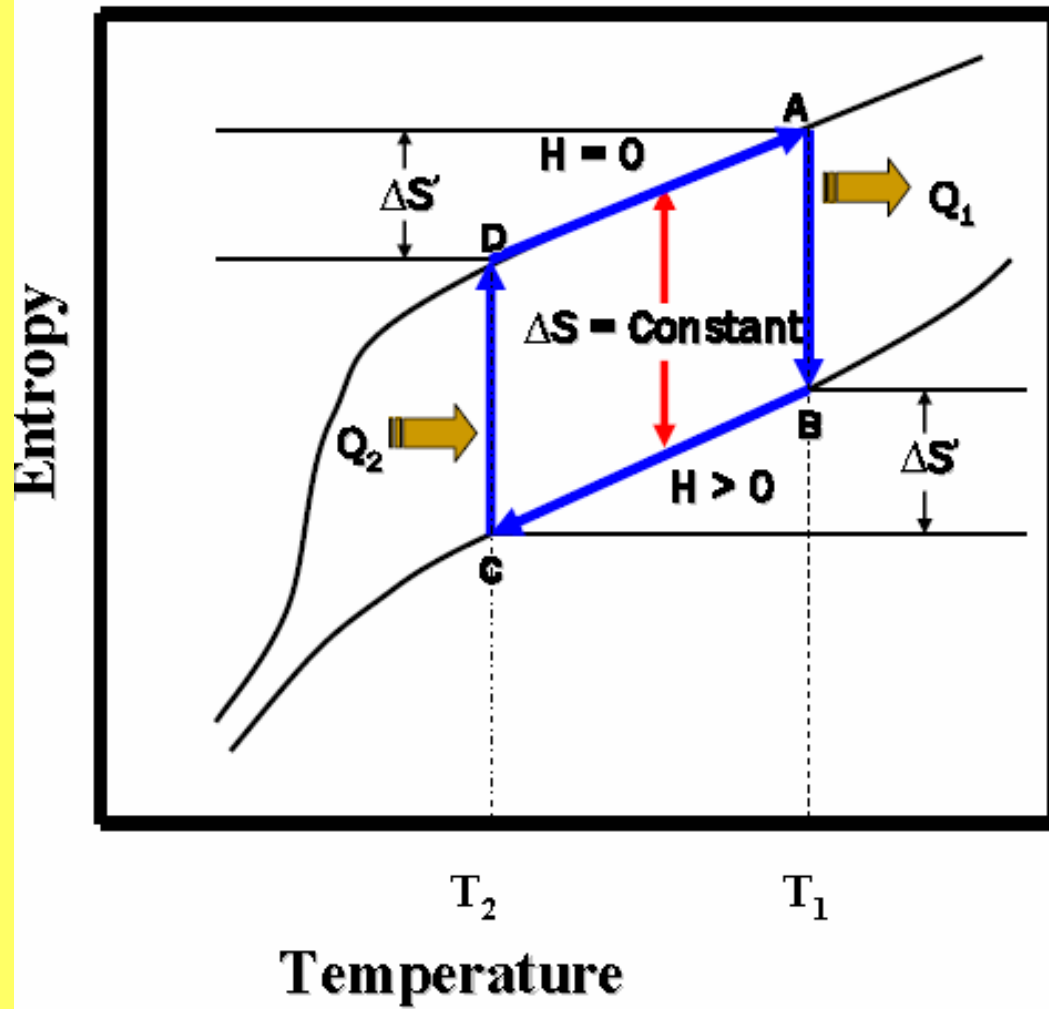
Adiabatic
Magnetisation / Demagnetisation



Type of magnetic transitions:
FM-PM,
AFM-PM,
AFM-FM (but not so large)

Ferromagnet, Ferrimagnet, Antiferromagnet,
Inhomogeneous Ferromagnet, Amorphous,
Superparamagnet....

Analysis of Ericsson cycle



A → B

The magnetic refrigerant emits ΔS in the form of heat $Q_1 = \Delta S * T_1$

B → C

The magnetic refrigerant changes its temperature from T_1 to T_2

C → D

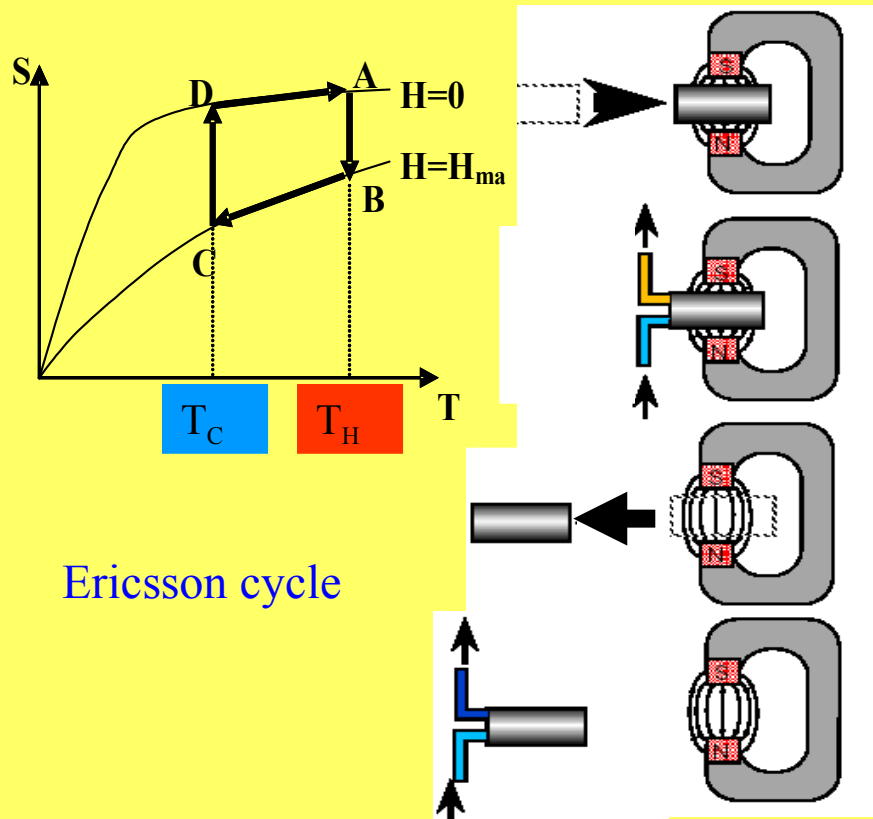
The magnetic refrigerant takes heat $Q_2 = \Delta S * T_2$ from the external heat source of temperature T_2

D → A

The M R takes back all the heat given to the regenerator in the second (B-C)

Analogy to thermodynamic cycle

Adiabatic magnetization/demagnetization

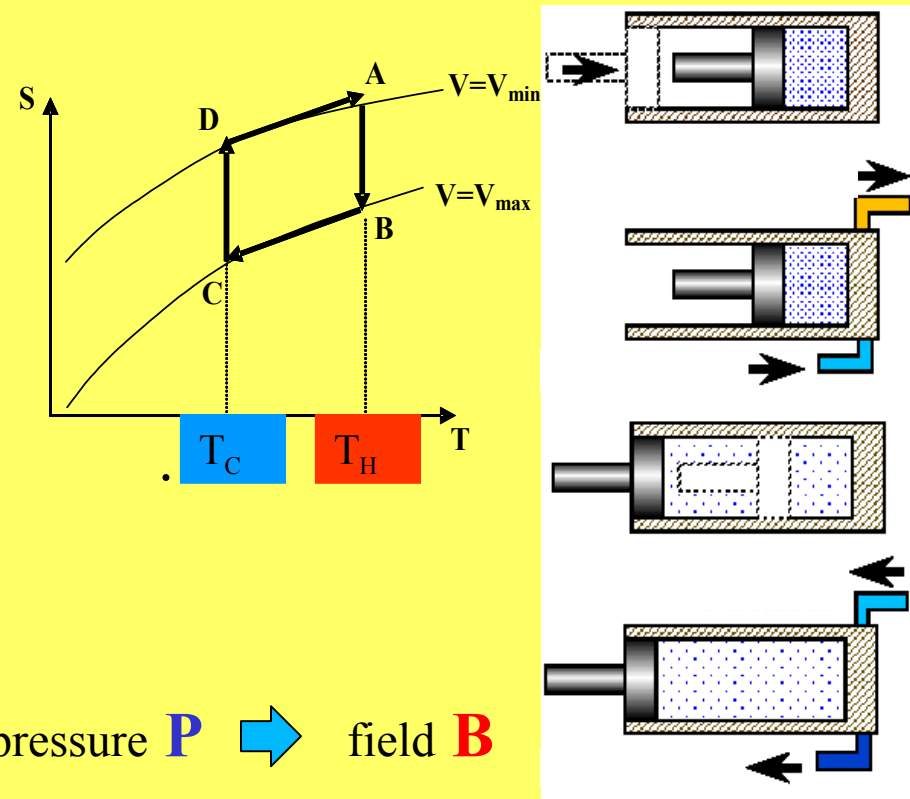


Ericsson cycle

$$B \cdot (M_1 - M_2) = \Delta S \cdot \Delta T = -RCP$$

Ideal Carnot cycle :

$$\eta = \frac{\Delta W}{\Delta Q_H} = 1 - \frac{T_C}{T_H} \quad \Delta W = \oint P dV = (T_H - T_C)(S_B - S_A)$$



pressure **P** → field **B**

volume **V** → magnetization **M**

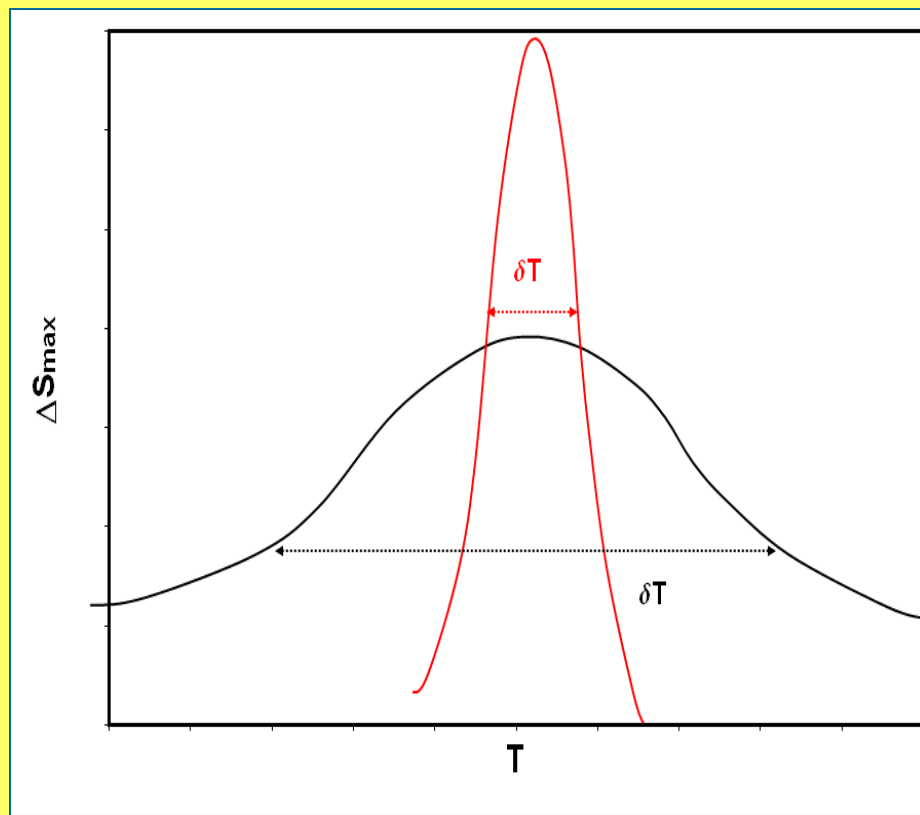
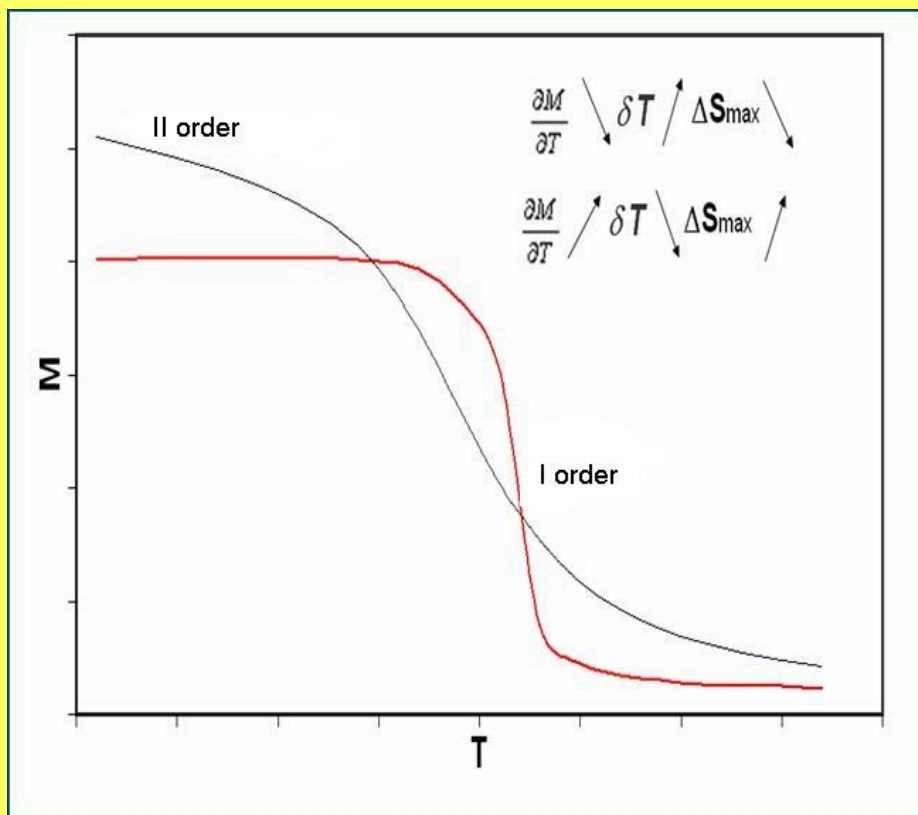
RCP – relative cooling power

$$\Delta Q_C = T_C(S_B - S_A)$$

$$\Delta Q_H = T_H(S_B - S_A)$$

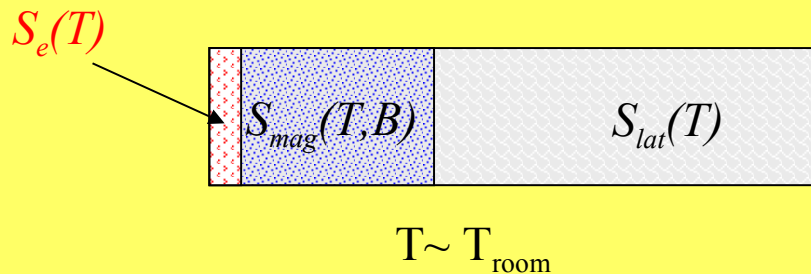
Important conditions for giant MCE

What model to apply for ?



It depends first on the nature of the transition, on the type of magnetic ordering, on the nature of the material....

