

**Opis zjawisk transportu elektronów
w materii skondensowanej
*konwersja termoelektryczna***

Pierwsza kwantowa teoria elektronów w metalach (model Drude-Sommerfeld) - przypomnienie

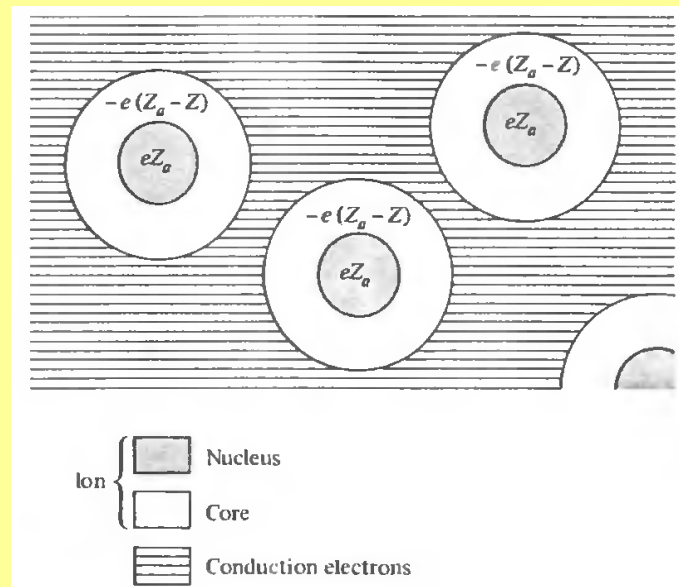
1838 Michael Faraday obserwuje przepływ prądu przez rozrzedzone powietrze, pomiędzy anodą i katodą wytwarza się łuk świetlny oprócz okolicy katody (tzw. ciemnia Faradaya) odkrycie promieni katodowych

1897 Joseph John Thomson odkrywa elektron w podobnym eksperymencie, ale z przyłożonym poprzecznym polem \mathbf{E} , którym można kierować wiązkę „promieni katodowych”; wyznacza e/m .

1900 Paul Drude formułuje pierwszą elektronową teorię metali

1927 Arnold Sommerfeld używa statystyki Fermiego-Diraca do modelu Drudego i proponuje pierwszą kwantową teorię ruchu elektronów w metalach dając początek tzw. modelowi Drudego-Sommerfelda elektronów swobodnych.

$$\mathbf{j} = -e n \mathbf{v}$$



Współczynnik Halla wybranych pierwiastków w słabych i średnich polach B.

METAL	VALENCE	$-1/R_H nec$
Li	1	0.8
Na	1	1.2
K	1	1.1
Rb	1	1.0
Cs	1	0.9
Cu	1	1.5
Ag	1	1.3
Au	1	1.5
Be	2	-0.2
Mg	2	-0.4
In	3	-0.3
Al	3	-0.3



dobra
zgodność



słaba zgodność



niezgodność

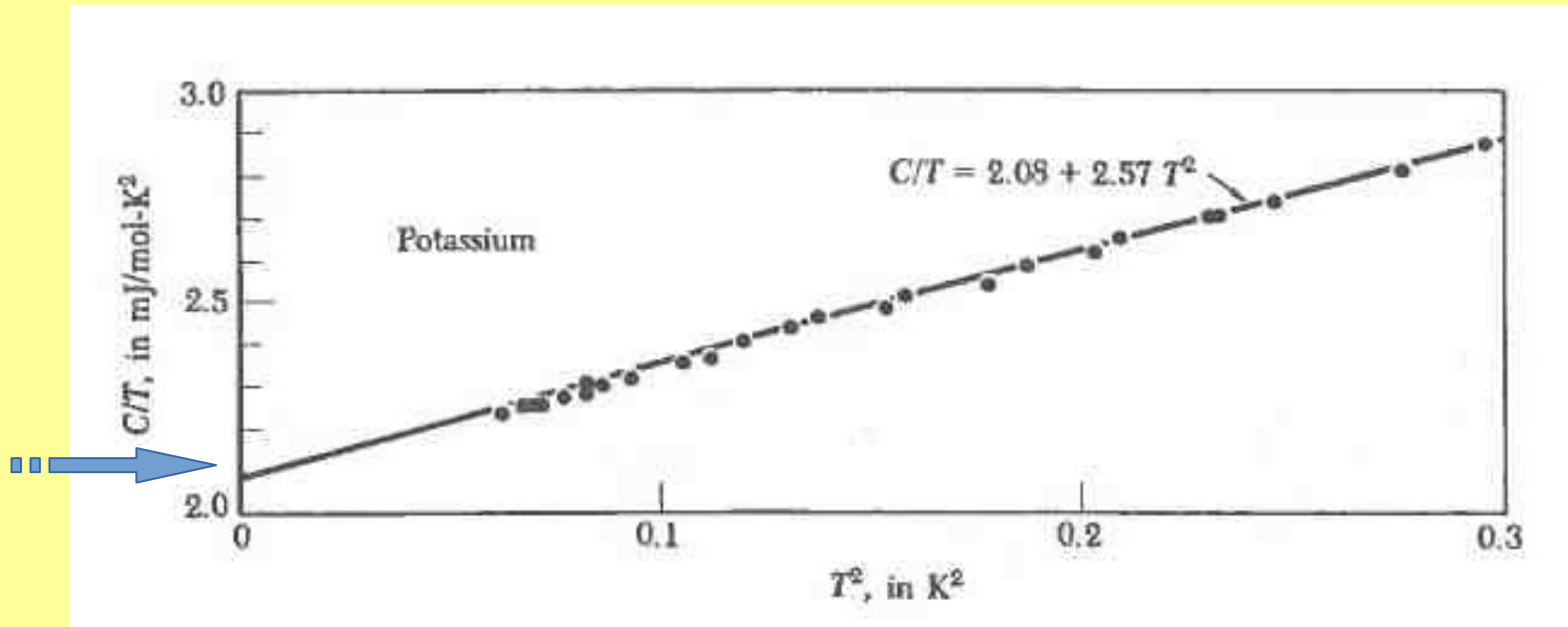
^a These are roughly the limiting values assumed by R_H as the field becomes very large (of order 10^4 G), and the temperature very low, in carefully prepared specimens. The data are quoted in the form n_0/n , where n_0 is the density for which the Drude form (1.21) agrees with the measured R_H : $n_0 = -1/R_H ec$. Evidently the alkali metals obey the Drude result reasonably well, the noble metals (Cu, Ag, Au) less well, and the remaining entries, not at all.

Eksperymentalne wartości przewodności cieplnych i liczb Lorentza dla wybranych metali

ELEMENT	273 K		373 K	
	κ (watt/cm-K)	$\kappa/\sigma T$ (watt-ohm/K ²)	κ (watt/cm-K)	$\kappa/\sigma T$ (watt-ohm/K ²)
Li	0.71	2.22×10^{-8}	0.73	2.43×10^{-8}
Na	1.38	2.12		
K	1.0	2.23		
Rb	0.6	2.42		
Cu	3.85	2.20	3.82	2.29
Ag	4.18	2.31	4.17	2.38
Au	3.1	2.32	3.1	2.36
Be	2.3	2.36	1.7	2.42
Mg	1.5	2.14	1.5	2.25
Nb	0.52	2.90	0.54	2.78
Fe	0.80	2.61	0.73	2.88
Zn	1.13	2.28	1.1	2.30
Cd	1.0	2.49	1.0	
Al	2.38	2.14	2.30	2.19
In	0.88	2.58	0.80	2.60
Tl	0.5	2.75	0.45	2.75
Sn	0.64	2.48	0.60	2.54
Pb	0.38	2.64	0.35	2.53
Bi	0.09	3.53	0.08	3.35
Sb	0.18	2.57	0.17	2.69

Source: G. W. C. Kaye and T. H. Laby, *Table of Physical and Chemical Constants*, Longmans Green, London, 1966.

Pomiar doświadczalny ciepła właściwego w metalicznym potasie



Współczynniki elektronowe dla ciepła właściwego (pomiar/teoria)

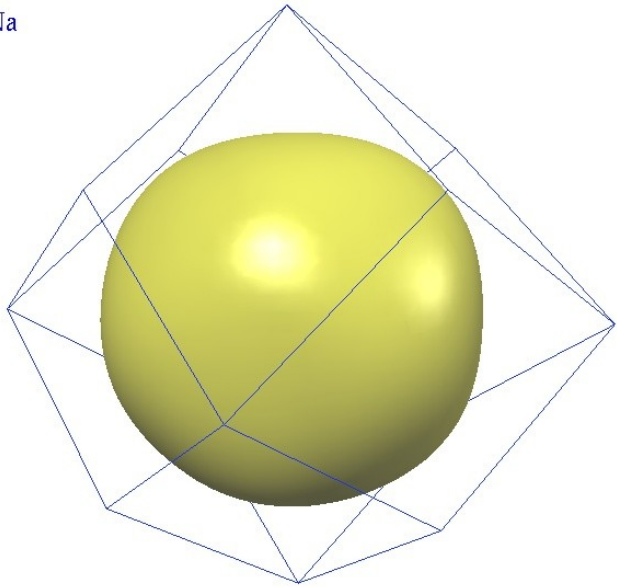
Table 2 Experimental and free electron values of electronic heat capacity constant γ of metals

(From compilations kindly furnished by N. Phillips and N. Pearlman. The thermal effective mass is defined by Eq. (38).

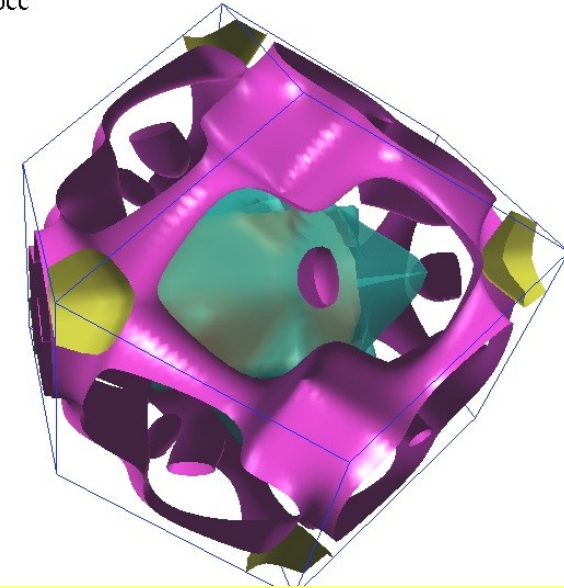
Observed γ in $\text{mJ mol}^{-1} \text{K}^{-2}$.												B	C	N	
Calculated free electron γ in $\text{mJ mol}^{-1} \text{K}^{-2}$												Al	Si	P	
$m_{\text{th}}/m = (\text{observed } \gamma)/(\text{free electron } \gamma)$.												Al	Si	P	
Li	Be														
1.63	0.17														
0.749	0.500														
2.18	0.34														
Na	Mg														
1.38	1.3														
1.094	0.992														
1.26	1.3														
K	Ca	Sc	Ti	V	Cr	Mn(γ)	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	
2.08	2.9	10.7	3.35	9.26	1.40	9.20	4.98	4.73	7.02	0.695	0.64	0.596		0.19	
1.668	1.511									0.505	0.753	1.025			
1.25	1.9									1.38	0.85	0.58			
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd*	In	Sn (w)	Sb	
2.41	3.6	10.2	2.80	7.79	2.0	—	3.3	4.9	9.42	0.646	0.688	1.69	1.78	0.11	
1.911	1.790									0.645	0.948	1.233	1.410		
1.26	2.0									1.00	0.73	1.37	1.26		
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg(α)	Tl	Pb	Bi	
3.20	2.7	10.	2.16	5.9	1.3	2.3	2.4	3.1	6.8	0.729	1.79	1.47	2.98	0.008	
2.238	1.937									0.642	0.952	1.29	1.509		
1.43	1.4									1.14	1.88	1.14	1.97		

Investigations of electronic states near the Fermi surface $E(\mathbf{k})=E_F$

Na



Fe_bcc



$$E(\mathbf{k}) = \frac{\hbar^2 (k_x^2 + k_y^2 + k_z^2)}{2m}$$

Electron motion in solids (semi-classical)

Group velocity of electrons

$$v_g = \frac{d\omega}{dk} = \frac{1}{\hbar} \frac{\partial E(k)}{\partial k} = \nabla_k E(k) = v(k)$$

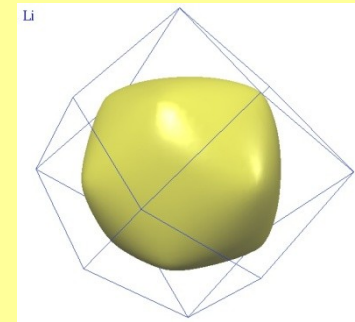
In general v -vector is NOT parallel to k -vector (e.g. ellipsoid), but it is perpendicular to isoenergetic surface $E(k)$

$$v = \frac{\hbar k}{m} \Leftrightarrow E(k) = \frac{\hbar^2 k^2}{2m}$$

$v(k)$ parallel to k only if Fermi surface is spherical

Acceleration of electrons

$$F = \hbar \frac{dk}{dt} \Rightarrow a_k = \frac{dv_k}{dt} = \frac{1}{\hbar} \frac{\partial^2 E(k)}{\partial k \partial k} \frac{dk}{dt} = \frac{1}{\hbar^2} \frac{\partial^2 E(k)}{\partial k \partial k} F$$



$$a_k = (m)^{-1} F \quad \text{where} \quad (m_{ij})^{-1} = \frac{1}{\hbar^2} \frac{\partial^2 E}{\partial k_i \partial k_j}$$

In general, tensor of effective mass is independent on electron velocity

$$n(E_F) \propto \frac{\partial E(k)}{\partial k}$$

How to measure ?

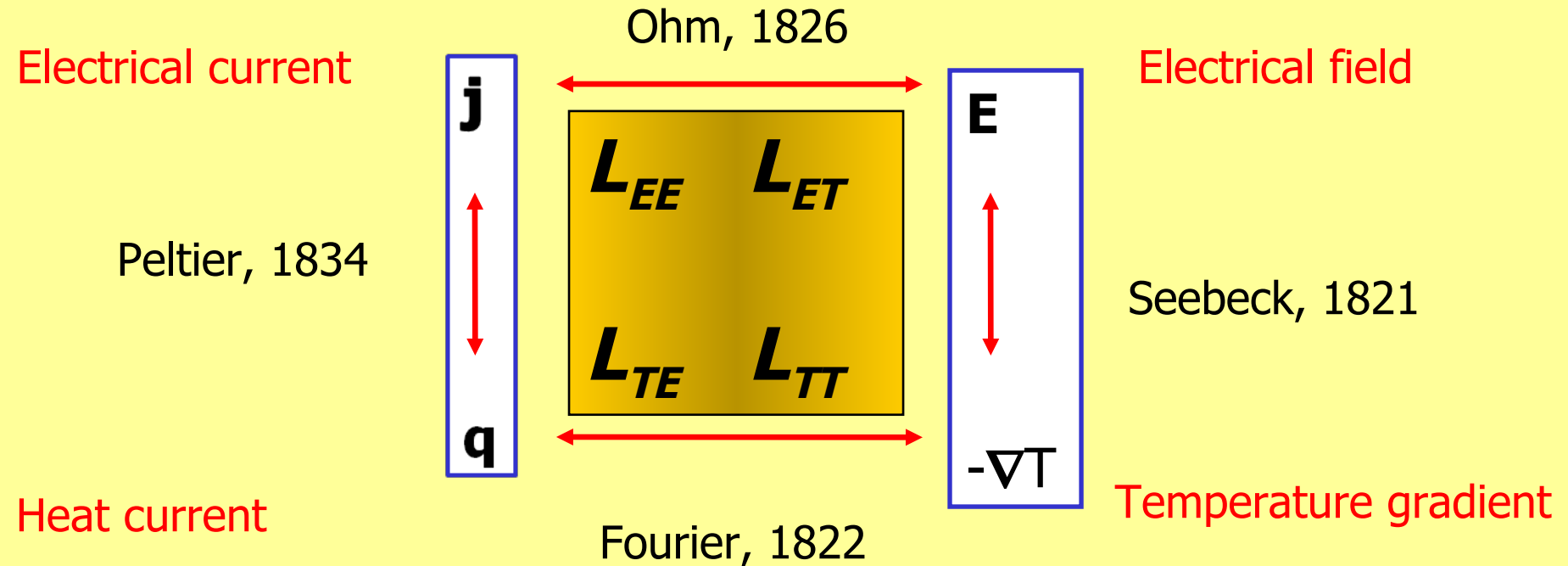
$$(m_{ij})^{-1} \propto \frac{\partial^2 E}{\partial k_i \partial k_j}$$

DOS near $E=E_F$ can be detected in specific heat and magnetic susceptibility measurements

Effective masses can be detected in dH-vA or transport measurements

Thermoelectric „tetragon“

$$\begin{bmatrix} \underline{j} \\ q \end{bmatrix} = \begin{bmatrix} L_{EE} & L_{ET} \\ L_{TE} & L_{TT} \end{bmatrix} \begin{bmatrix} E \rightarrow \\ -\nabla T \end{bmatrix}$$



$$S = \Pi T$$

(Kelvin-Onsager)

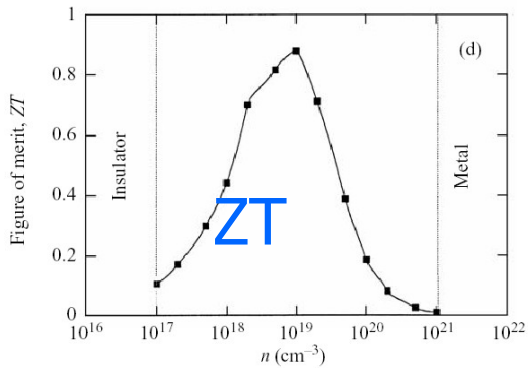
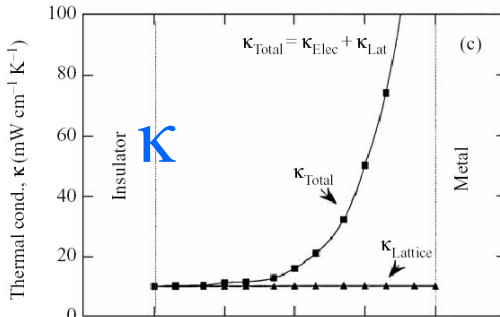
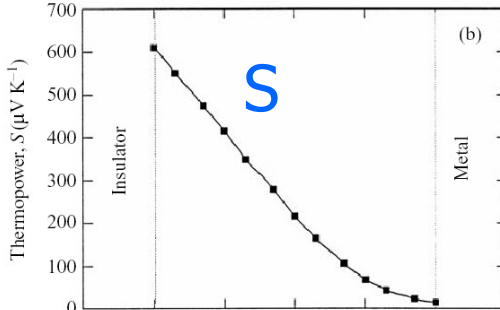
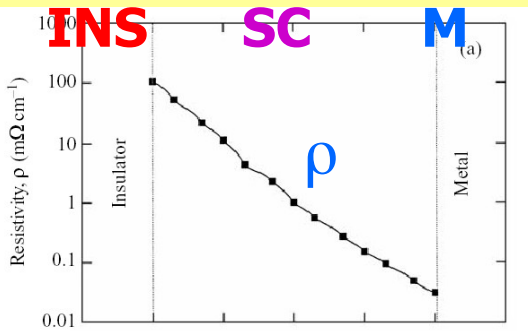
$$L_{ET} = L_{TE} / T$$

$$\kappa / \sigma \approx L_0 T$$

(Wiedemann-Franz, L_0 Lorentz number)

$$\kappa \approx -L_{TT}$$

Volta (1800), Ampere (1820), Faraday (1831), Gauss (1832), ...