Entropy



$$S_{tot} = S_{el} + S_{mag} + S_{lat}$$

$$\Delta S_{mag} + \Delta S_{lat} = 0$$

Adiabatic Process

$$\Delta S_{mag}(T, \Delta B) = \int_0^B \left(\frac{\partial M}{\partial T} \right)_B dB$$

$$\Delta S_{lat} = C_p(B, T) \frac{\Delta T}{T}$$

$$\Delta T_{max} = \frac{-T \Delta S_{mag}}{C_p(B, T)}$$

Calorific Capacity

$$C_p(B, T)$$



Magnetic Entropy

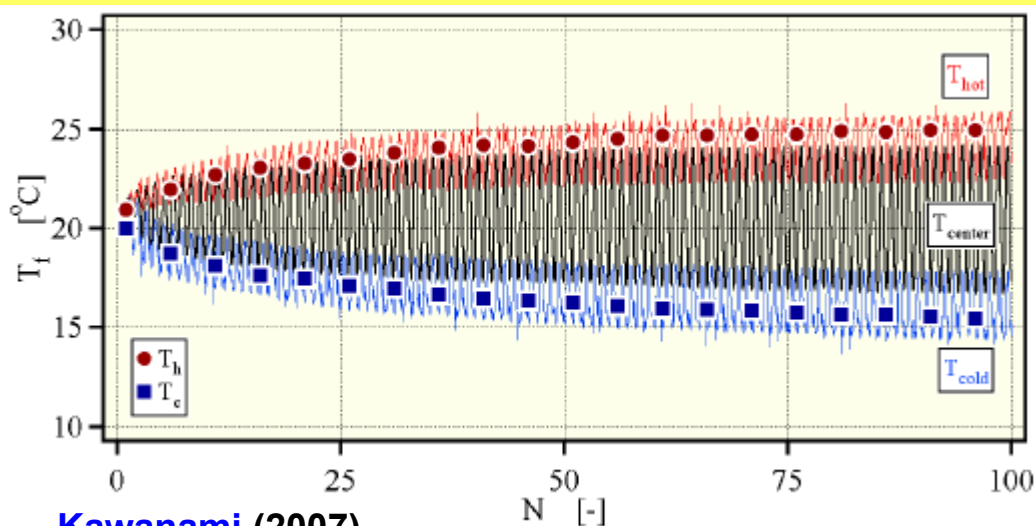
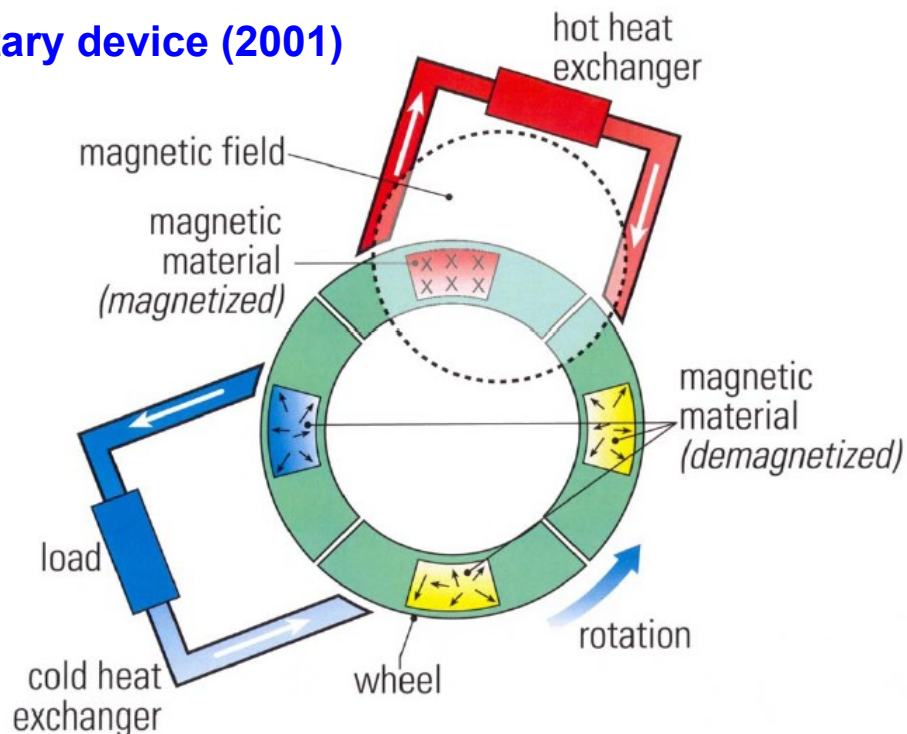
$$\Delta S_{mag}$$



$$\Delta T_{max}$$

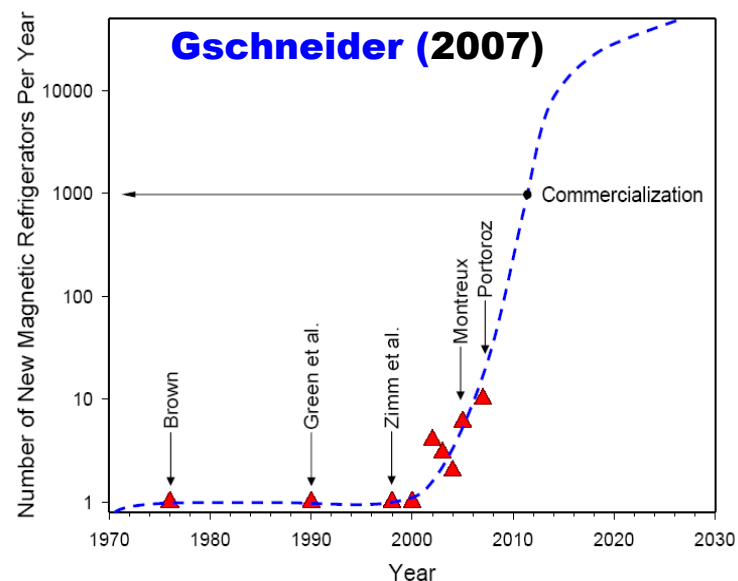
ASTRONAUTICS

rotary device (2001)

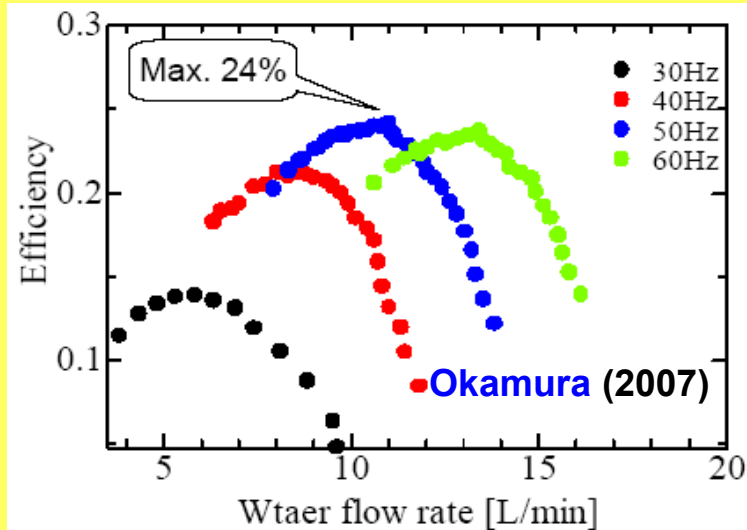


Kawanami (2007)

(S-growth curve for new technologies)



Gschneider (2007)



Efficiency = (Pump work) / (Power consumption)

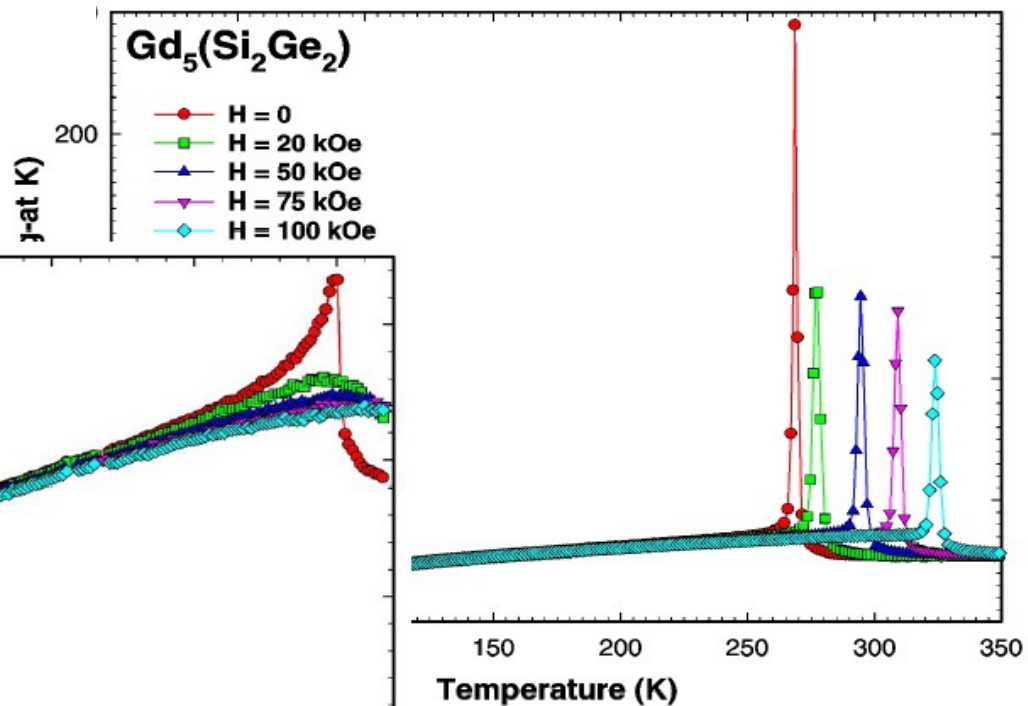
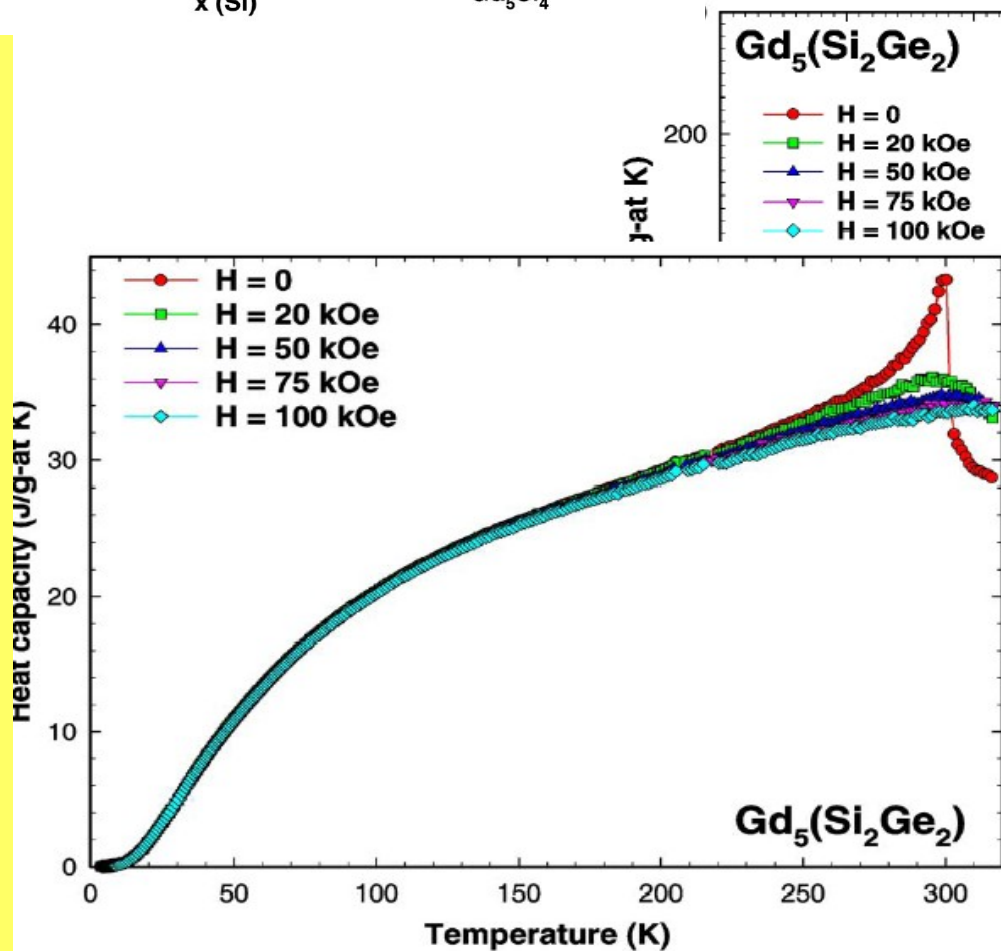
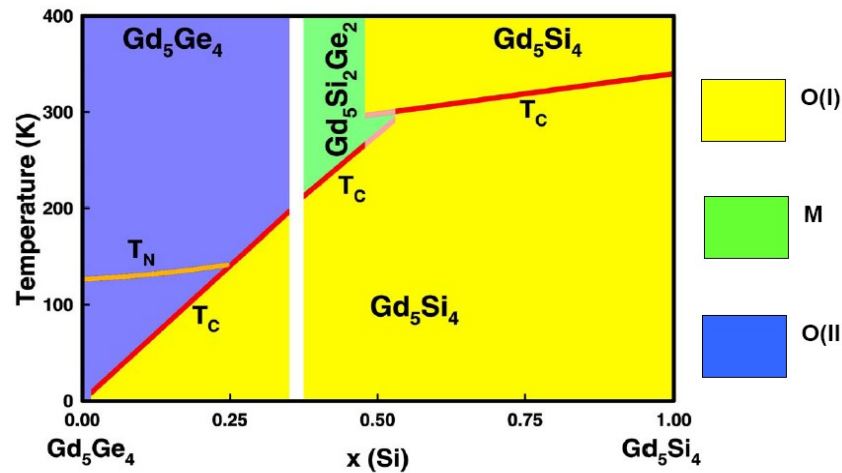
Compound	$-\Delta S$ [$\text{J} \cdot \text{kg}^{-1} \cdot \text{K}^{-1}$]	T [K]	References
MnAs	40	318	[1]
Mn_{0.99}Cr_{0.01}As	34.6	310	SCTE2006
Mn_{0.98}V_{0.02}As	30.5	286	SCTE2006
Mn_{0.90}Ti_{0.05}V_{0.05}As	24	274	SCTE2006
Mn_{0.98}Ti_{0.02}As	35.7	316	SCTE2006
MnAs _{0.9} Sb _{0.1}	30	283	[1-3]
FeMn(As,P)	18	305	[4]
La(Fe _{0.88} Si _{0.12}) ₁₃ H ₁	23	274	[5]
Gd ₅ Si ₂ Ge ₂	36.4	272	[6]
Gd	2.5	294	[7]
Fe ₄₉ Rh ₅₁ ($\Delta B = 2\text{T}$)	22	313	[7]
MnAs (under pressure)	267 !!	~280	[8]

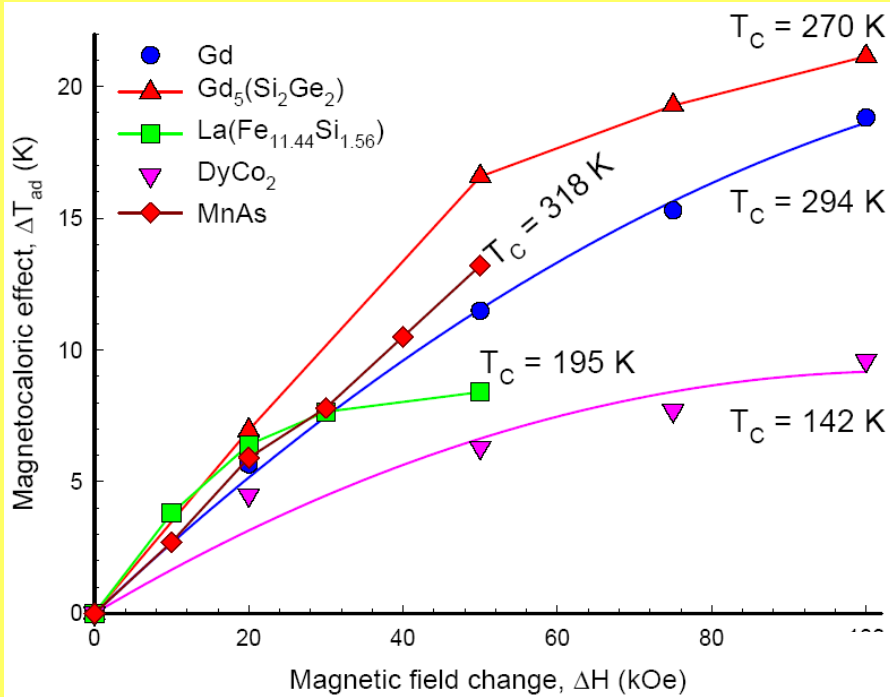
$\Delta B = 5 \text{ T}$

- [1] H.Wada and Y. Tanabe, Appl. Phys. Lett. **79**, 3302 (2001).
 [2] H.Wada, K. Taniguchi, and Y. Tanabe, Mater. Trans., JIM **43**, 73 (2002).
 [3] H. Wada, T. Morikawa, K. Taniguchi, T. Shibata, Y. Yamada, and Y. Akishige, Physica B (Amsterdam) **328**, 114 (2003).
 [4] O. Tegus, E. Brućk, K. H. J. Buschow, and F. R. de Boer, Nature (London) **415**, 150 (2002).
 [5] A. Fujita, S. Fujieda, Y. Hasegawa, and K. Fukamichi, Phys. Rev. B **67**, 104416 (2003).
 [6] A.O. Pecharsky, K. A. Gschneidner, Jr., V. K. Pecharsky, J. Appl. Phys. **93**, 4722 (2003).
 [7] A.M. Tishin and Y. I. Spichkin, (Institute of Physics, Bristol and Philadelphia, 2003), 1st ed., Vol. 1, Chap. 11, p.351.
 [8] S.Gama et al, Phys. Rev. Lett. **93**, 237202 (2004)

Giant MCE system

Pecharsky & Gschneider, 1997-2007

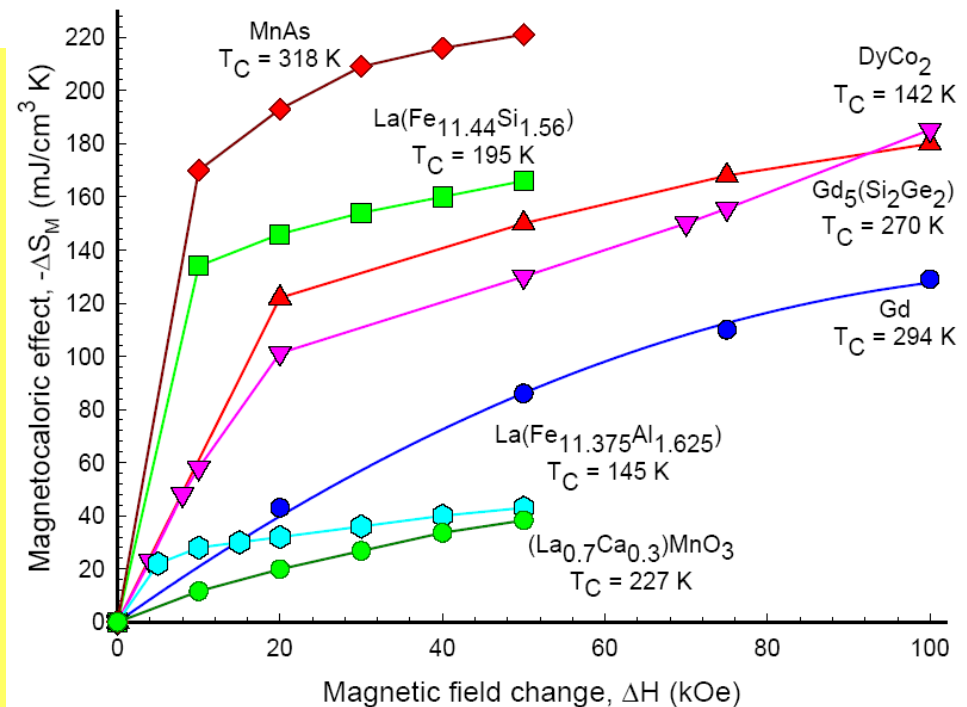




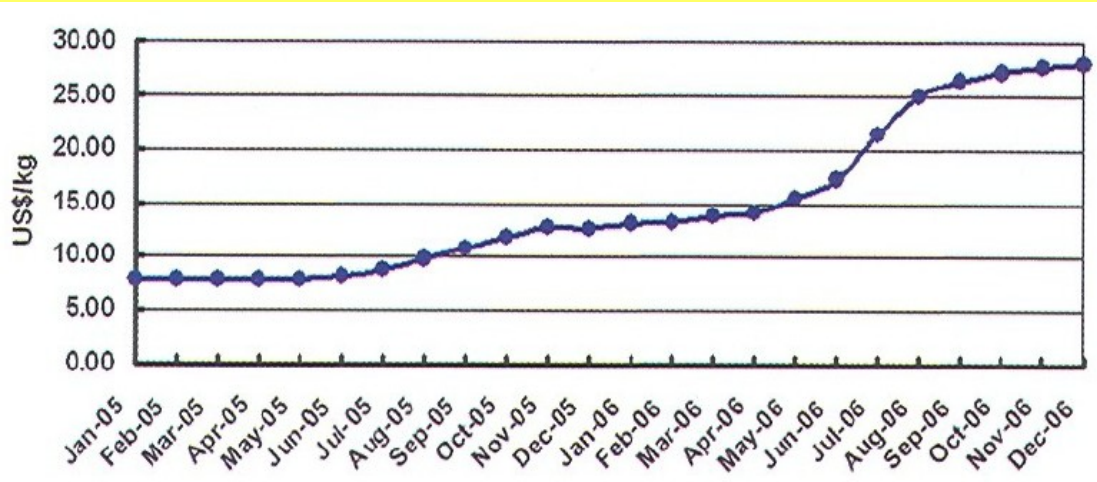
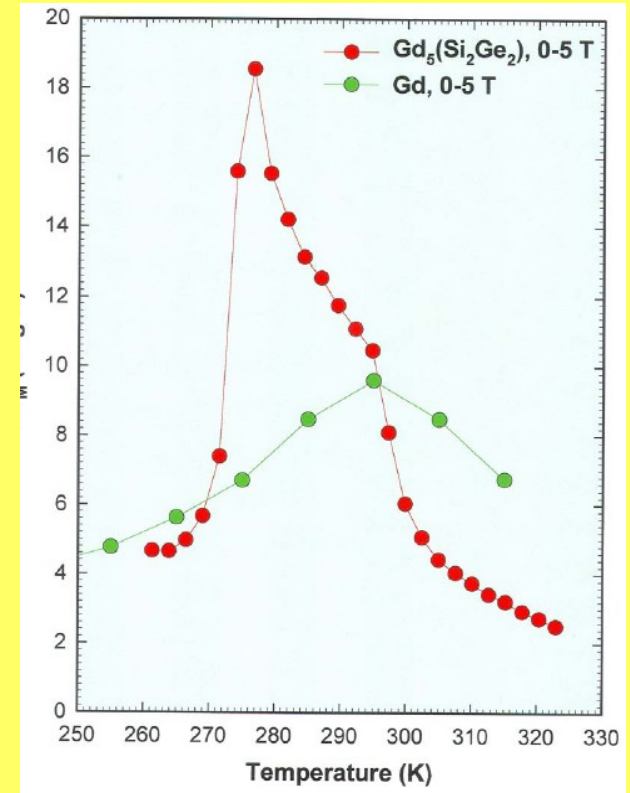
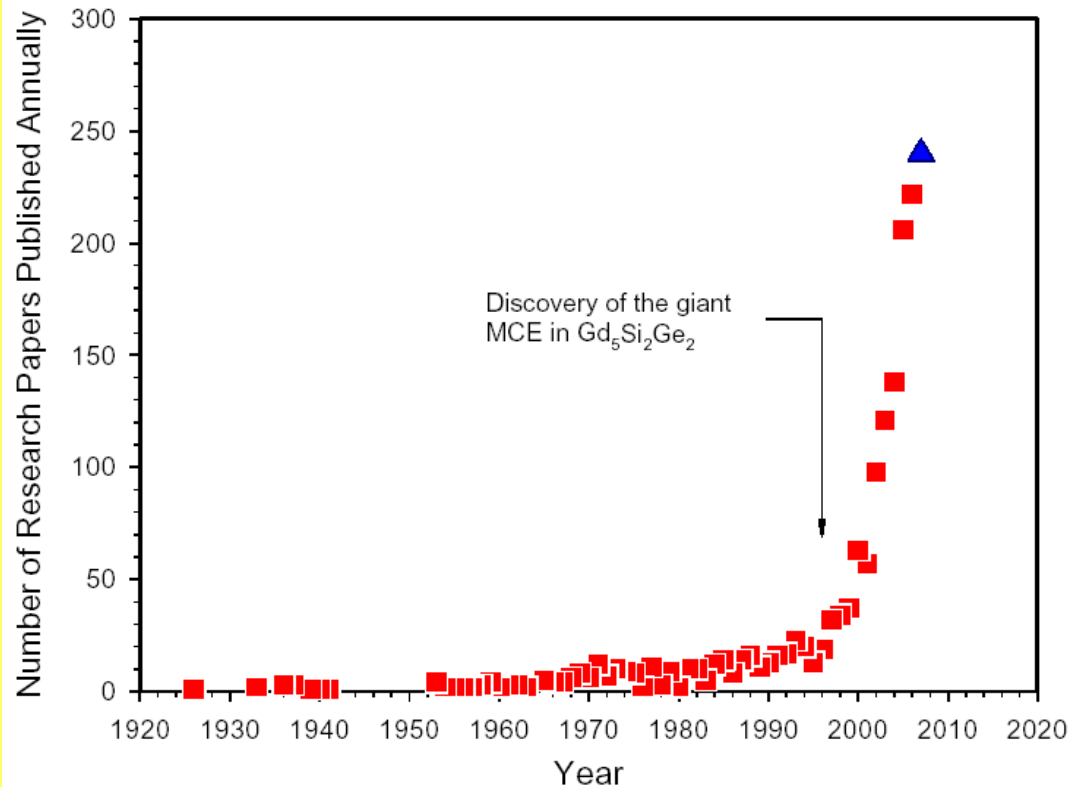
New MCE materials

← Temperature jump

Entropy jump →



Giant MCE – magnets demanded



Active magnetic refrigerator (AMR), e.g. Gd, La-Fe-Si

0.1-100 kg / AMR

Efficient magnets
Nd-Fe-B

0.1-100 kg / AMR

Gschneider, 2007

Entropy contributions and relations to *ab initio* calculations

$$S_{\text{tot}} = S_{\text{el}} + S_{\text{mag}} + S_{\text{lat}}$$

for $h^{\text{ext}} = 0$, the integral gives S_{el}

$$S_{\text{mag}}(T, h^{\text{ext}}) = R \left[\sum_{\sigma} \int_{-\infty}^{\mu} \ln \left(1 + e^{-\beta(\varepsilon - \mu)} \right) \rho_{\sigma}^{\text{el}}(\varepsilon) d\varepsilon \right. \\ \left. + \frac{1}{kT} \sum_{\sigma} \int_{-\infty}^{\mu} (\varepsilon - \mu) \rho_{\sigma}^{\text{el}}(\varepsilon) f(\varepsilon) d\varepsilon \right]$$

de Oliveira, Eur. Phys. J. B (2004)

$$S_{\text{lat}} = R \left[- \int \ln \left(1 - e^{-\beta \hbar \tilde{\omega}} \right) \rho^{\text{ph}}(\tilde{\omega}) d\tilde{\omega} \right. \\ \left. + \frac{1}{kT} \int \frac{\hbar \tilde{\omega}}{(e^{\beta \hbar \tilde{\omega}} - 1)} \rho^{\text{ph}}(\tilde{\omega}) d\tilde{\omega} \right]$$

**Phonon DOS is needed
to estimate lattice contribution**

Estimations of entropy can be made for electrons and phonons if DOS is known.
Using Debye temperature, S_{lat} may be roughly estimated - allowing to interpret ΔS jump in experiment.

adiabatic process

$$\Delta S_{\text{mag}} + \Delta S_{\text{lat}} = 0$$

$S_{\text{el}} \approx \gamma T$ often sufficient

in MCE systems smaller than $S_{\text{mag}}, S_{\text{lat}}$

$$S_{\text{lat}}(T, h^{\text{ext}}) = \left[-3R \ln \left(1 - \exp \left(-\frac{\tilde{\Theta}_D}{T} \right) \right) \right. \\ \left. + 12R \left(\frac{T}{\tilde{\Theta}_D} \right)^3 \int_0^{\tilde{\Theta}_D/T} \frac{x^3}{\exp(x) - 1} dx \right]$$

**BUT this can be approximatively
done e.g. from Debye model**

Reminder: magnetic susceptibility

Free energy (Helmholtz)

$$F = -k_B T \ln Z$$

$$Z = \sum_n e^{-\frac{E_n}{k_B T}}$$

Partition function

$$\begin{aligned} Z &= \sum_{J_z=-J}^J e^{-\eta J_z} = \frac{e^{-\eta J} - e^{\eta(J+1)}}{1 - e^{\eta}} \quad J_z = -J, \dots, J \\ &= \frac{e^{-\eta(J+1/2)} - e^{\eta(J+1/2)}}{e^{-\eta/2} - e^{\eta/2}} = \frac{\sinh[(J+1/2)\eta]}{\sinh[\eta/2]} \end{aligned}$$

Magnetisation

$$M(T) = -\frac{1}{\mu_0 V} \frac{\partial F}{\partial H} = -\frac{1}{\mu_0 V} \frac{\partial(-k_B T \ln Z)}{\partial H}$$

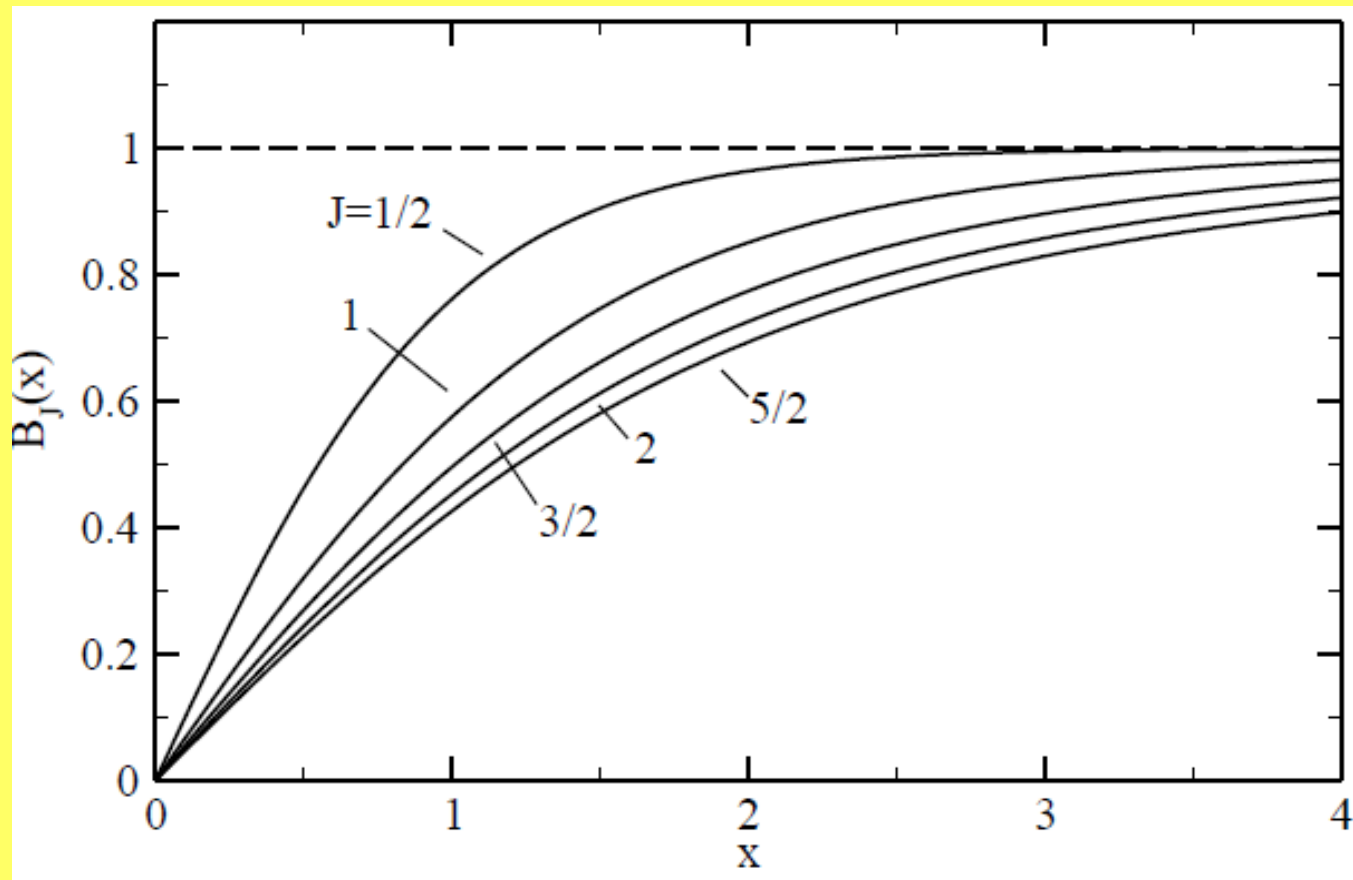
$$= \frac{k_B T}{\mu_0 V} \frac{\partial}{\partial H} [\ln(\sinh[(J+1/2)\eta]) - \ln(\sinh[\eta/2])] = \frac{g(JLS)\mu_B J}{V} B_J(\eta)$$

$$B_J(\eta) = \frac{1}{J} \left\{ \left(J + \frac{1}{2}\right) \coth \left[\left(J + \frac{1}{2}\right) \eta / J \right] - \frac{1}{2} \coth \left[\frac{\eta}{2J} \right] \right\}$$