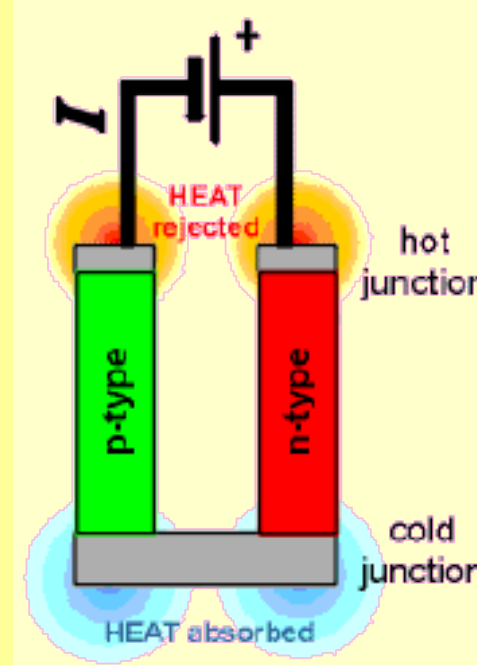
Thermoelectric properties



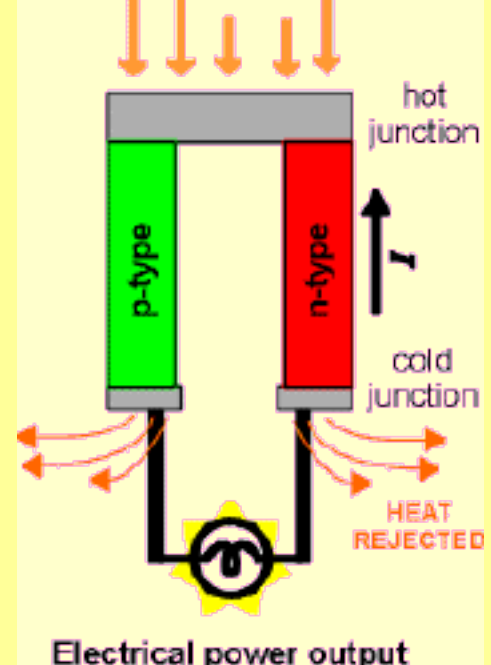
A. Joffe

$$ZT = \frac{S^2}{\rho \kappa}$$

Electrical power input



HEAT input



Thermoelectric properties - search for optimum

Carnot limit

COOLING ELEMENTS

$$COP = (T_H - T_C)(\gamma - 1)(T_C + \gamma T_H)^{-1}$$

POWER GENERATORS

$$\eta = (\gamma T_C - T_H)[(T_H - T_C + (\gamma + 1))]^{-1}$$

Improvement of figure of merit



Geometry of the devices

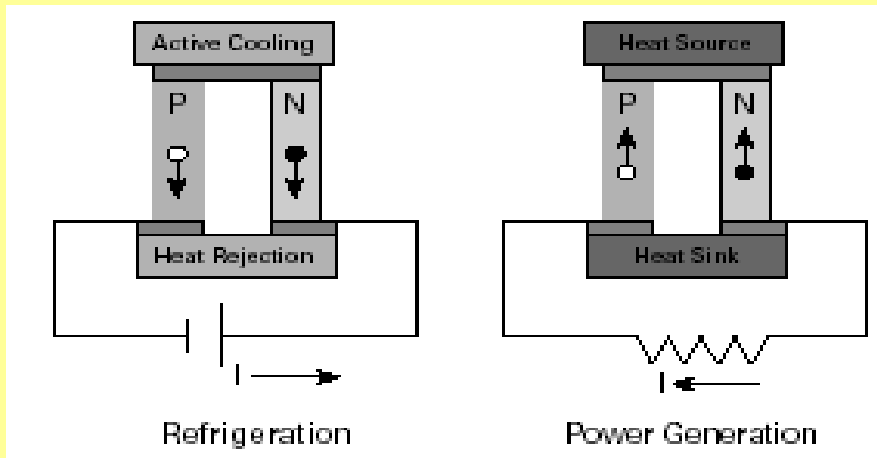
Physical properties of the system $\gamma = (1 + ZT)^{1/2}$

$$ZT = \frac{S^2 \sigma}{\kappa} T = \underbrace{\frac{S^2}{L}}_{\text{calculated}} \frac{1}{1 + \frac{\kappa_L}{\kappa_e}}$$

$$L = \frac{\kappa_e}{\sigma T}$$

Lorentz factor

Thermal conductivity (phonons / electrons)



$$\begin{bmatrix} \underline{j} \\ q \end{bmatrix} = \begin{bmatrix} L_{EE} & L_{ET} \\ L_{TE} & L_{TT} \end{bmatrix} \begin{bmatrix} E \rightarrow \\ -\nabla T \end{bmatrix}$$

Seebeck effect (1821)



1770 Tallin
1854 Berlin

Electric field

$$\mathbf{E} = S \nabla T$$

Temperature gradient

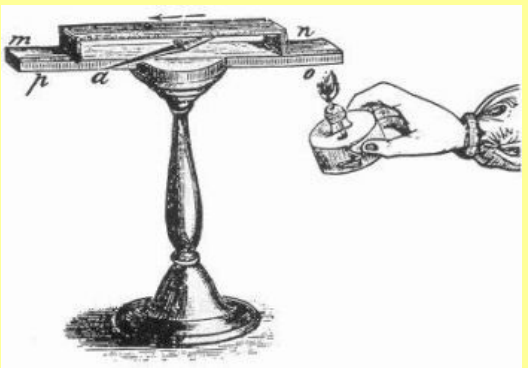
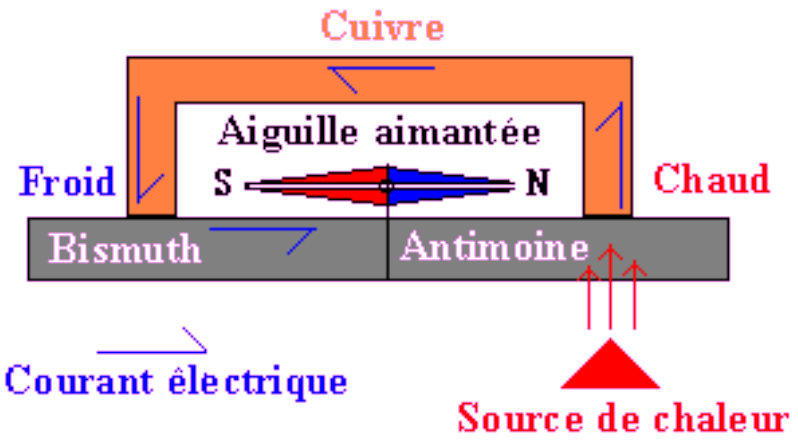
$$\left[\frac{\mu V}{K} \right]$$

thermopower

$$S = L_{EE}^{-1} L_{ET}$$

Vivid personality of the Romanticism

temperature gradient causes changes of magnetic field of Earth !!,
Oersted's experiments (1820) „blind” scientists.



Explanation : thermomagnetism - „magnetic”
polarisation of metals and alloys due to the difference of temperature !!

$$\begin{bmatrix} \underline{j} \\ q \end{bmatrix} = \begin{bmatrix} L_{EE} & L_{ET} \\ L_{TE} & L_{TT} \end{bmatrix} \begin{bmatrix} E \rightarrow \\ -\nabla T \end{bmatrix}$$

Peltier effect (1834)



1785 Ham
1845 Paris

Heat current

$$\mathbf{q} = \Pi \mathbf{j}$$

Electrical density current

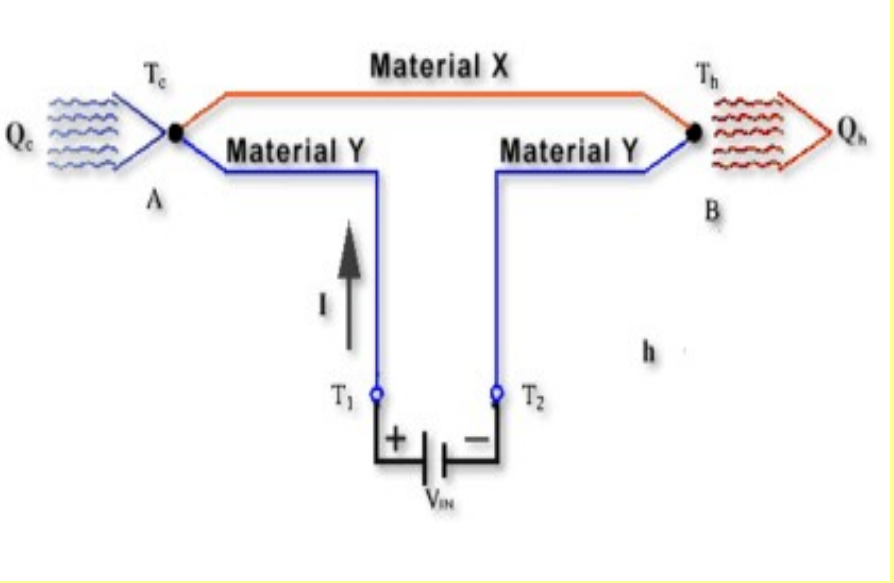
Peltier coefficient

$$\Pi = L_{TE} L_{EE}^{-1}$$

“Reverse” process to Seebeck effect

Thomson effect (1834)

Heat generation in the presence of electrical current \mathbf{j} and temperature gradient dT/dx