Reminder: Brillouin functions & Curie law

$$B_J(\eta) = \frac{1}{J} \left\{ \left(J + \frac{1}{2} \right) \coth \left[\left(J + \frac{1}{2} \right) \eta / J \right] - \frac{1}{2} \coth \left[\frac{\eta}{2J} \right] \right\}$$

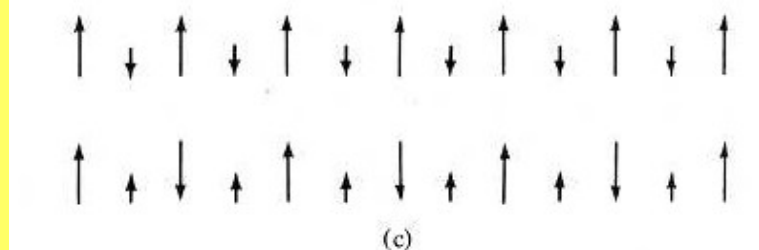
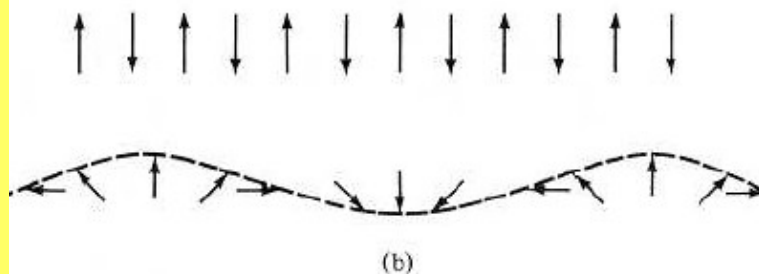
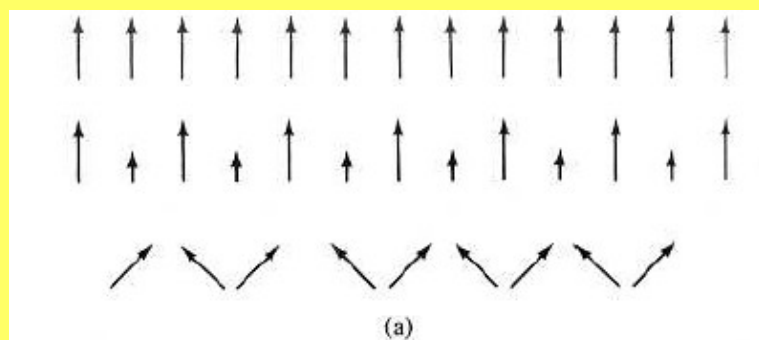
$$\eta = (g(JLS)\mu_B B)/(k_B T)$$



$$B_J(\eta \ll 1) \approx \frac{J+1}{3} \eta + O(\eta^3)$$

$$\chi^{\text{mag,para}}(T) = \frac{\partial M}{\partial H} = \frac{\mu_o \mu_B^2 g^2 (JLS)^2 J(J+1)}{3V k_B} \frac{1}{T} = \frac{C}{T}$$

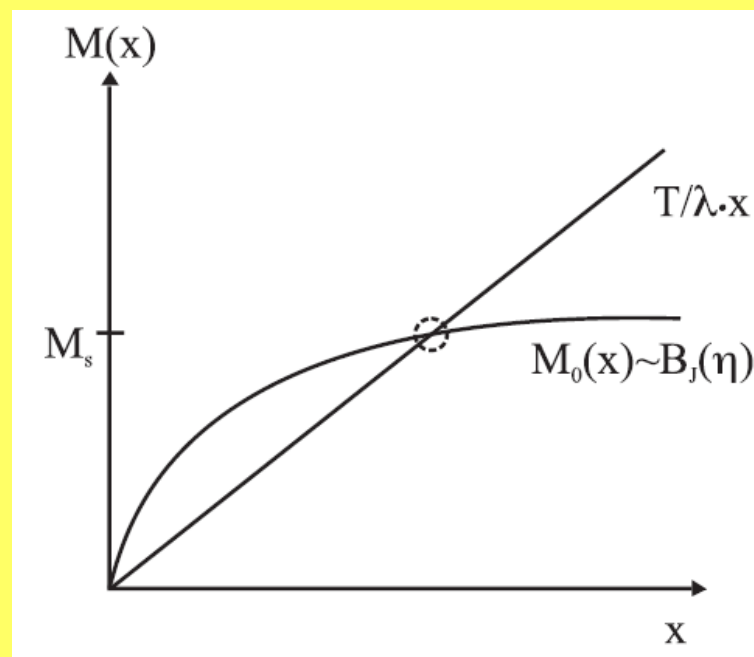
Reminder: magnetic ordering & molecular field theory (Weiss)



$$H^{\text{eff}} = H + H^{\text{mol}} = H + \mu_o \lambda M$$

$$M_0(T) = \frac{g(JLS)\mu_B J}{V} B_J(\eta) \quad \text{with } \eta \sim \frac{H}{T}$$

$$M(T) = M_0 \left(\frac{H_{\text{eff}}}{T} \right) \rightarrow M_0 \left(\frac{\lambda M}{T} \right)$$



Reminder: Heisenberg and Ising hamiltonians

$$H_{i,j}^{\text{coupling}} = -\frac{J_{ij}}{\mu_B^2} \mathbf{m}_i \cdot \mathbf{m}_j$$

J_{ij}

exchange integral (in eV)

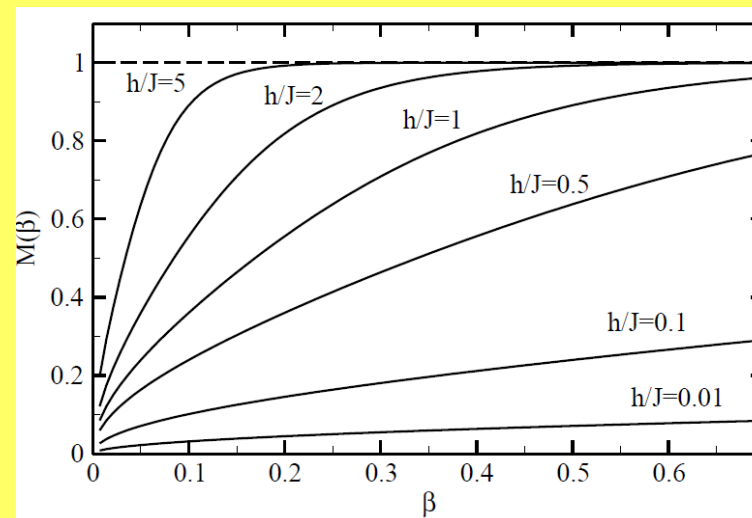
$-J_{ij}m_i m_j / \mu_B^2 \Rightarrow$ ferro $+J_{ij}m_i m_j / \mu_B^2 \Rightarrow$ antiferro

$$H^{\text{Heisenberg}} = \sum_{i,j=1}^M H_{i,j}^{\text{coupling}} = -\sum_{i,j=1}^M \frac{J_{ij}}{\mu_B^2} \mathbf{m}_i \cdot \mathbf{m}_j$$

$$H^{\text{Ising}} = -\sum_{i,j=1}^M \frac{J_{ij}}{\mu_B^2} \underbrace{\mathbf{m}_{i,z} \cdot \mathbf{m}_{j,z}}_{\pm 1 \text{ only}}$$

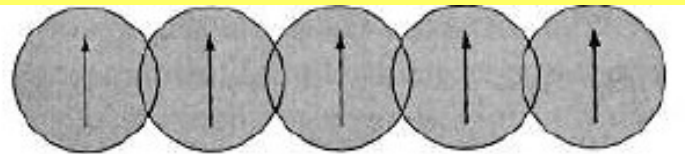
$$H^{\text{Ising}} = -J \sum_{i=1}^N \sigma_i \sigma_{i+1} - h \sum_i \sigma_i$$

1D in magnetic field

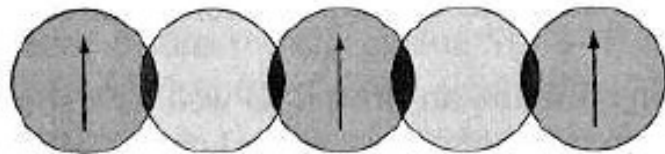


Magnetisation in Ising model

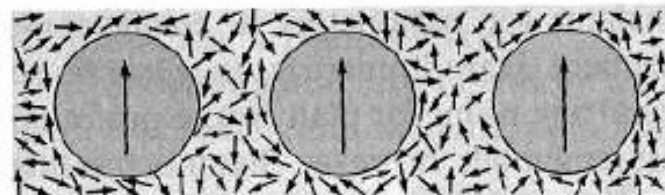
$$\beta = (k_B T)^{-1}$$



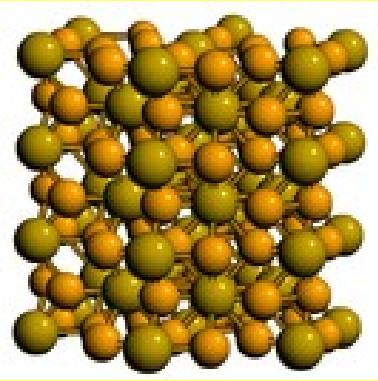
(a) Direct exchange



(b) Super-exchange via non-magnetic ions



(c) Indirect exchange via conduction electrons

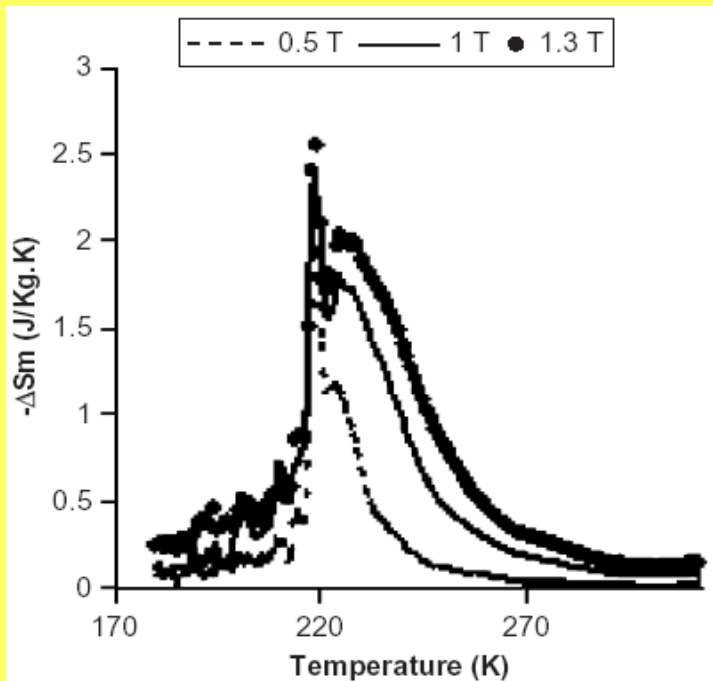


Fe_2P (magneto-elastic transition) at 217 K

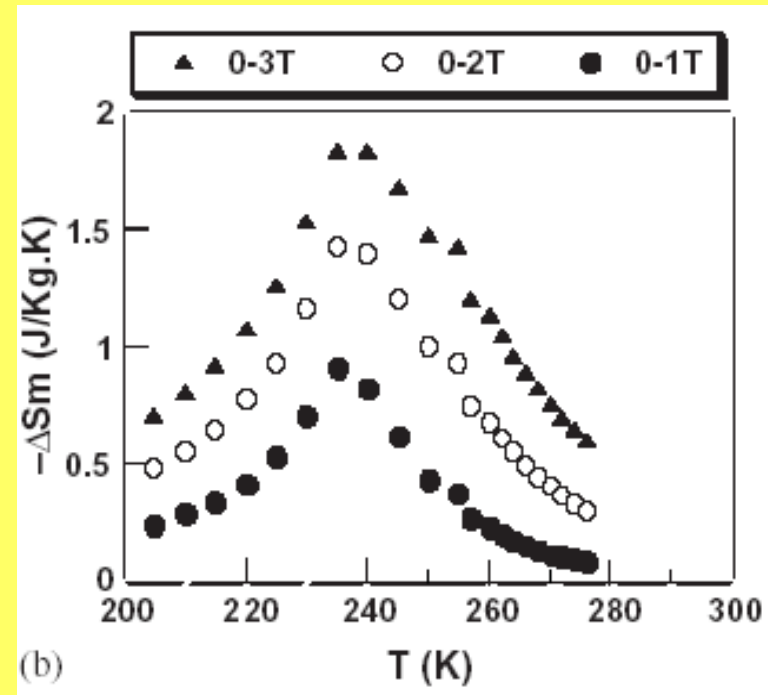
Hexagonal (P-62m, #189) $a = 5.872 \text{ \AA}$, $c = 3.460 \text{ \AA}$, $Z=3$

2 Fe sites: 3f (small magnetic moment) & 3g (large magnetic moment)

T_C increases from 217 K for Fe_2P to 235 K for $\text{Fe}_{1.85}\text{Ru}_{0.15}\text{P}$

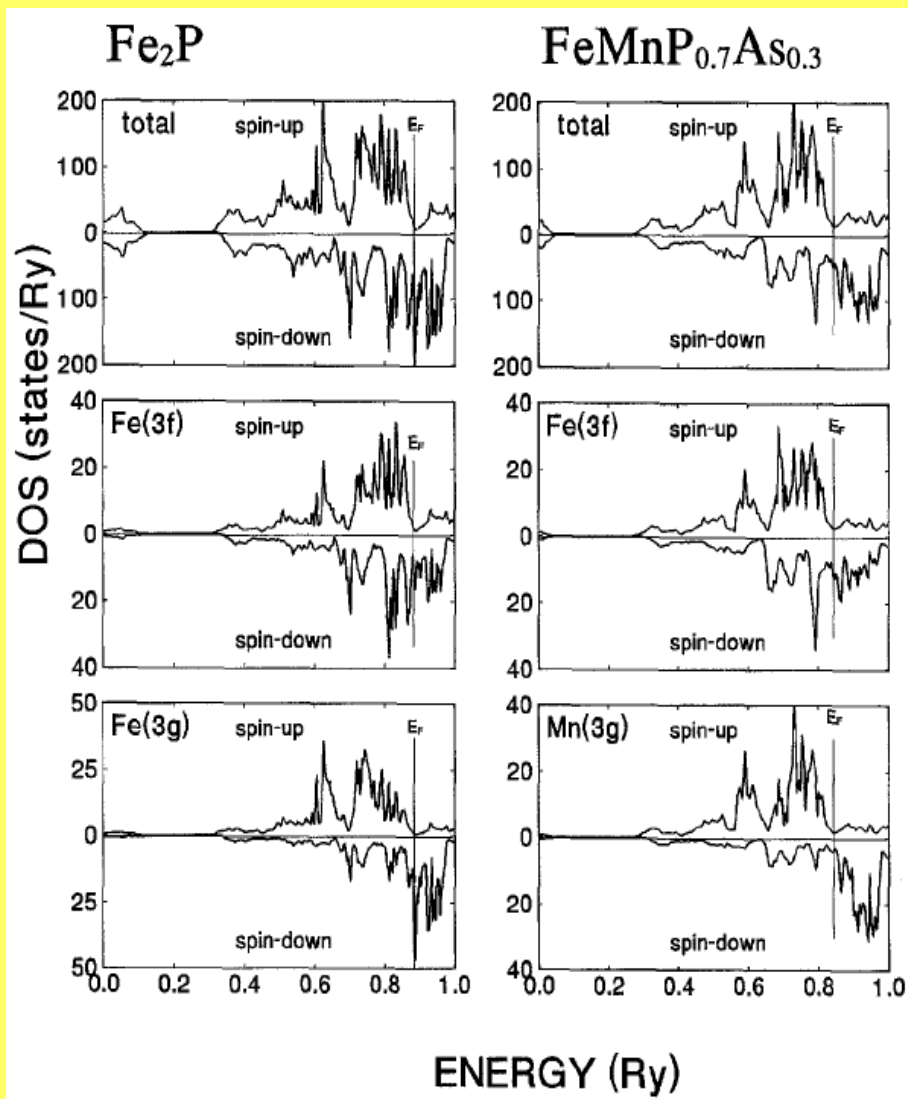


Fruchart et al., Physica A (2005)

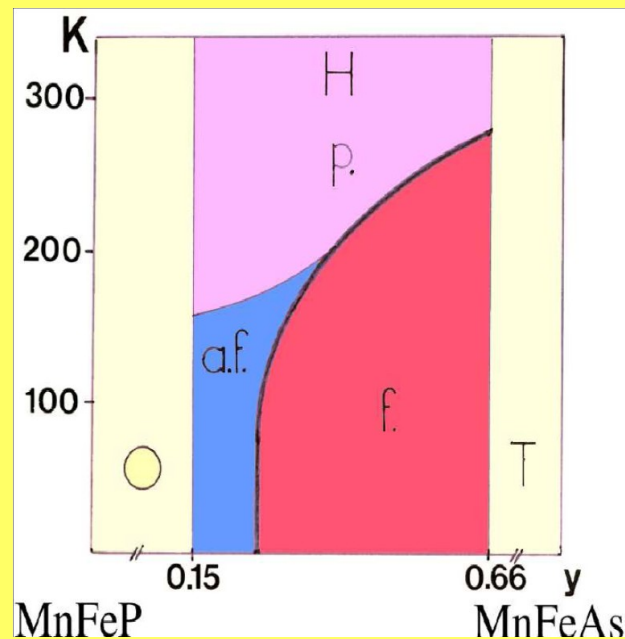


Influence of electrons polarisation at E_F in increase of T_C , presence of small moment $0.4 \mu_B/\text{Ru}$, similar effect in $\text{Fe}_{2-x}\text{Ni}_x\text{P}$

Fe₂P and MnFe(P-As)



Tobola et al., JMMM (1996)



Bacmann et al., JMMM (1994)

MnFe(P-As)

	Neutrons	KKR-CPA
Fe(3f)	1.24	1.25
Mn(3g)	2.55	2.95

Fe₂P

	Neutrons	KKR-MT	KKR-FP
Fe(3f)	0.59	0.80	0.60
Fe(3g)	2.23	2.33	2.40

Calculation of entropy contributions in $\text{Fe}_{2-x}\text{T}_x\text{P}$

$$S_{\text{el}} = -R \int_{E_{\text{min}}}^{\mu_c} dE n(E) [f \ln f + (1 - f) \ln(1 - f)],$$

$$f = f(E, \mu_c, T) = \frac{1}{\exp[(E - \mu_c)/k_B T] + 1}$$

$$N_{\text{val}} = \int_{E_{\text{bottom}}}^{\mu_c} dE n(E) f(E, \mu_c, T),$$

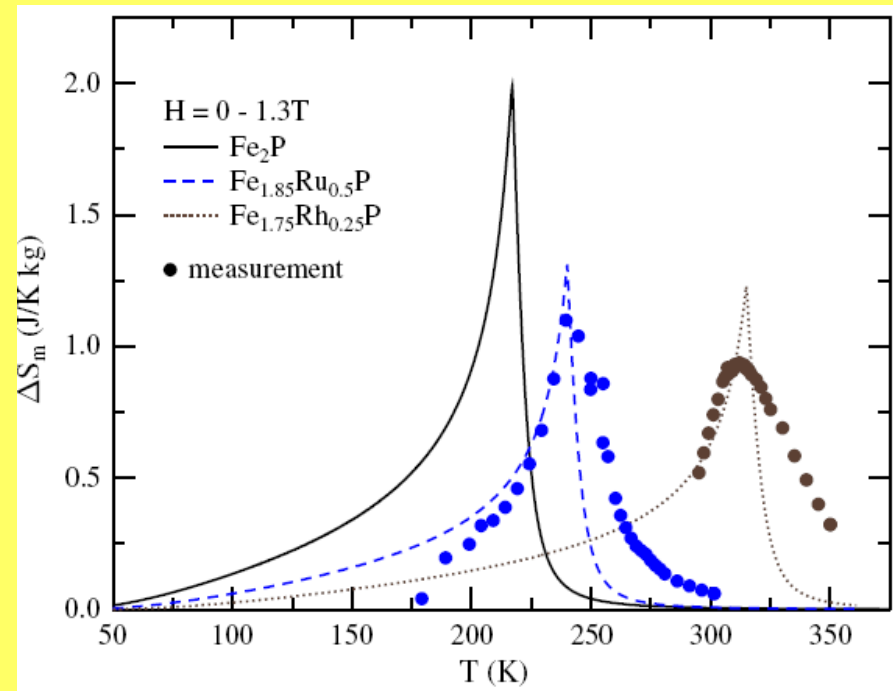
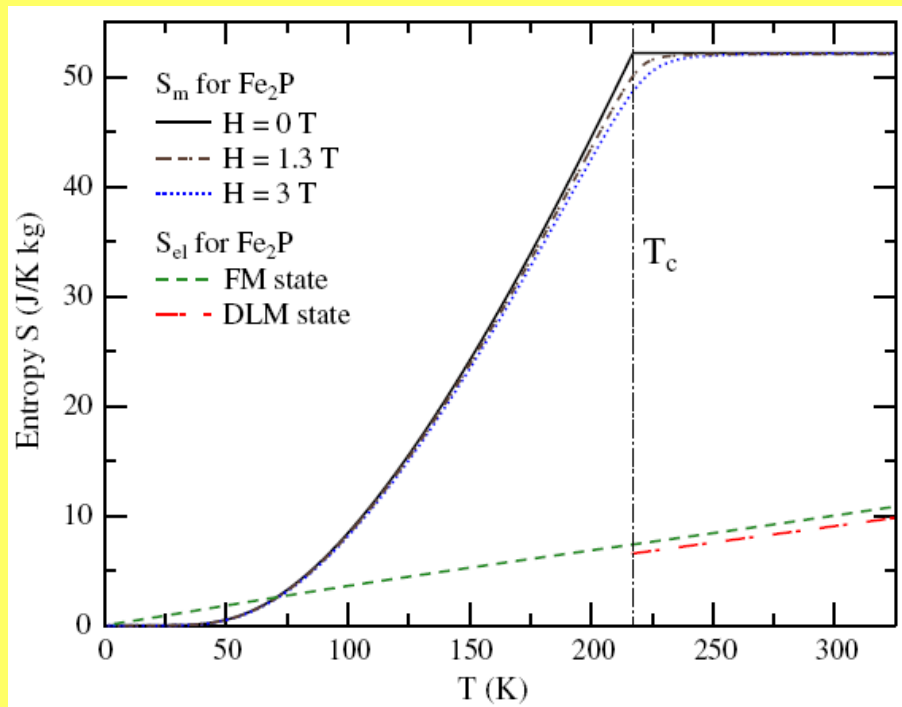
$$S_{\text{tot}} = S_{\text{el}} + S_{\text{m}} + S_{\text{lat}}.$$

$$\Delta S(H_{\text{max}}) = \int_0^{H_{\text{max}}} \left(\frac{\partial M}{\partial T} \right)_H dH$$

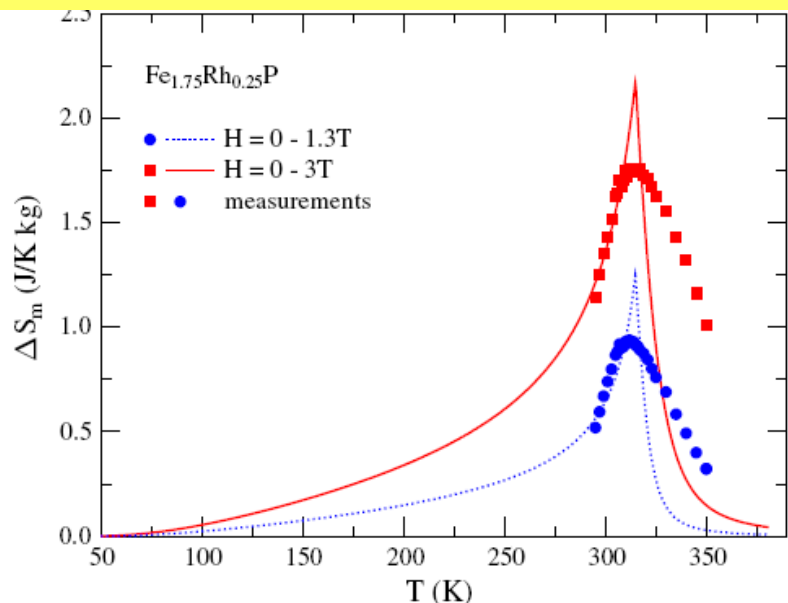
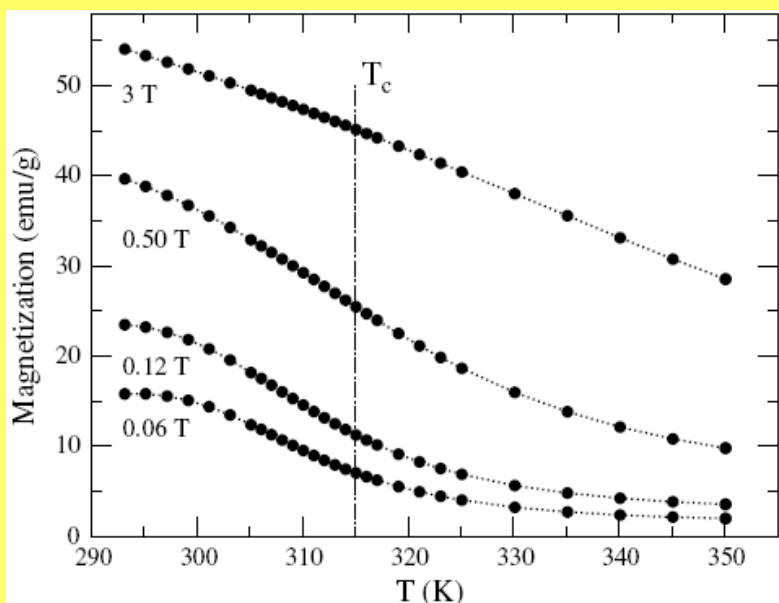
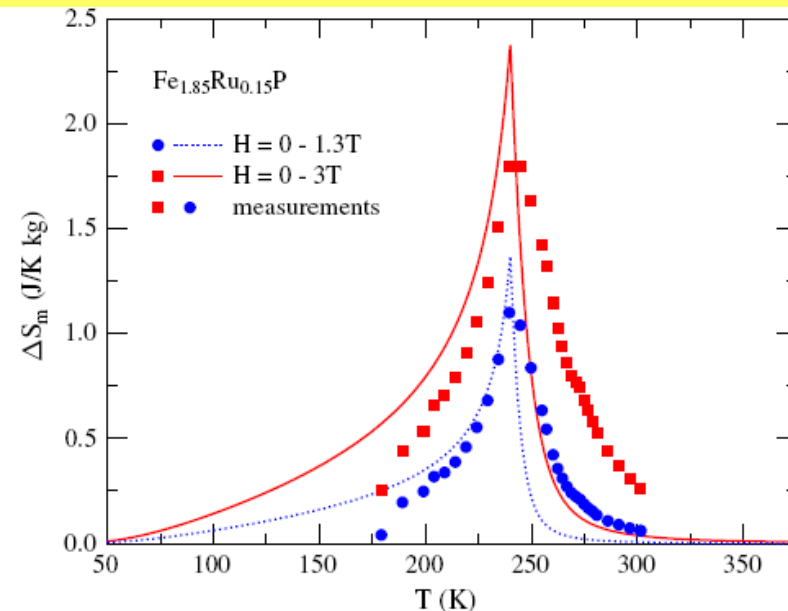
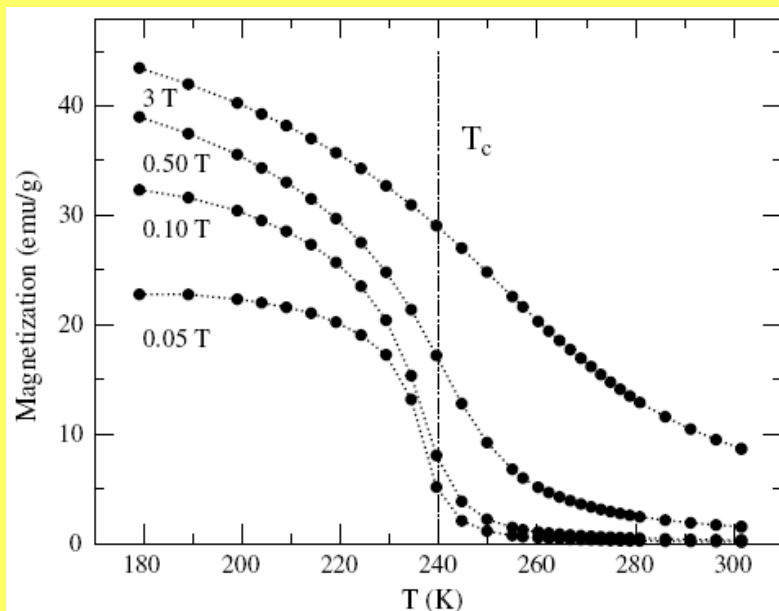
$$S_{\text{m}} = R \left[\ln \frac{\sinh \frac{2J+1}{2J} x}{\sinh \frac{1}{2J} x} - x B_J(x) \right]$$

$$x = \frac{g \mu_B J H}{k_B T} + 3 \frac{T_C}{T} \frac{\mu(T)}{g \mu_B (J+1)}$$

$$S_{\text{m}}^{\text{max}} = R \ln(2J + 1)$$



Entropy from electronic structure KKR-CPA & MFT



Simulations of electronic structure above Curie temperature

DLM (*disordered local moments*)

1. Analogy with chemical alloy within the coherent potential approximation) CPA **with 2 atoms on 1 site**.
2. **atom A – Fe^{up}** (iron with magnetic moment 'up')
atom B – Fe^{down} (iron with magnetic moment 'down')
3. **A** and **B** atoms occupy the same crystallographic site.
4. For concentration 50% the total magnetic moment per site and unit cell is zero, but the 'local' magnetic moments may be **non-zero**.
5. CPA medium is used to **randomly distribute the magnetic moments** among the sites (like in **paramagnetic state**)

KKR+CPA

$T_C = 1250 \text{ K}$

Experiment

$T_C = 1044 \text{ K}$

Ferromagnetic phase transitions in metals

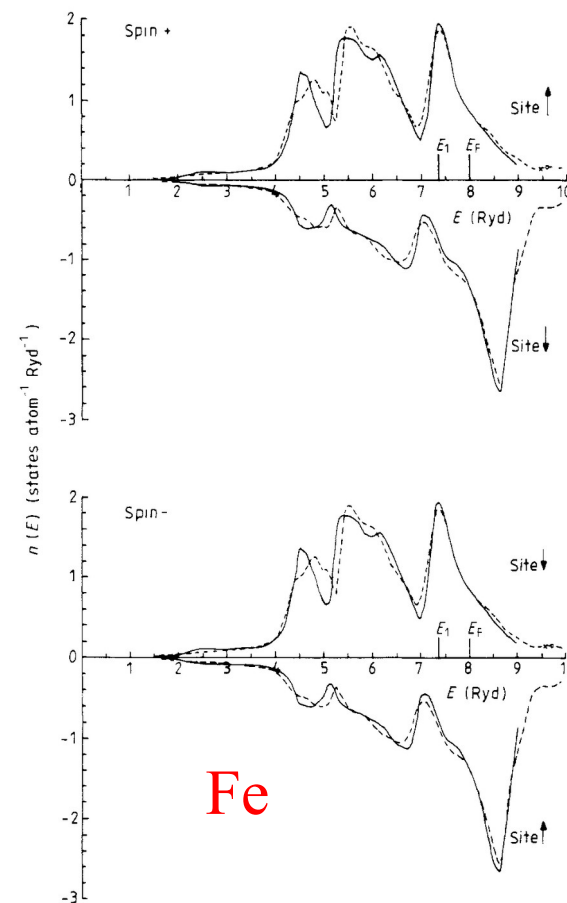


Figure 3. Density of states for Fe in its paramagnetic disordered local moment state.