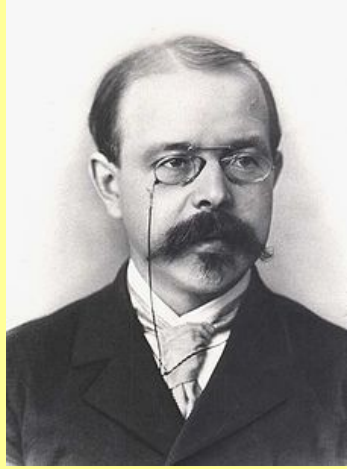
$$Q = \underbrace{j^2/\sigma}_{\text{Joule}} \pm \underbrace{\mu j dT/dx}_{\text{Thomson}}$$

$$\mu = T dS/dT$$

$$\Pi T = S \quad (\text{Thomson})$$

$$L_{ET} = L_{TE}/T$$

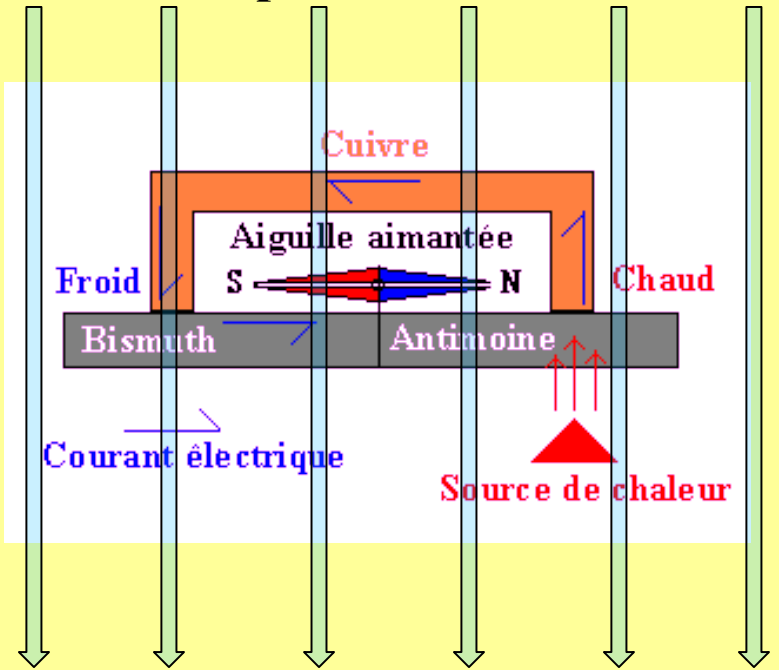
Nernst-(Ettingshausen) effect (1886)



Thermo-magneto-electric effect

$$|N| = \frac{E_y / B_z}{dT/dx} \quad \left[\frac{\mu V}{KT} \right]$$

“Reverse” process to Nernst effect = Ettingshausen effect



magnetic field **B**

Phenomenon observed when a sample conducting electrical current is subjected to a magnetic field **B** and a temperature gradient **dT/dx** perpendicular to each other.

E_y is the y -component of the electric field that results from the magnetic field's z -component B_z and the temperature gradient dT/dx .

$N \sim 0$ in metals

N large in semiconductors, superconductors, heavy-fermions, Dirac electrons in Bi, graphene, **Landau levels cross Fermi level**

1864 Wąbrzeźno
1941 Niwica

$$\begin{bmatrix} \dot{J} \\ q \end{bmatrix} = \begin{bmatrix} L_{EE} & L_{ET} \\ L_{TE} & L_{TT} \end{bmatrix} \begin{bmatrix} E \rightarrow \\ -\nabla T \end{bmatrix}$$

Fourier relation (1822)



1768 Auxerre
1830 Paris

Heat current

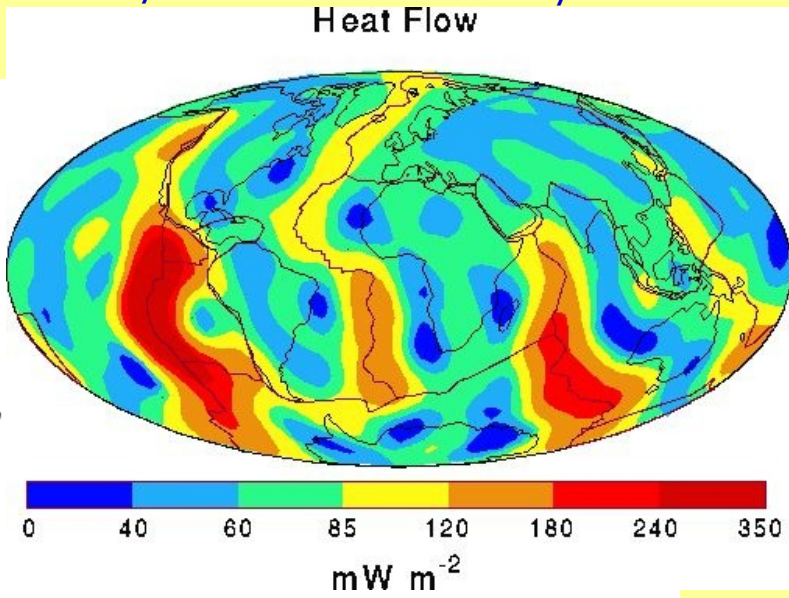
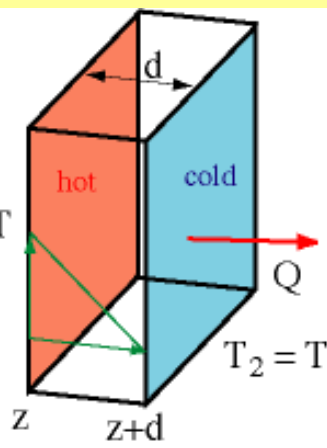
$$\mathbf{q} = -\kappa \nabla T$$

Temperature gradient

Thermal conductivity

$$\kappa = L_{TE} L_{EE}^{-1} L_{ET} - L_{TT}$$

Heat conducted (balance) = Heat generated in system - Heat accumulated in system



$$\nabla \mathbf{q} = q_{gen} - du/dt$$

$$du/dt = \rho c dT/dt$$

$$\nabla(-\kappa \nabla T) + \partial T / \partial t = q_{gen}$$

$$\nabla^2 T + (\rho c / \kappa) \partial T / \partial t = 0$$

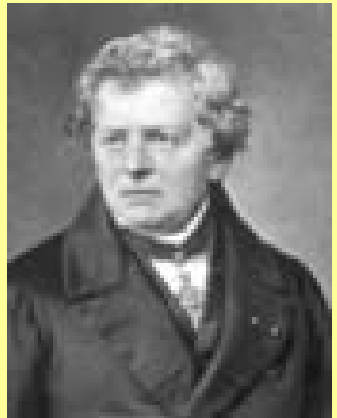
when $q_{gen} = 0$

in differential form: $Q(z) = -k \frac{dT}{dz}$

Heat conduction equation

$$\begin{bmatrix} \underline{j} \\ q \end{bmatrix} = \begin{bmatrix} L_{EE} & L_{ET} \\ L_{TE} & L_{TT} \end{bmatrix} \begin{bmatrix} E \rightarrow \\ -\nabla T \end{bmatrix}$$

Ohm law (1826)



1789 Erlangen
1854 Munchen

Electrical density current

$$\mathbf{j} = \sigma \mathbf{E}$$

Electric field

Electrical conductivity

$$\sigma = L_{EE} = ne\mu = ne\tau/m$$

Ohm's study inspired by works of Fourier and Seebeck



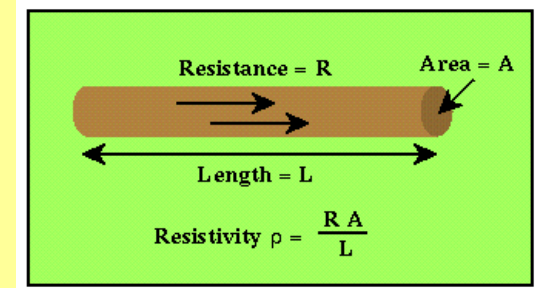
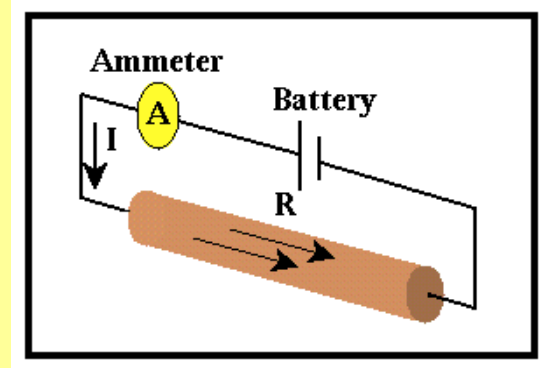
Metallic wire in cylinder

*Declination of magnetic needle proportional to electric current I

* Seebeck thermocouple – a source of electrical potential V

$$V/I = R = \text{constant}$$

when $R = \text{const.} !!$



„The Galvanic Circuit Investigated Mathematically” (1827)

Boltzmann equation



Electron system described by distribution function f in the (\mathbf{r}, \mathbf{k}) space.

$$\frac{1}{4\pi^3} f(\mathbf{k}, \mathbf{r}, t)$$

Fermi-Dirac function in equilibrium state

Electron density current

$$J(\mathbf{r}, t) = \frac{e}{4\pi^3} \int \mathbf{v}_k f(\mathbf{k}, \mathbf{r}, t) d\mathbf{k}$$

Transport equation

$$\frac{df}{dt} = -\frac{d\mathbf{k}}{dt} \cdot \nabla_{\mathbf{k}} f - \mathbf{v} \cdot \nabla_{\mathbf{r}} f + \frac{\partial f}{\partial t} + \left(\frac{\partial f}{\partial t} \right)_{coll}$$

Stationary condition

$$\frac{\partial f}{\partial t} = 0$$

time-independent forces

Collision integral $\left(\frac{\partial f}{\partial t} \right)_{coll}$

Describes **e-e** scatterings/collisions, probability of exit outside the $d\mathbf{k}d\mathbf{r}$ volume

Relaxation time approximation

$$\left(\frac{\partial f}{\partial t} \right)_{coll} = -\frac{f - f_0}{\tau}$$

Onsager coefficients

1-electron Boltzmann eq. in the presence of fields :

E, B & ∇T

$$\vec{v}_k \cdot \vec{\nabla} T \frac{\partial f}{\partial T} + \frac{q}{\hbar} (\vec{E} + \vec{v}_k \times \vec{B}) \cdot \frac{\partial f}{\partial \vec{k}} = - \frac{f - f_0}{\tau}$$



After linearisation

$$f = f_0 - \left(q\vec{E} - \frac{\nabla T}{T} (\varepsilon_k - \mu) \right) \frac{\partial f_0}{\partial \varepsilon} \cdot \vec{\Lambda}_k \quad \text{where} \quad \vec{\Lambda}_k = \tau \vec{v}_k \quad \text{Mean-free path}$$