Gyorffy et al., J. Phys. F (1985)

Ground state properties

KKR-CPA code

Total density of states DOS

$$N(E) = -\frac{1}{\pi} \text{Im} \int_{-\infty}^E dE G(E)$$

Component, partial DOS

$$\rho_{\sigma}(E) = \frac{\partial}{\partial E} N_{\sigma}(E).$$

Total magnetic moment

$$\mu = N_{+}(E_F) - N_{-}(E_F)$$

Spin and charge densities

$$\rho_{\sigma}^{(k)}(\mathbf{r}) = -\frac{1}{\pi} \int_{-\infty}^{E_F} dE \langle \sigma, \mathbf{r} + \mathbf{a}_k | G(E) | \sigma, \mathbf{r} + \mathbf{a}_k \rangle$$

Local magnetic moments

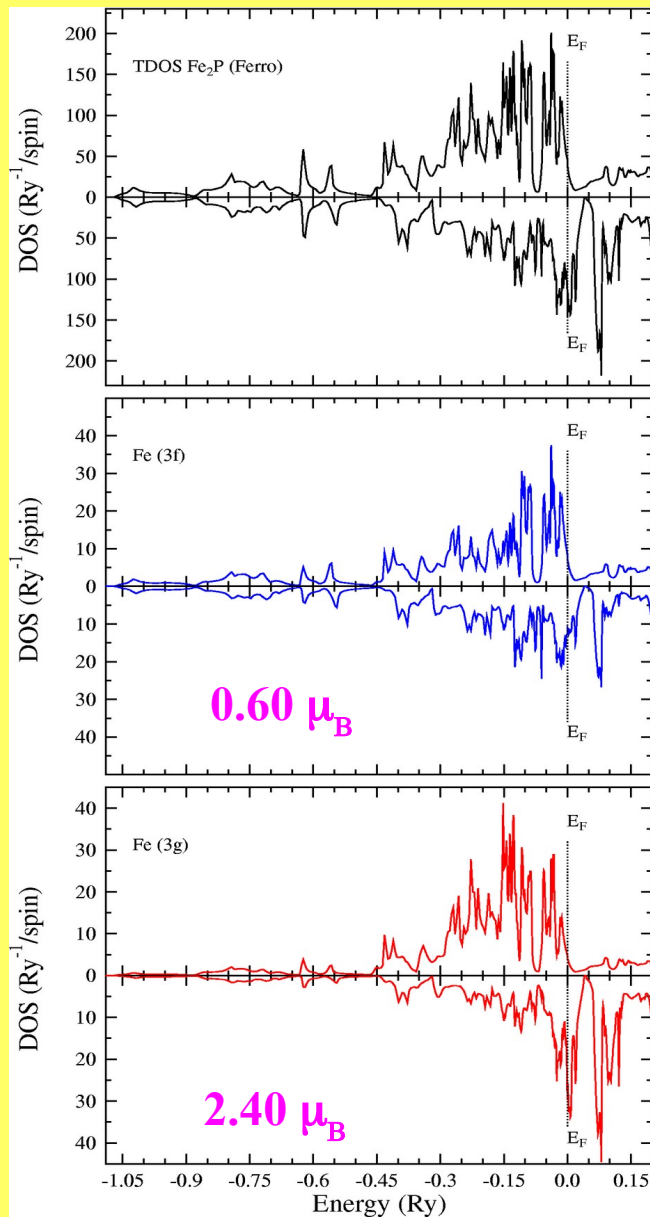
$$\mu^{(k)} = \mu_B \int_{\Omega_k} d^3r s^{(k)}(\mathbf{r})$$

Fermi contact hyperfine field

$$H_{Fermi} = \frac{8}{3} \pi \mu_B [\rho_{\uparrow}(0) - \rho_{\downarrow}(0)]$$

Bands $E(\mathbf{k})$, total energy, electron-phonon coupling, magnetic structures, transport properties, photoemission spectra, Compton profiles, ...

Fe₂P (ferromagnetic vs. 'paramagnetic' DLM state)

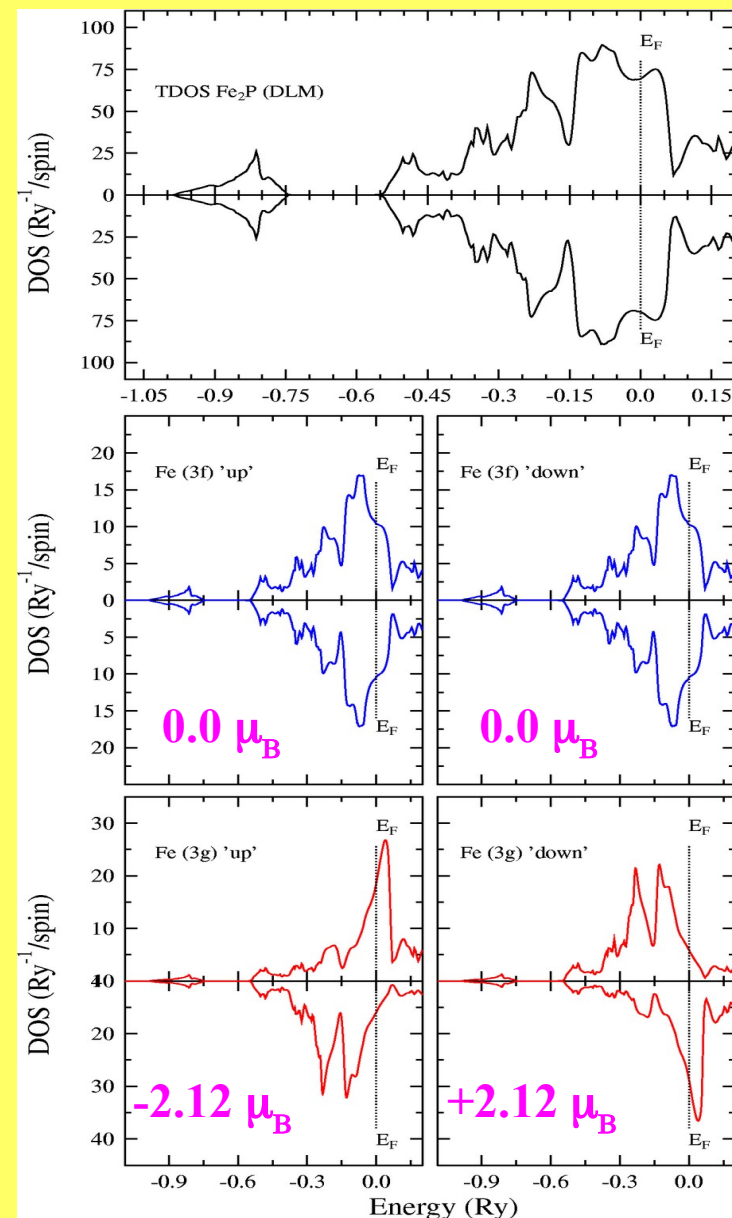


Disappearance of magnetic moment on one crystallographic site strongly modify entropy of PM state with respect to FM state:

huge entropy jump

WHAT IS NEEDED to have strong MCE!!

In computations all atoms are treated independently, so to obtain zero magnetisation from non-zero magnetic moments of atoms is not authomatic, time-consuming calculations

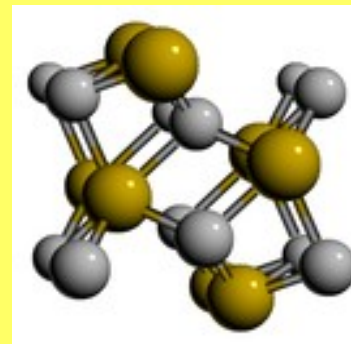


MnAs (magneto-structural transition) at 318 K



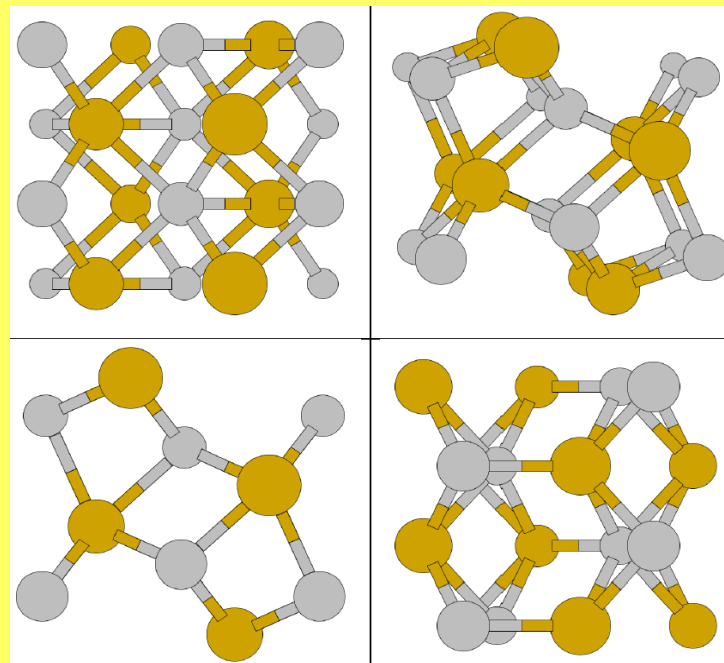
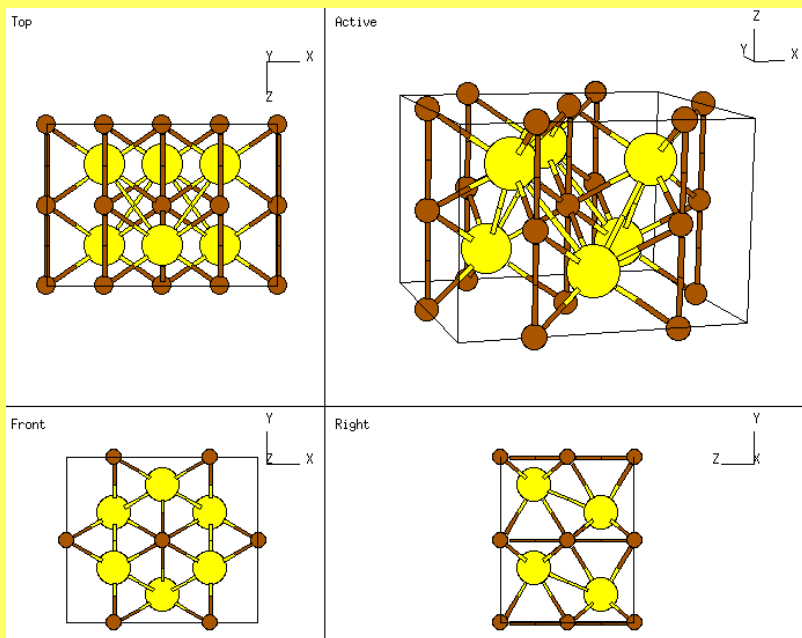
Hexagonal NiAs-type structure
(P63/mmc, #194)

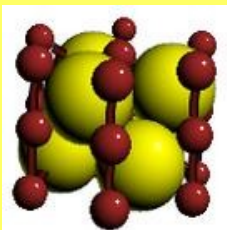
$a = 3.730 \text{ \AA}$, $c = 5.668 \text{ \AA}$, $Z=2$



Orthorhombic MnP-structure
(Pnma, #62)

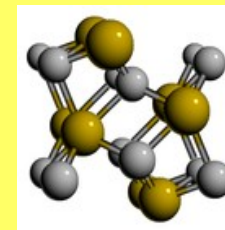
$a = 5.72 \text{ \AA}$, $b = 3.676 \text{ \AA}$, $c = 6.379 \text{ \AA}$, $Z=4$



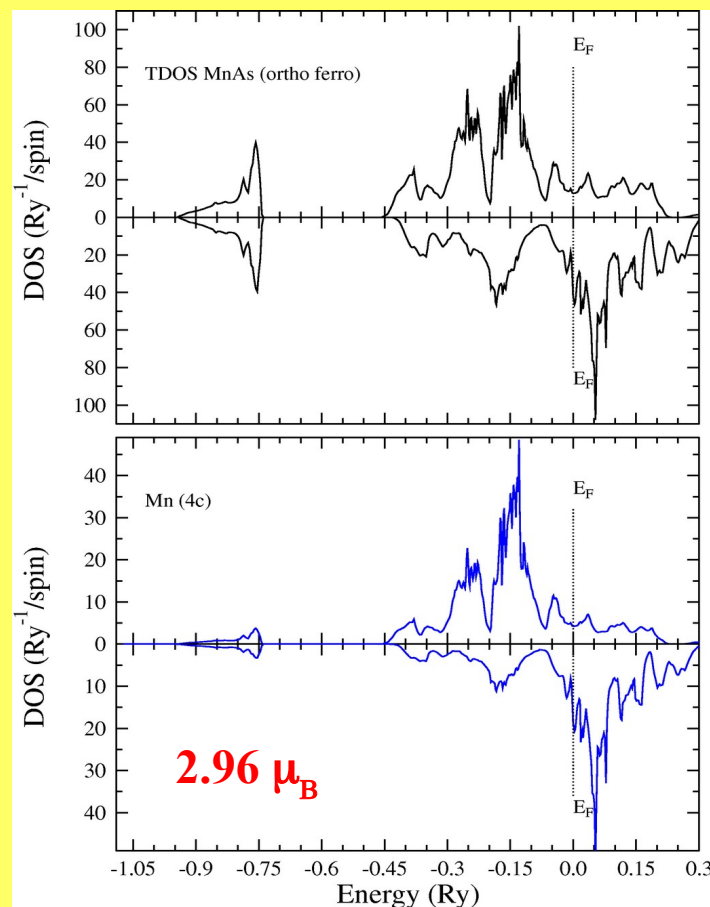
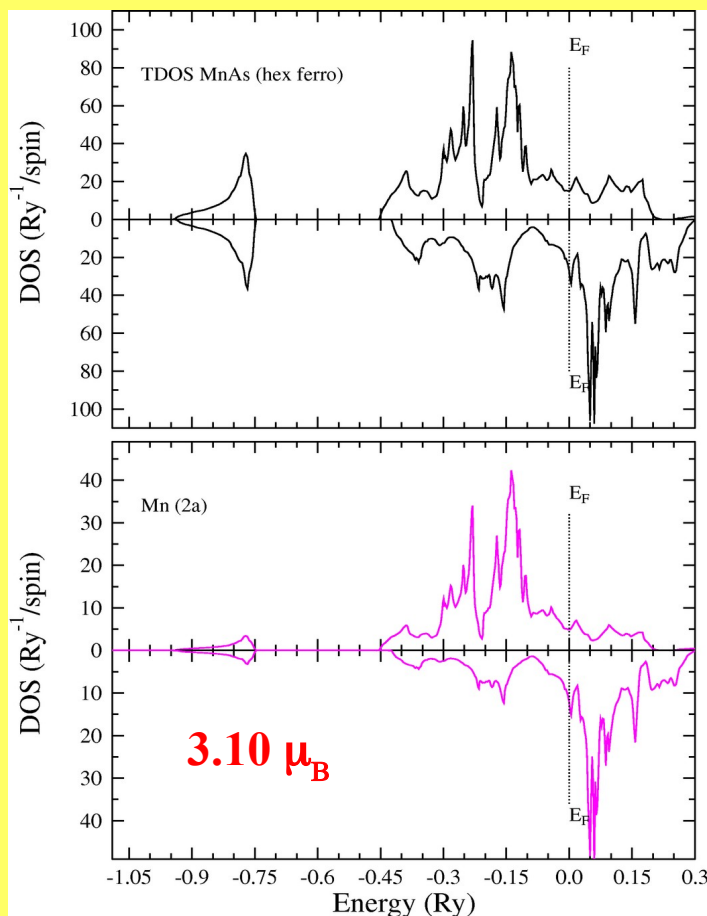


NiAs-type

MnAs in ferromagnetic state



MnP-type



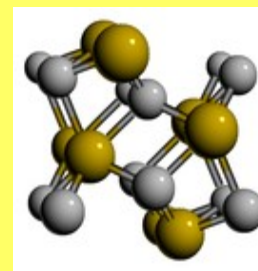
In excellent agreement with neutron diffraction data : $3.14 \mu_B$