Electric current density

$$\vec{j} = \frac{1}{V} \sum_k q \vec{v}_k f_k = \left(\int d\varepsilon \sigma(\varepsilon) \frac{\partial f_0}{\partial \mu} \right) \vec{E} + \left(\int d\varepsilon \frac{1}{q} \sigma(\varepsilon) (\varepsilon - \mu) \frac{\partial f_0}{\partial \mu} \right) \left(- \frac{\nabla T}{T} \right)$$

Heat density current

$$\vec{j}^Q = \frac{1}{V} \sum_k (\varepsilon_k - \mu) \vec{v}_k f_k = \left(\int d\varepsilon \frac{1}{q} \sigma(\varepsilon) (\varepsilon - \mu) \frac{\partial f_0}{\partial \mu} \right) \vec{E} + \left(\int d\varepsilon \frac{1}{q^2} \sigma(\varepsilon) (\varepsilon - \mu)^2 \frac{\partial f_0}{\partial \mu} \right) \left(- \frac{\nabla T}{T} \right),$$

$$\vec{j} = L_{11} \vec{E} + L_{12} \left(- \frac{\nabla T}{T} \right)$$

$$\vec{j}^Q = L_{21} \vec{E} + L_{22} \left(- \frac{\nabla T}{T} \right)$$

Transport functions

With applied \mathbf{E} and ∇T ($\mathbf{B}=\mathbf{0}$)

Transport function

$$\sigma(\varepsilon) = \frac{q^2 \tau}{V} \sum_k \vec{v}_k \vec{v}_k \delta(\varepsilon_k - \varepsilon)$$

Applying additional magnetic field \mathbf{B} (Hall effect)

Mean free path of electrons

$$\vec{\Lambda}_k = \tau \vec{v}_k - \frac{q\tau}{\hbar} \left(\vec{v}_k \times \vec{B} \cdot \frac{\partial}{\partial \vec{k}} \right) \vec{\Lambda}_k$$

Electrical current density

$$\vec{j} = \frac{1}{V} \sum_k q \vec{v}_k f_k = \left(\int d\varepsilon \sigma_B(\varepsilon) \frac{\partial f_0}{\partial \mu} \right) \vec{E} = \sigma(\vec{B}) \vec{E}$$

Magnetic transport function

$$\sigma_B(\varepsilon) = \frac{q^2}{V} \sum_k \vec{v}_k \vec{\Lambda}_k \delta(\varepsilon_k - \varepsilon)$$

Transport coefficients



Electrical conductivity

$$\sigma = L_{11},$$

when $\nabla T = 0$

Thermopower

$$S = \frac{L_{11}^{-1} L_{12}}{T},$$

when $\mathbf{j} = 0$

Thermal conductivity

$$\kappa_e = \frac{1}{T} \left(L_{22} - \frac{L_{21} L_{12}}{L_{11}} \right),$$

Hall coefficient

$$R_H = \frac{\rho_{yx}}{B},$$

Hall concentration

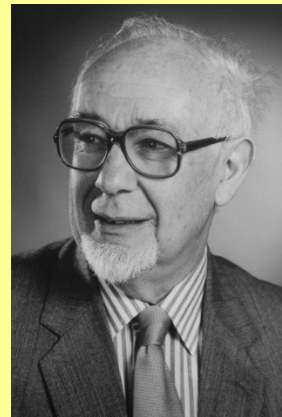
$$n_H \equiv \frac{1}{R_H q} = \alpha(n) n$$

Lorenz factor

$$L = \frac{\kappa_e}{T \sigma} = \frac{1}{T} \frac{L_{22} - L_{21} (L_{11})^{-1} L_{12}}{L_{11}}$$

$$\begin{bmatrix} \underline{j} \\ q \end{bmatrix} = \begin{bmatrix} L_{EE} & L_{ET} \\ L_{TE} & L_{TT} \end{bmatrix} \begin{bmatrix} E \rightarrow \\ -\nabla T \end{bmatrix}$$

Kinetic theory of Ziman



$$\sigma(T) = e^2/3 \int dE N(E) v^2(E) \tau(E, T) [-\partial f(E)/\partial E]$$

Electrical conductivity

$$S(T) = e(3T\sigma)^{-1} \int dE N(E) v^2(E) E \tau(E, T) [-\partial f(E) / \partial E] =$$

$$(3eT\sigma)^{-1} \int dE \sigma(E, T) E [-\partial f(E) / \partial E]$$

Thermopower (Seebeck coefficient)

$$N(E) = (2\pi)^{-3} \int \delta(E(\mathbf{k})-E) d\mathbf{k}$$

DOS (density of states)

Thermal conductivity

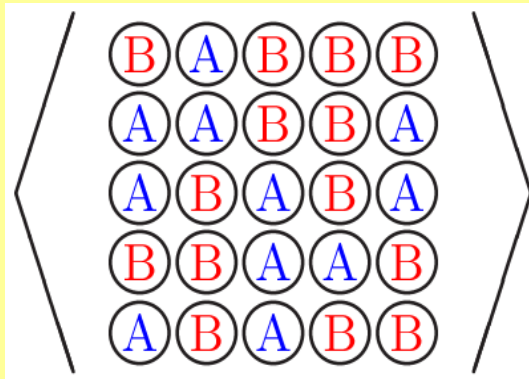
$$\kappa/\sigma \approx L_0 T, L_0 = \text{const} \quad \kappa \approx -L_{TT}$$

Wiedemann-Franz law, L_0 Lorentz number

Relaxation time in transport Boltzman equation

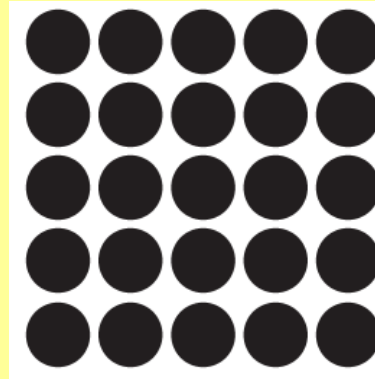
KKR-CPA method & complex bands

- Disordered alloys: ~~periodic~~ - Coherent Potential Approximation (CPA):



CPA “trick”

=



CPA condition

$$c_A T^A + c_B T^B = T^{CP}$$

In multi-atomic systems more imagination needed !

$$T_{k'\sigma'L',k\sigma L}^{CP} = \frac{1}{N} \sum_{\mathbf{k} \in BZ} [\tau_{CP}^{-1} - B(E, \mathbf{k})]_{k'\sigma'L',k\sigma L}^{-1}$$

CPA crystal - restored periodicity

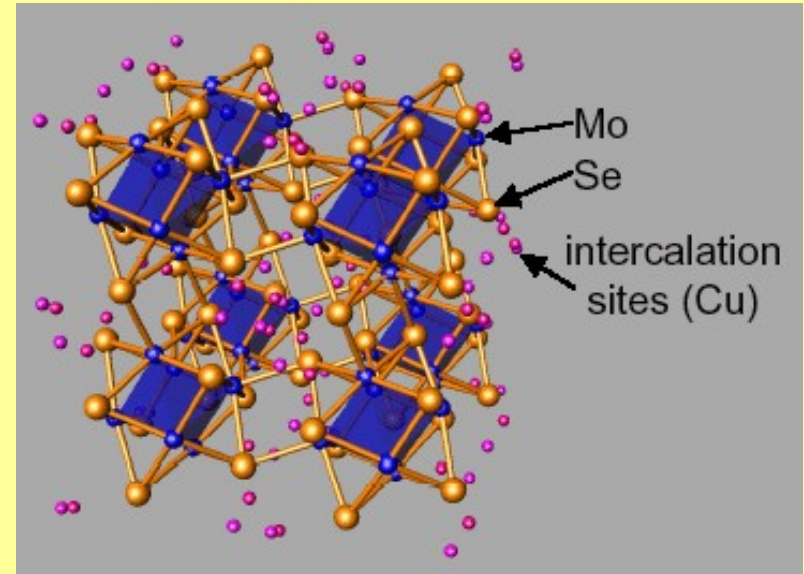
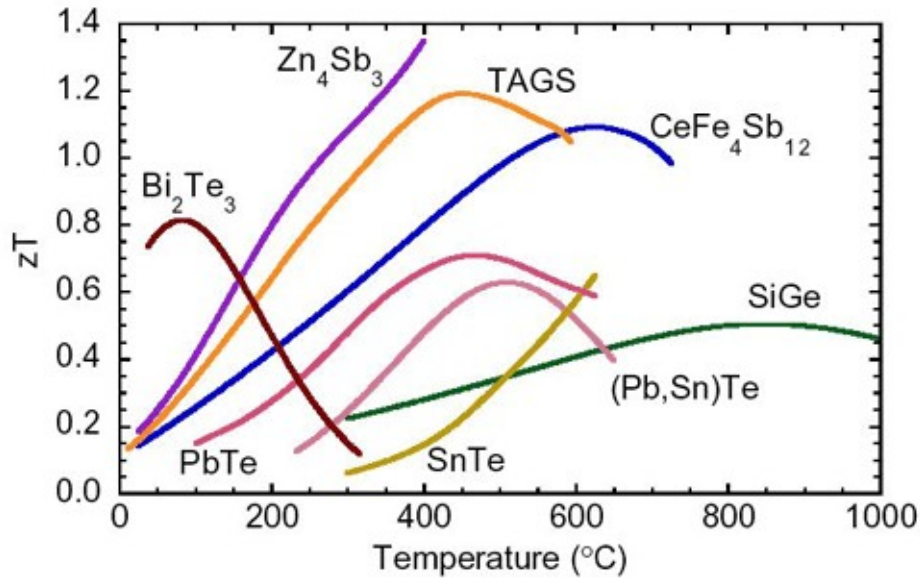
• **price: complex potential**