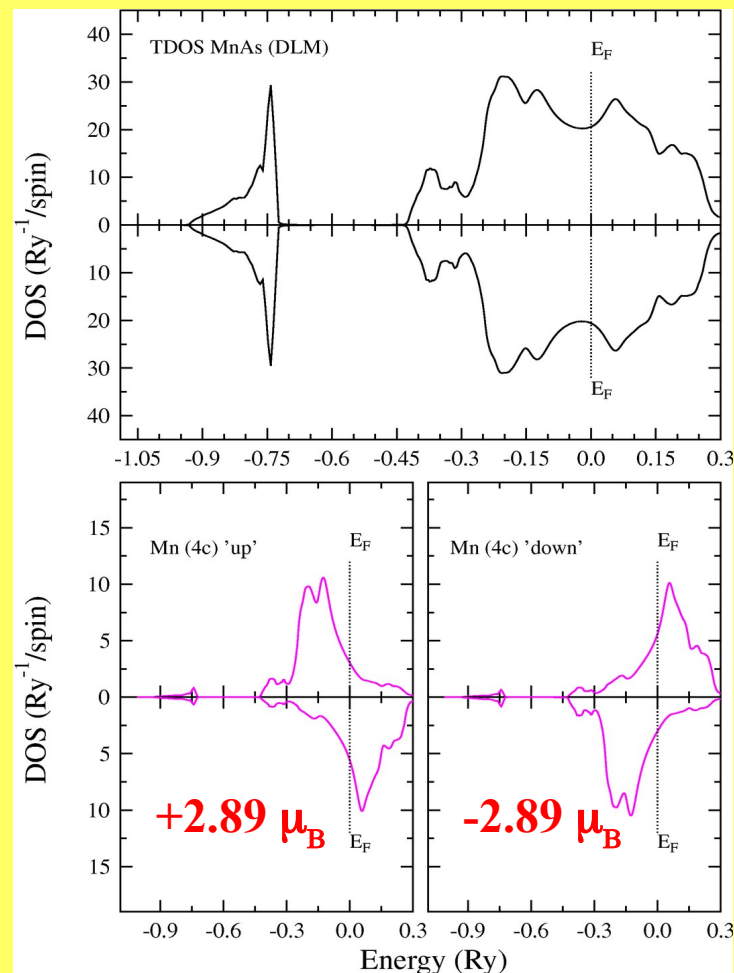
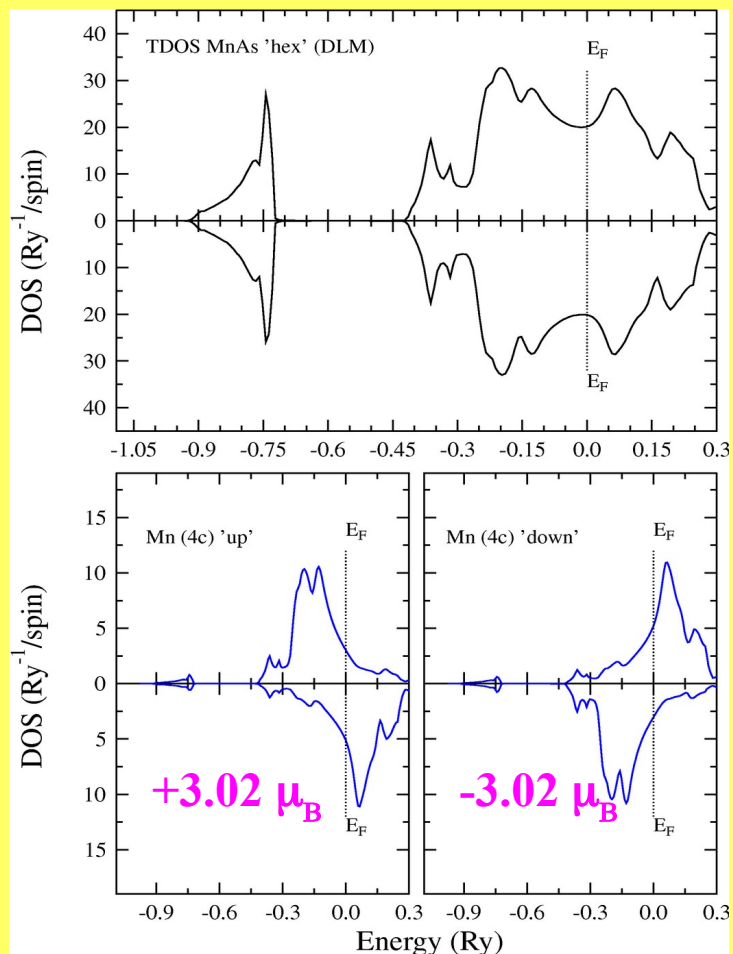
NiAs-type

MnAs in 'paramagnetic' state

DLM (disordered local moments)



MnP-type

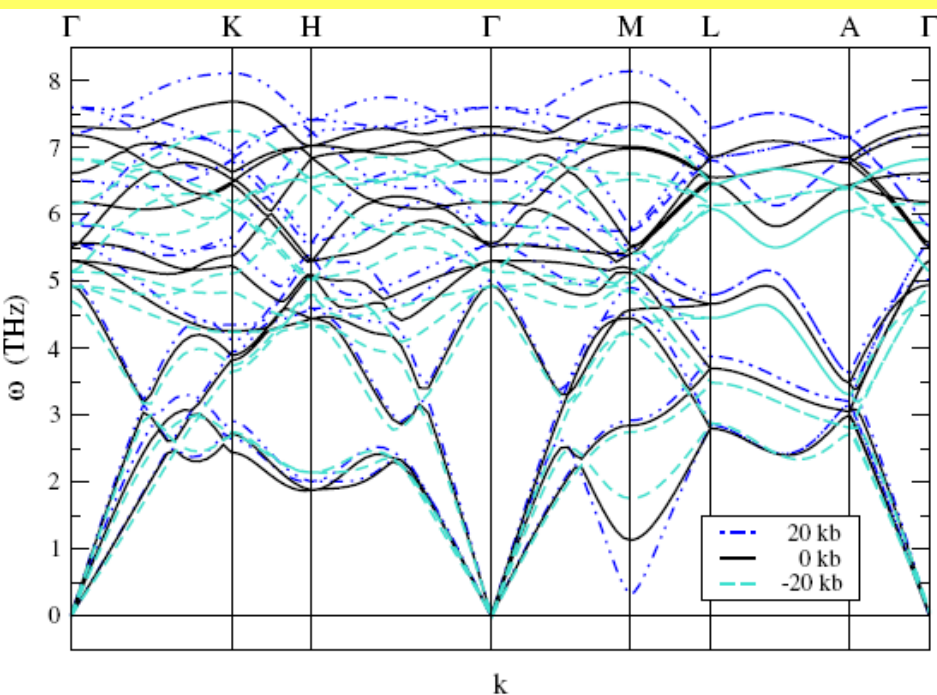


MnAs

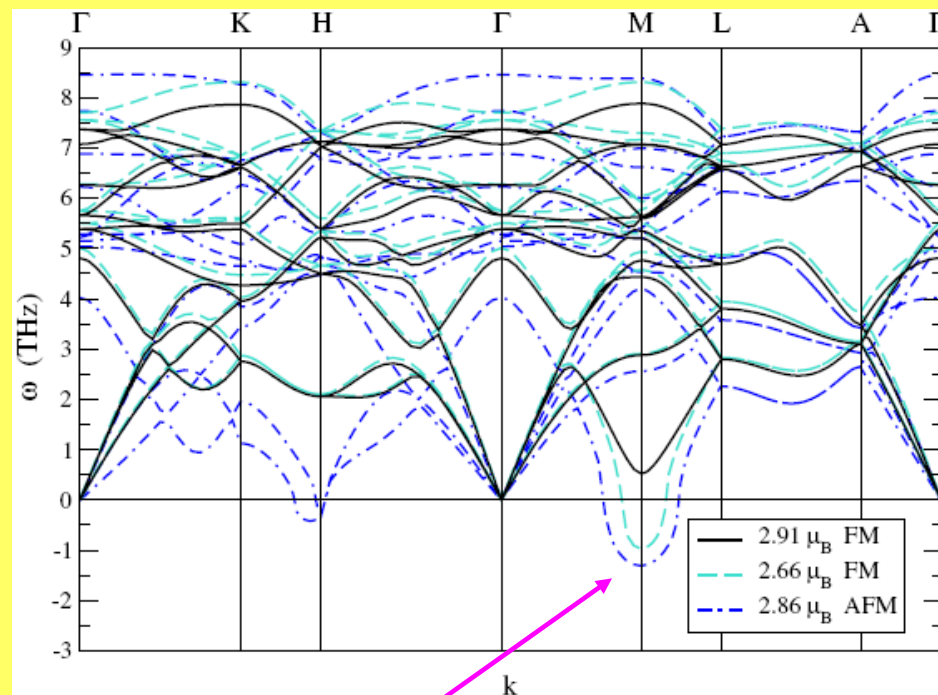
phonon mechanism of magneto-structural phase transition

$$P6_3/mmc \rightarrow [M_2^+, \mathbf{k} = (0.5, 0, 0)] \rightarrow Pnma.$$

Hexagonal NiAs-type structure



Orthorhombic MnP-structure

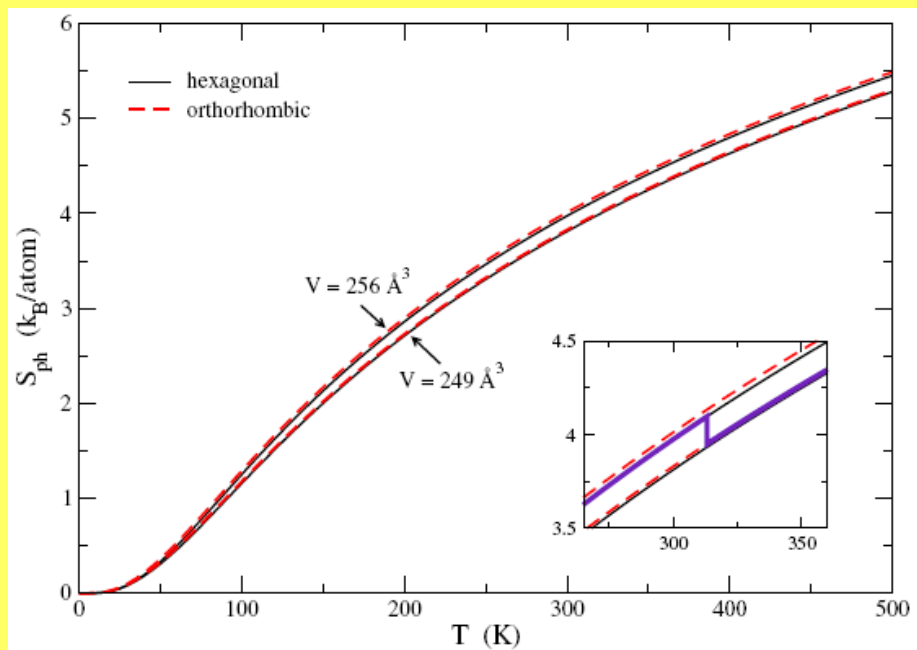


volume contraction ($\Delta V/V \sim 2\%$) near
Curie temperature

soft mode near M point (phonon calculations)

MnAs

phonon mechanism of magneto-structural phase transition

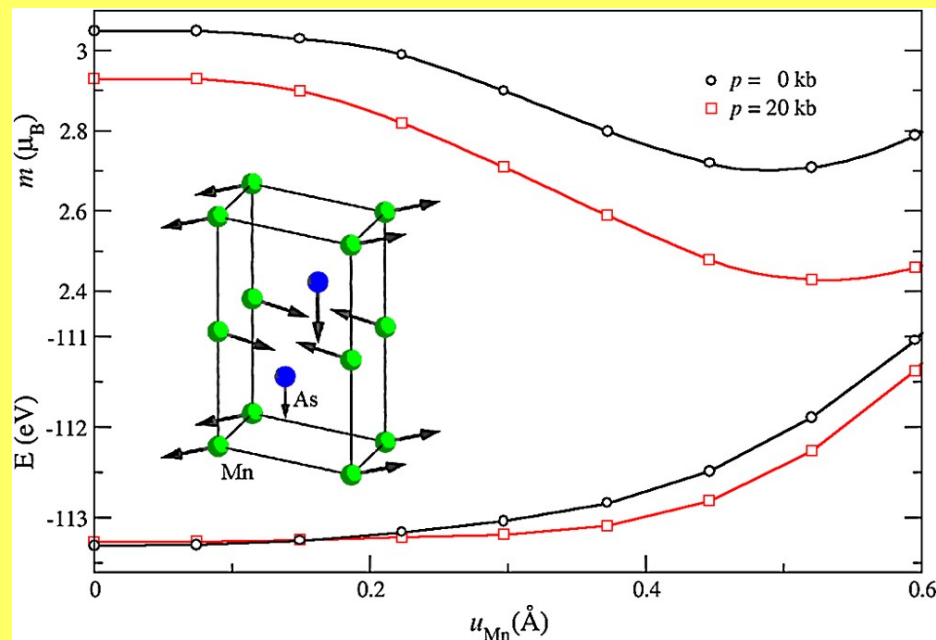


$$S_{\text{tot}} = S_{\text{el}} + S_{\text{m}} + S_{\text{lat}}$$

experiment $\Delta S_{\text{tot}} = -30 \text{ J/(K kg)}$ for $\Delta B = 5 \text{ T}$

theory $\Delta S_{\text{lat}} = +9.3 \text{ J/(K kg)}$

Entropy jump mainly related to magnetic entropy



giant coupling between the soft mode and magnetic moments

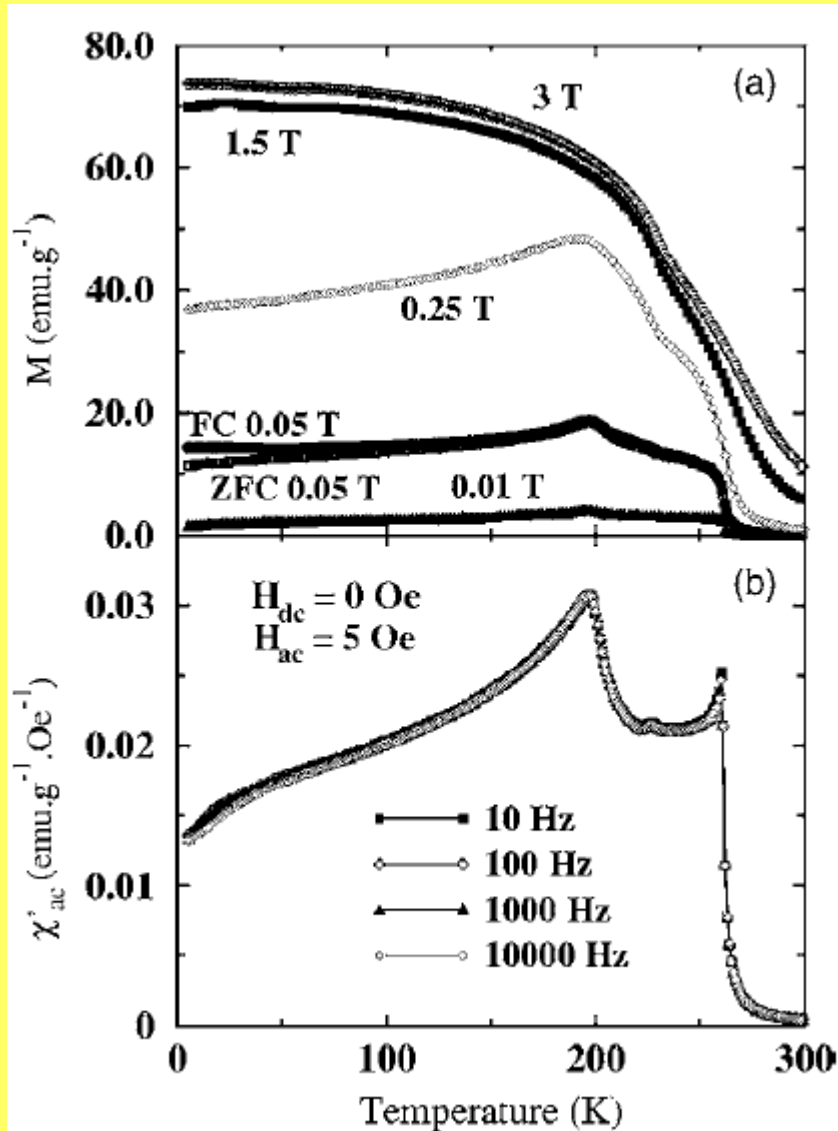
$$\omega = \omega_0 + \lambda \langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle$$