CPA much better than virtual crystal approx. V_{VCA}

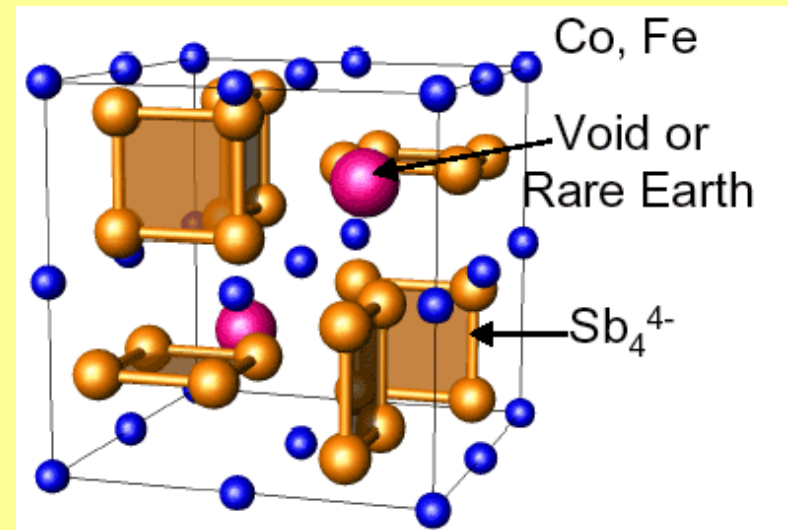
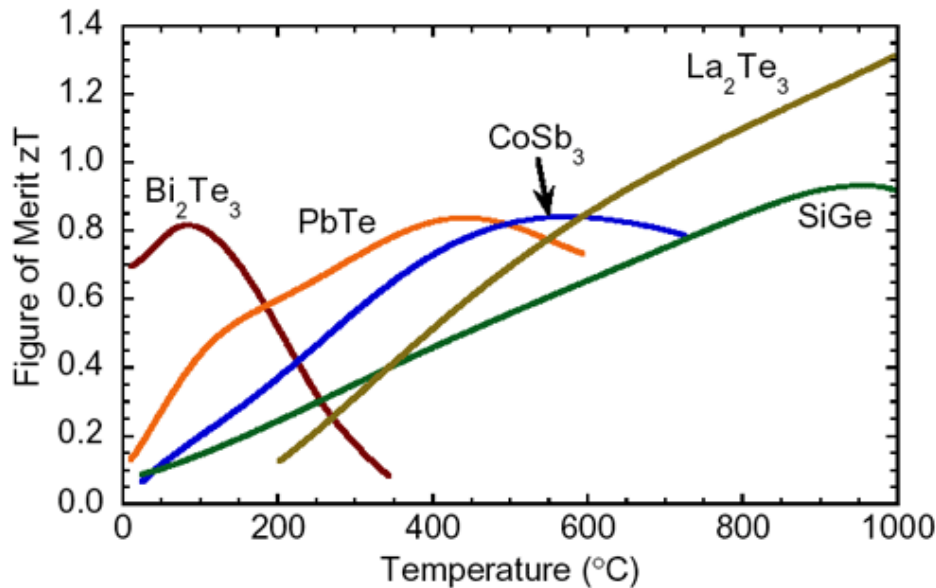
Present KKR-CPA code allows for treatment of more than 2 atoms on disordered site, but within *muffin-tin* potential (problem with CPA condition), CPA is also solved self-consistently; imaginary part of $E(\mathbf{k})$ related to electron life-time due to disorder !

Thermoelectric materials

$$ZT = \frac{S^2}{\rho \kappa}$$



Chevrel phases



Skutterudites

J. Snyder, JPL-NASA

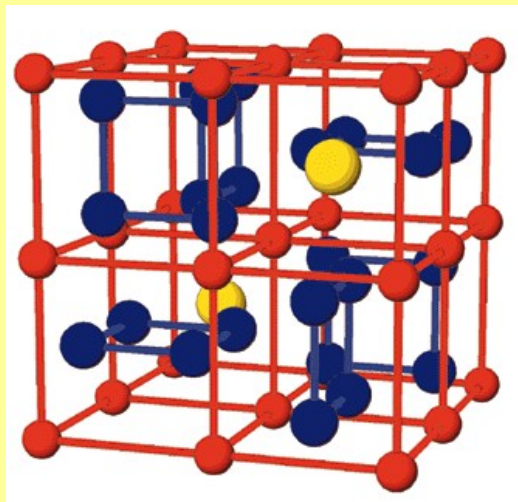
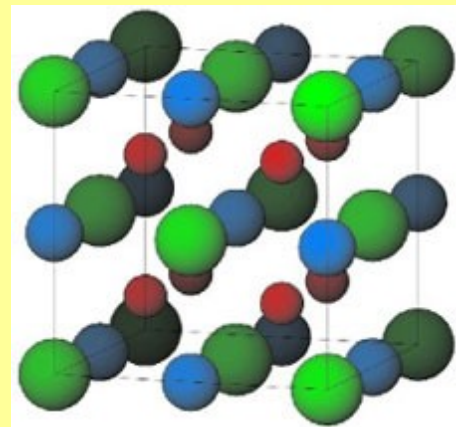
Electronic structure peculiarities

Half-Heusler (VEC=18)

Semiconductors/semimetals

(CoTiSb, NiTiSn, FeVSb, ...)

9 + 4 + 5=18 wide variety !!



Skutterudites (VEC=96)

semiconductors/semimetals

(CoSb₃, RhSb₃, IrSb₃, CoP₃ ...)

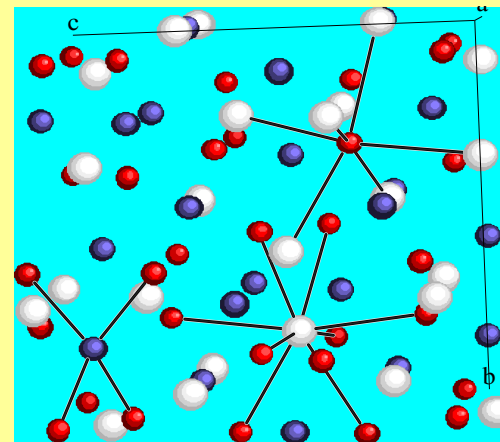
4 x 9 + 12 x 5 = 96

Zintl phases (VEC=62)

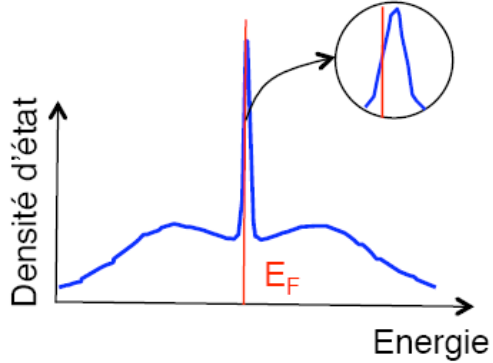
semiconductors/semimetals

(Y₃Cu₃Sb₄, Y₃Au₃Sb₄, ...)

3 x 4 + 3 x 10 + 4 x 5 = 62

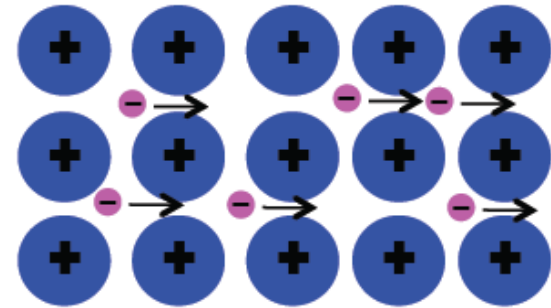
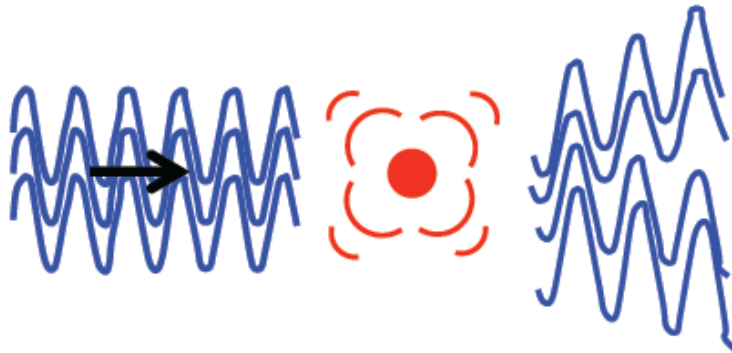


Concepts of ZT improvement

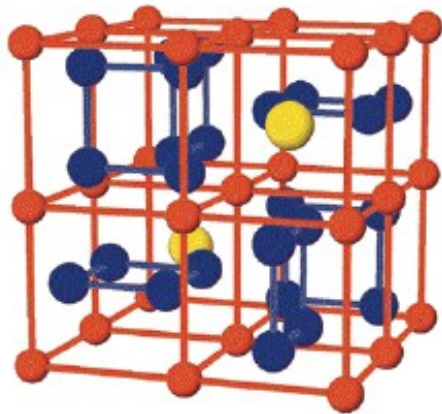


Sharp DOS (heavy fermions, QC, low dimension).

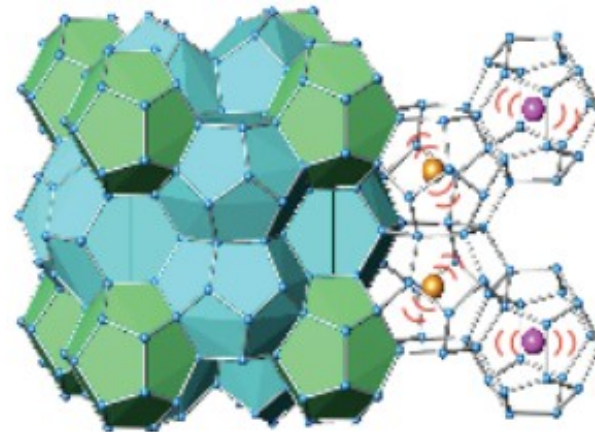
PGEC – „phonon glass” + „electron crystal” (Slack, '95)



more complex structures + specific vibrations (rattling, phonon, magnon)



skutterudites



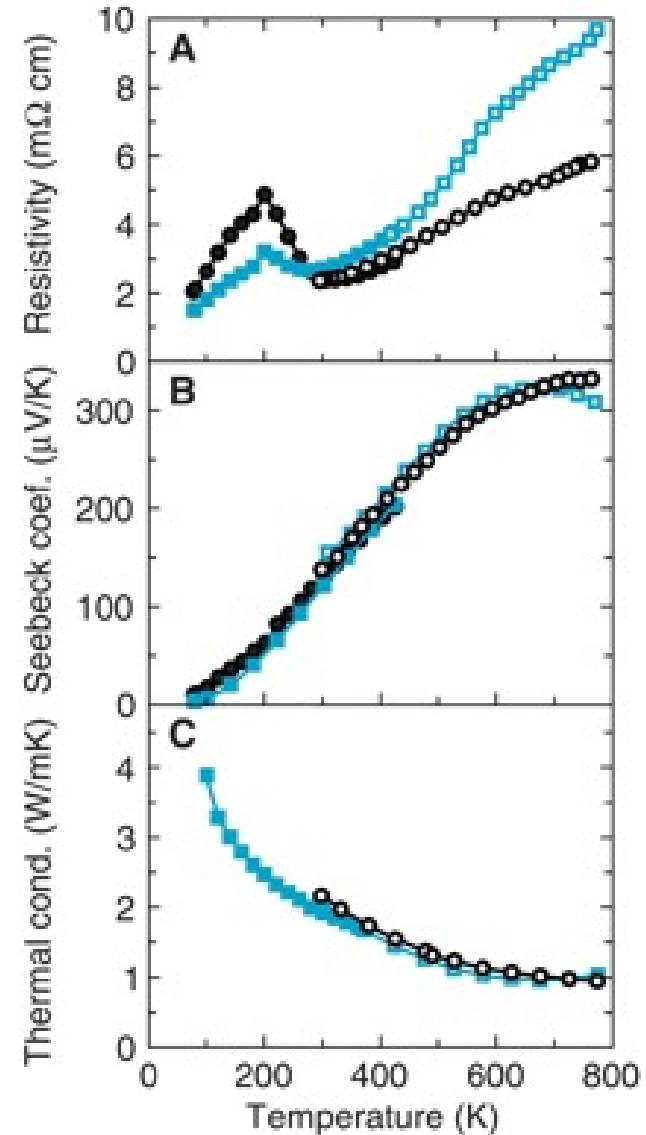
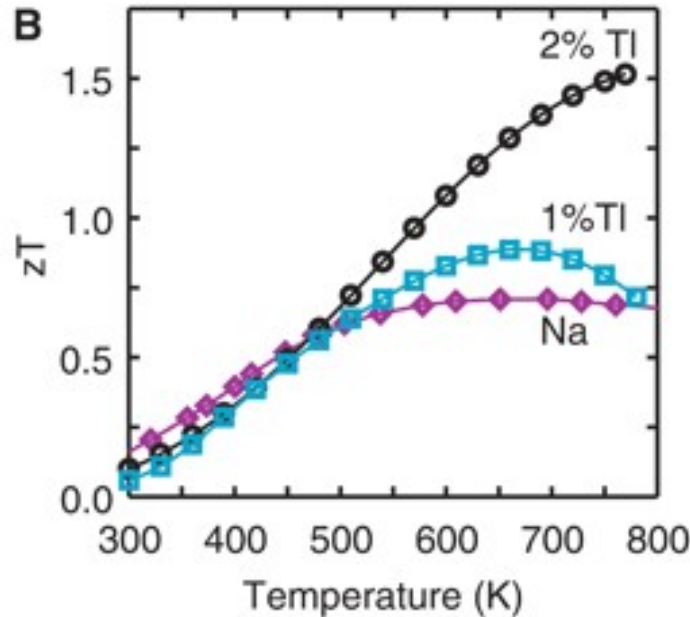
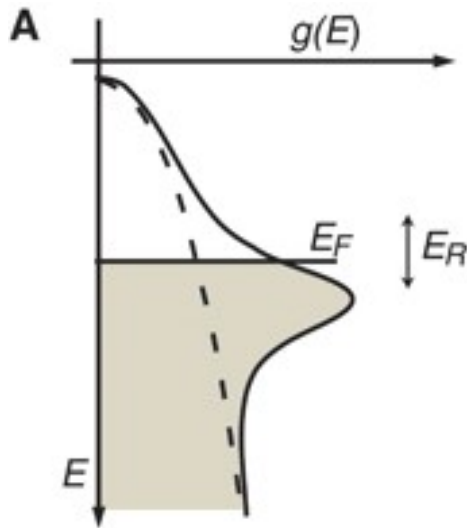
clathrates

Enhancement of TE efficiency in **PbTe**

(distortion of electronic DOS)

$$S = \frac{\pi^2}{3} \frac{k_B}{q} k_B T \left\{ \frac{1}{n} \frac{dn(E)}{dE} + \frac{1}{\mu} \frac{d\mu(E)}{dE} \right\}_{E=E_F}$$

Mott's formula for thermopower



J. Heremans et al., Science **321** (2008) 544

Electron transport coefficients

$$\sigma_e = \mathcal{L}^{(0)},$$

Electrical conductivity

$$S = -\frac{1}{eT} \frac{\mathcal{L}^{(1)}}{\mathcal{L}^{(0)}},$$

Seebeck coefficient (thermopower)

$$\kappa_e = \frac{\mathcal{L}^{(2)}}{e^2 T} - \frac{\mathcal{L}^{(1)} \mathcal{L}^{(1)}}{e^2 T \mathcal{L}^{(0)}}$$

Electronic thermal conductivity

$$L(T) = \frac{\kappa_e(T)}{\sigma(T)T} \quad \text{Wiedemann-Franz-Lorenz}$$

$$L = \frac{\kappa_e}{\sigma T}$$

$$PF = S^2 \sigma$$

Onsager-related functions

$$\mathcal{L}^{(\alpha)} = \int d\mathcal{E} \left(-\frac{\partial f}{\partial \mathcal{E}} \right) (\mathcal{E} - \mu)^\alpha \sigma(\mathcal{E})$$

$$ZT = \frac{S^2 \sigma T}{\kappa_e + \kappa_l}$$

$$L(T, n)$$

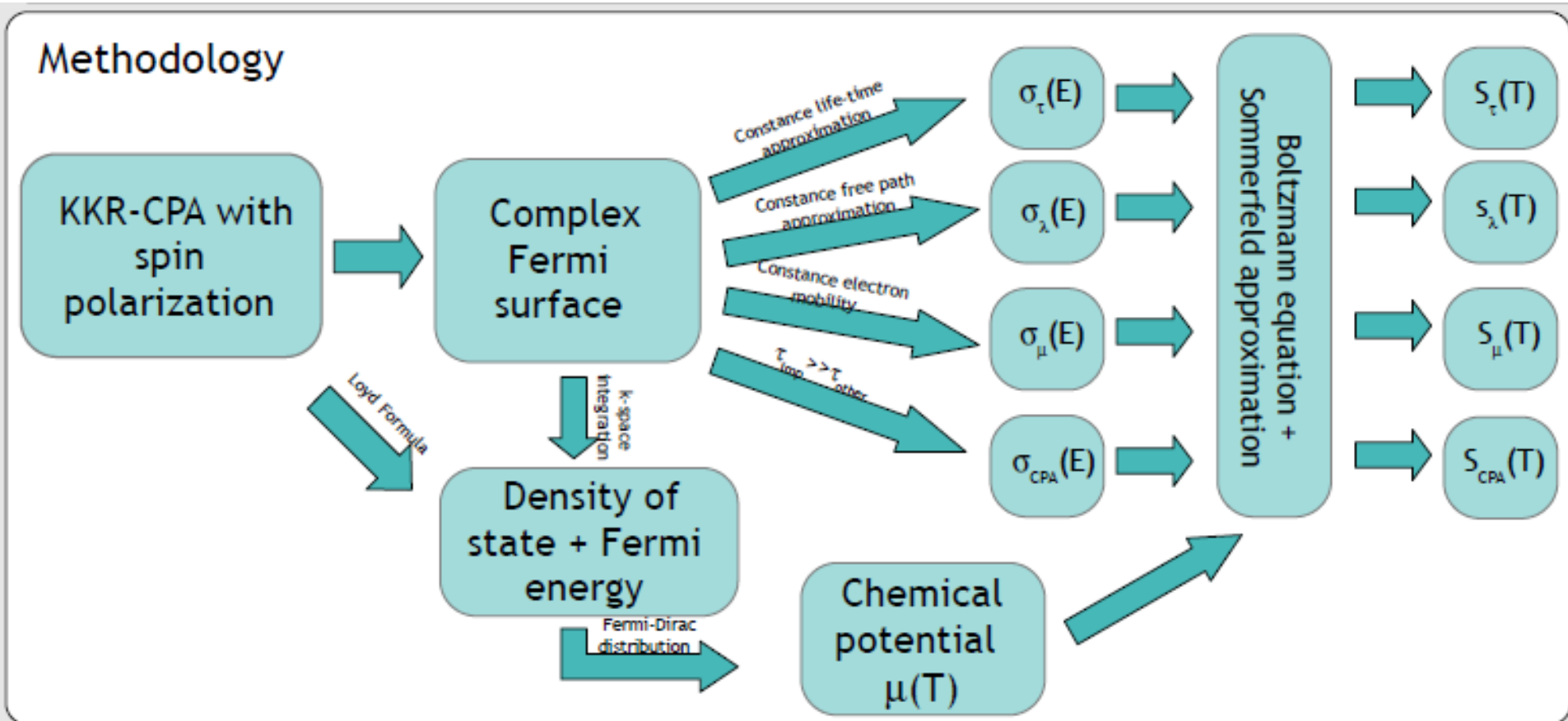
$$PF(T, n)$$

$$ZT(T, n)$$

Transport functions (in general tensors)

$$\sigma(\mathcal{E}) = e^2 \sum_n \int \frac{d\mathbf{k}}{4\pi^3} \tau_n(\mathbf{k}) \mathbf{v}_n(\mathbf{k}) \otimes \mathbf{v}_n(\mathbf{k}) \delta(\mathcal{E} - \mathcal{E}_n(\mathbf{k}))$$