$\lambda \sim 4 \text{ THz}$

$$\langle \mathbf{S}_i \cdot \mathbf{S}_j \rangle = S^2 = \frac{1}{4} m^2$$

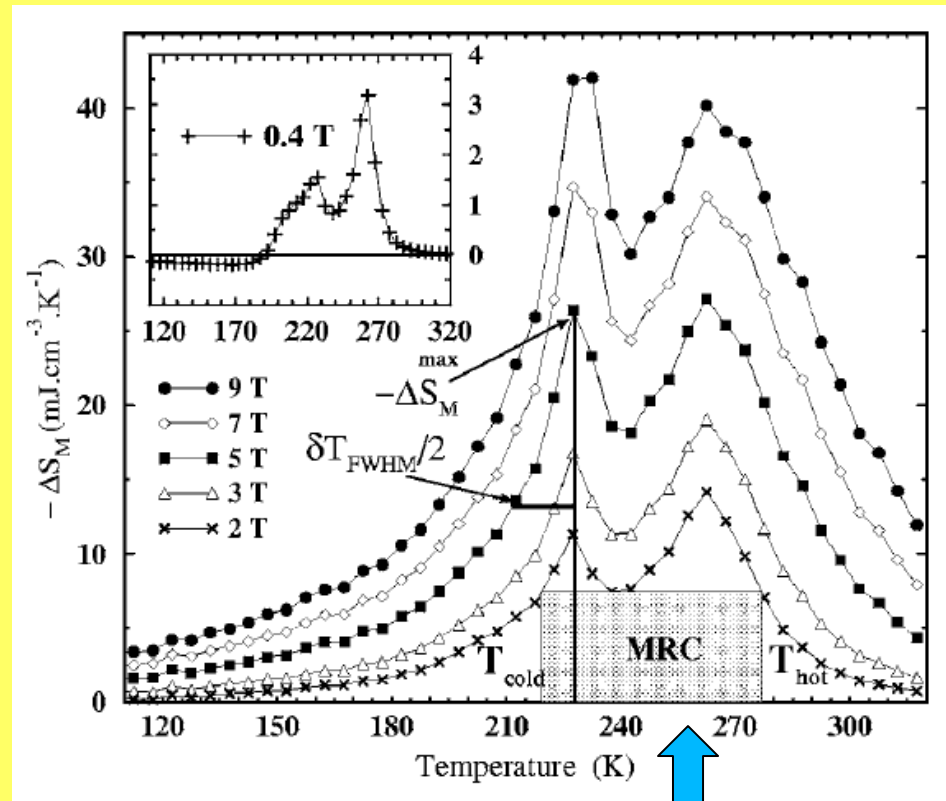
Magnetocaloric effect in Mn_3Sn_2 (i)

Magnetisation curves $M(B, T)$



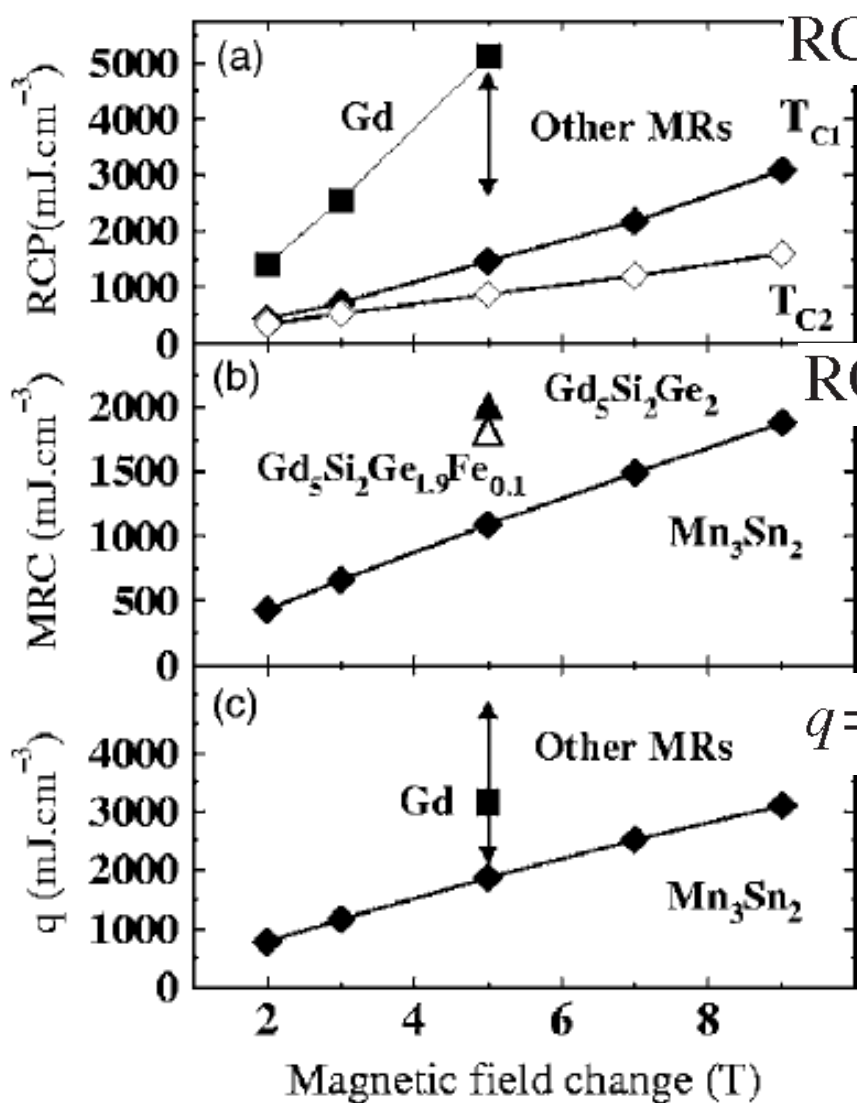
Mazet, Ihou-Mouko, and Malaman, Appl. Phys. Lett. 89, 022503 (2006)

Magnetic entropy



MRC - maximum refrigerant capacity

Magnetocaloric effect in Mn_3Sn_2 (ii)



$$\text{RCP} = -\Delta S_M^{\text{max}} \times \delta T_{\text{FWHM}}$$

Mazet, Ihou-Mouko, and Malaman, Appl. Phys. Lett. **89**, 022503 (2006)

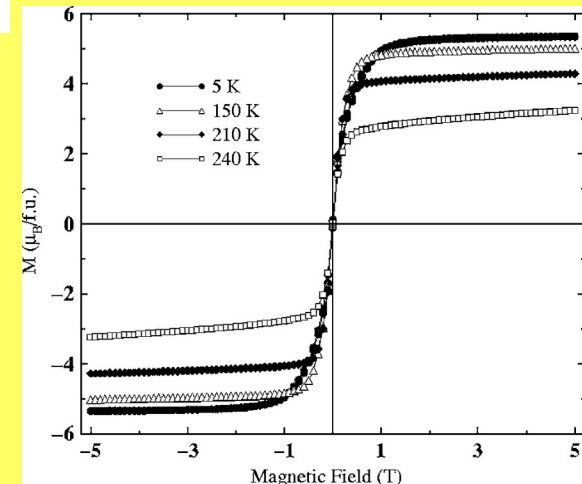
$$\text{RC} = -\Delta S_M \Delta T_{\text{cycl}}$$

MRC = max of RC

$$q = -\int_{T_1}^{T_2} \Delta S_M(T) dT$$

$$\text{RCP} \sim 4/3 q$$

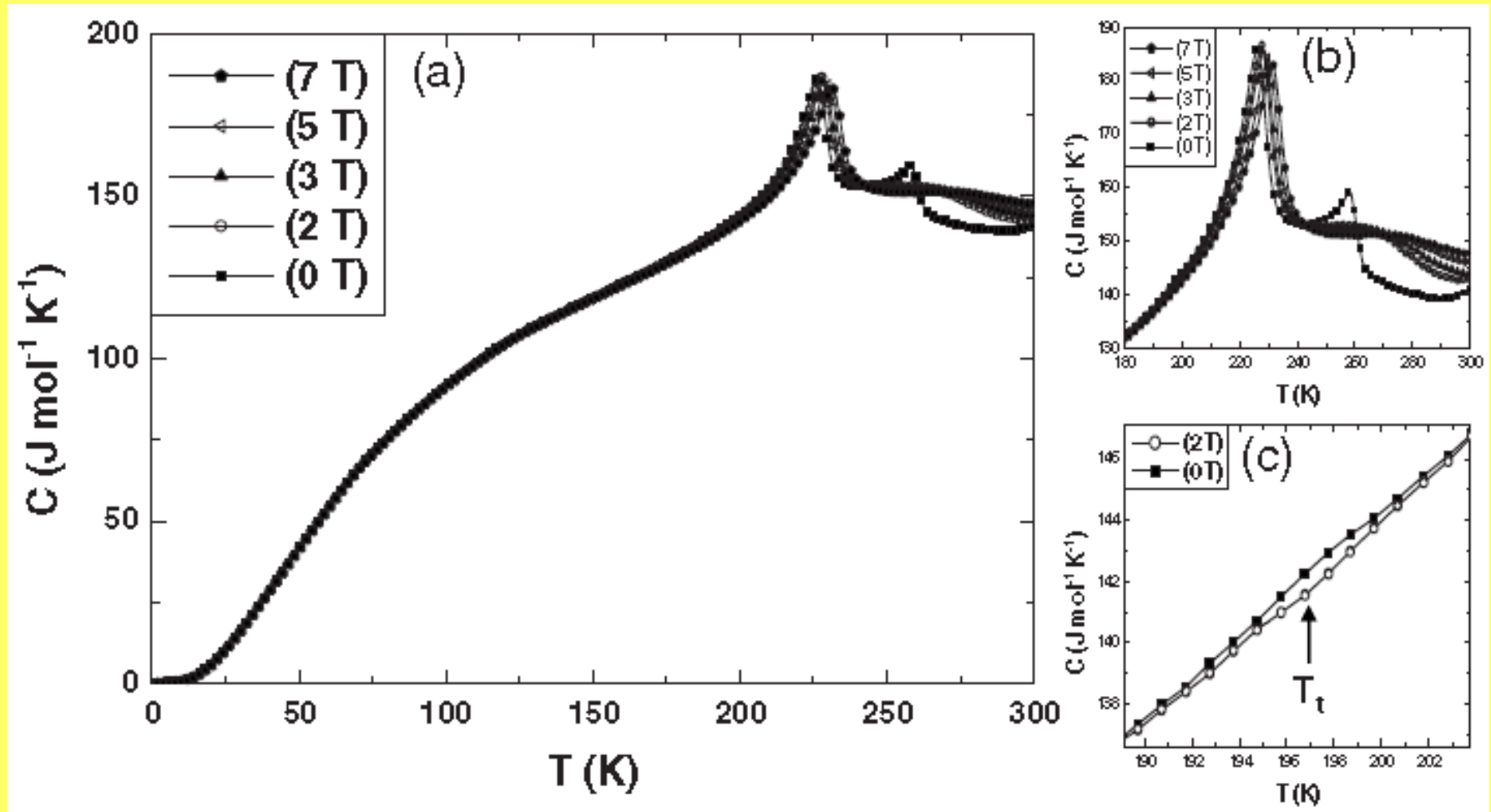
Hysteresis loops



MCE „figure of merit”

Magnetocaloric effect in Mn_3Sn_2 (iii)

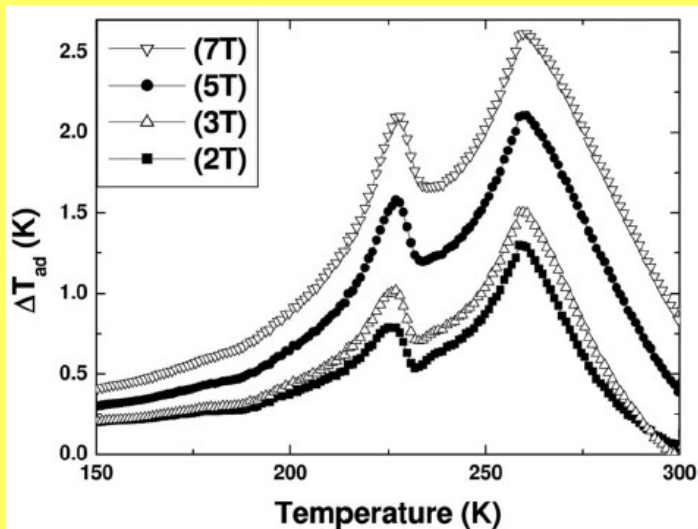
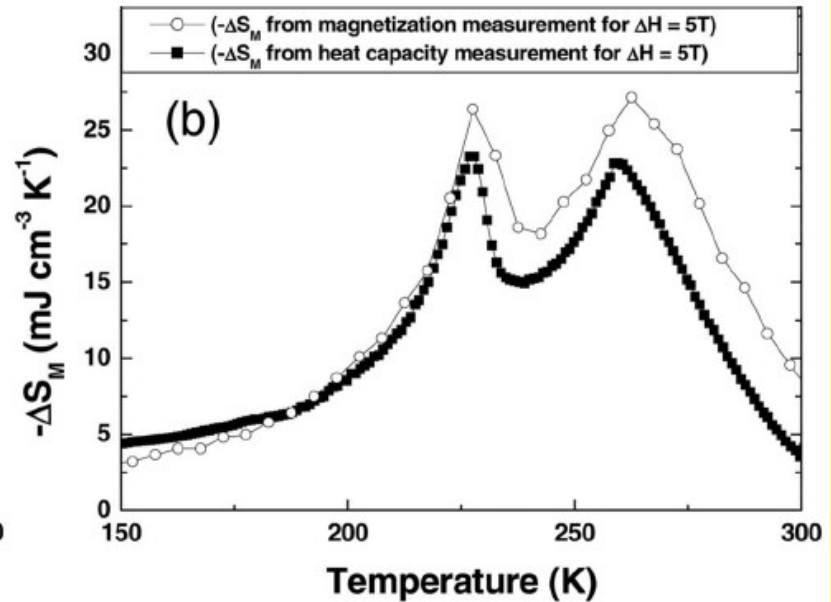
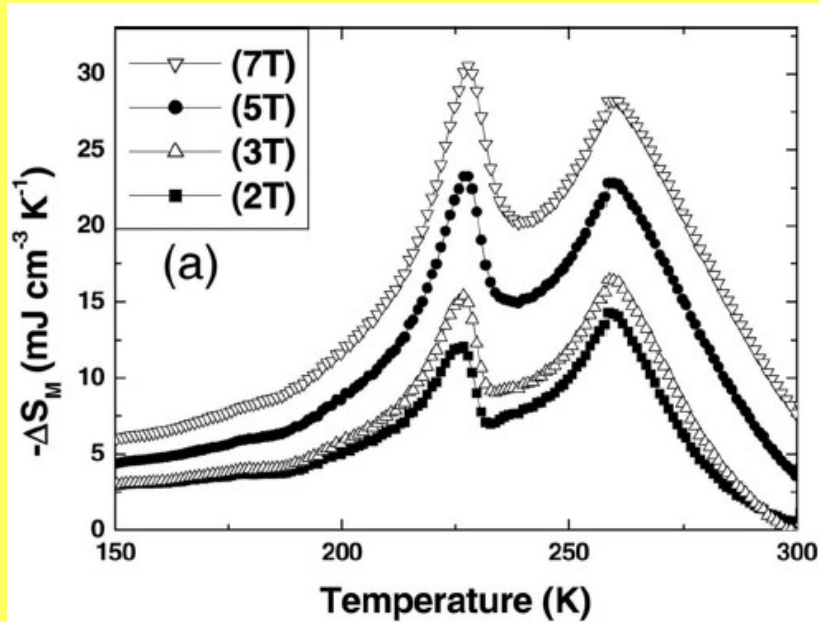
Heat capacity $C(T, H)$



Recour, Mazet, and Malaman J. Appl. Phys. **105**, 033905 (2009)

Magnetocaloric effect in Mn_3Sn_2 (iv)

Entropy change from magnetisation & heat capacity measurements



Recour, Mazet, and Malaman,
J. Appl. Phys. **105**, 033905 (2009)



Adiabatic temperature change

Summary

- **First principle calculations** – helpful in interpretation and description of magnetocaloric materials. Best way is to combine electronic structure and phonon calculations to enabling to estimate entropy jump near transition temperature-crucial for large MC effect.
- **The concept of DLM** were successfully applied to study complex MCE systems: MnAs, MnFe(As-P), Fe₂P by simulating paramagnetic state from KKR-CPA .

Illustrative examples

- **MnAs** - the calculated magnetic moment on Mn in DLM state (ortho) is comparable to FM state (hex), likely promoting large entropy jump near transition; phonon mechanism responsible for hex-ortho magneto-structural phase transition; giant spin-phonon coupling; Mn_{1-x}T_xAs - remarkable variation of local magnetic moments with T impurity.
- **Fe₂P** - the magnetic moment appearing on Fe(3f) in FM state, completely vanishes in DLM state, while that one on Fe(3g) remains only slightly smaller. with respect to the FM state; MFT + KKR-CPA nicely reproduce entropy jump in disordered alloys.
- **Mn₃Sn₂** - with two second-order magnetic transitions very interesting compound for MCE cooling ; more difficult for calculations – noncollinear magnetism.