Boltzmann transport & KKR-CPA calculations of complex energy bands and thermopower



K. Kutorasinski, Ph.D. Thesis (2014)

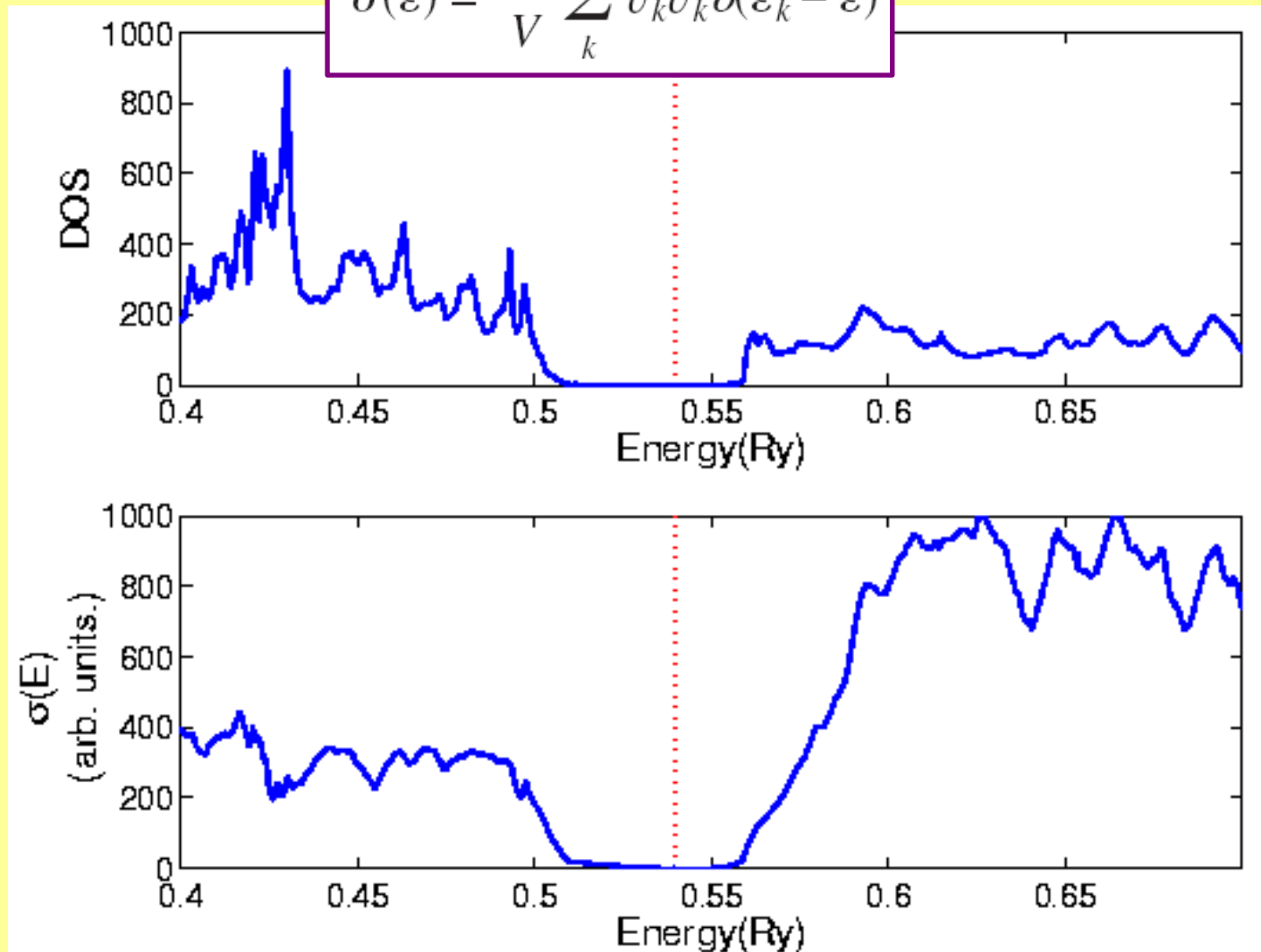
Different approximations used

- (1) $\tau = \text{const}$; (2) $\lambda = \text{const}$; (3) $\mu = \text{const}$; (4) CPA (velocity + life-time);

DOS vs. transport function $\sigma(E)$

$$\sigma(\varepsilon) = \frac{q^2 \tau}{V} \sum_k \vec{v}_k \vec{v}_k \delta(\varepsilon_k - \varepsilon)$$

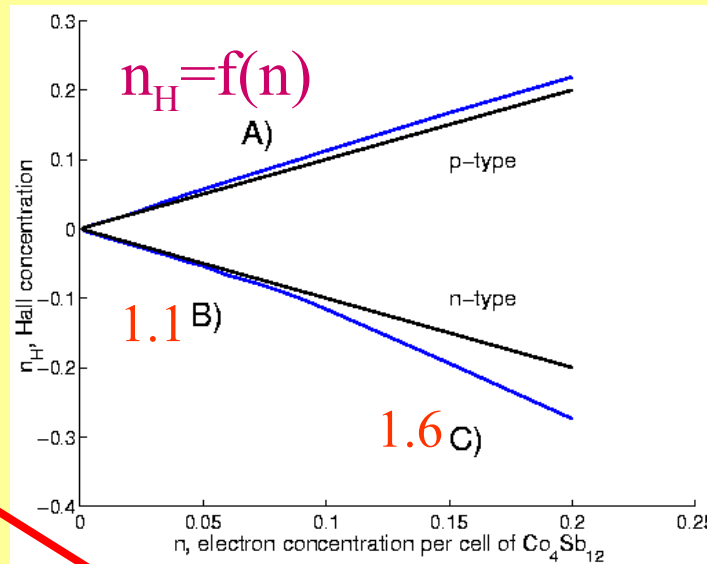
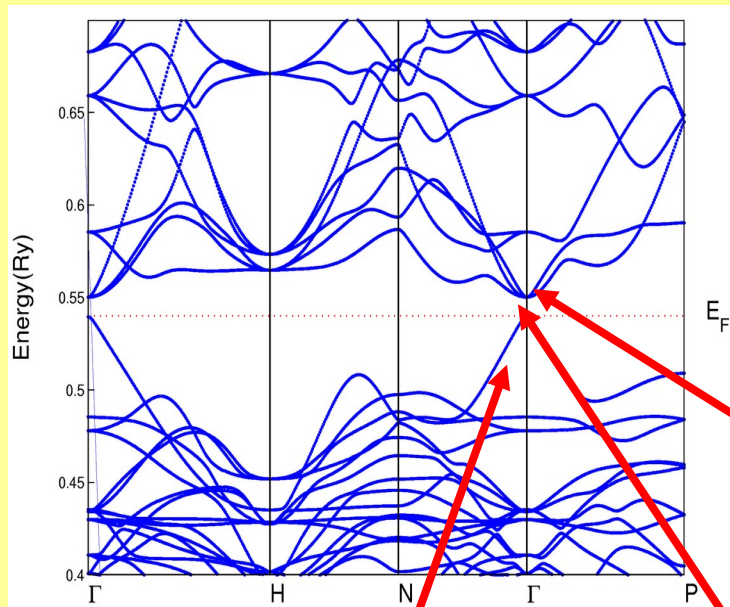
Chaput, ... JT, PRB (2005)



Small substitution/doping 0.01-0.05 el. per $\text{Co}_4\text{Sb}_{12}$ $\rightarrow \Delta E_F \approx 1-2$ mRy

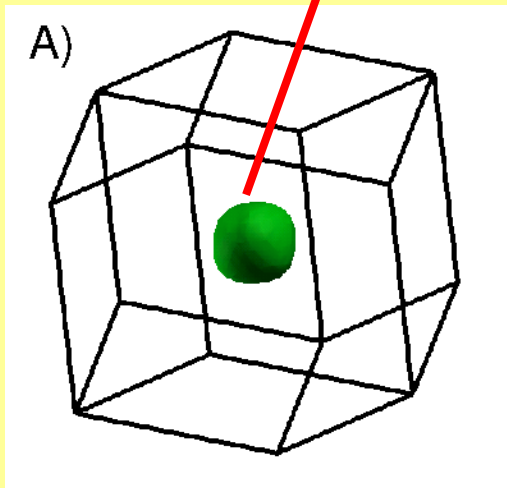
Doped CoSb_3 : FS vs. Hall concentration (rigid band)

Chaput, ... JT, PRB (2005)

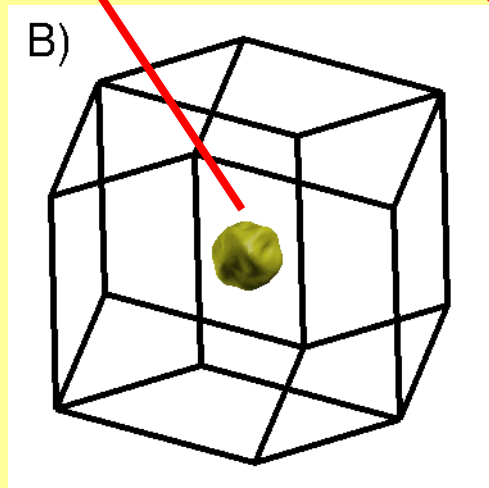


Valence bands

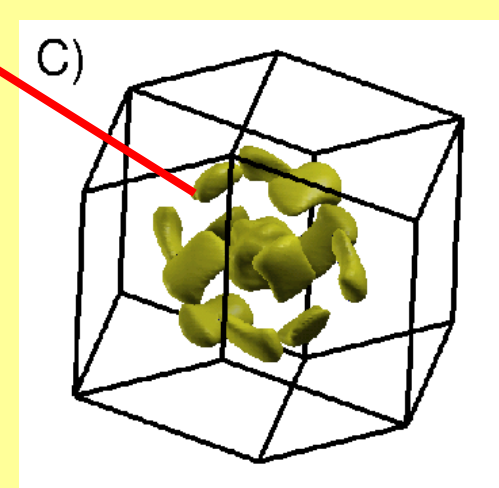
Conduction bands



$E_F = 0.5191 \text{ Ry}, n = 0.01$



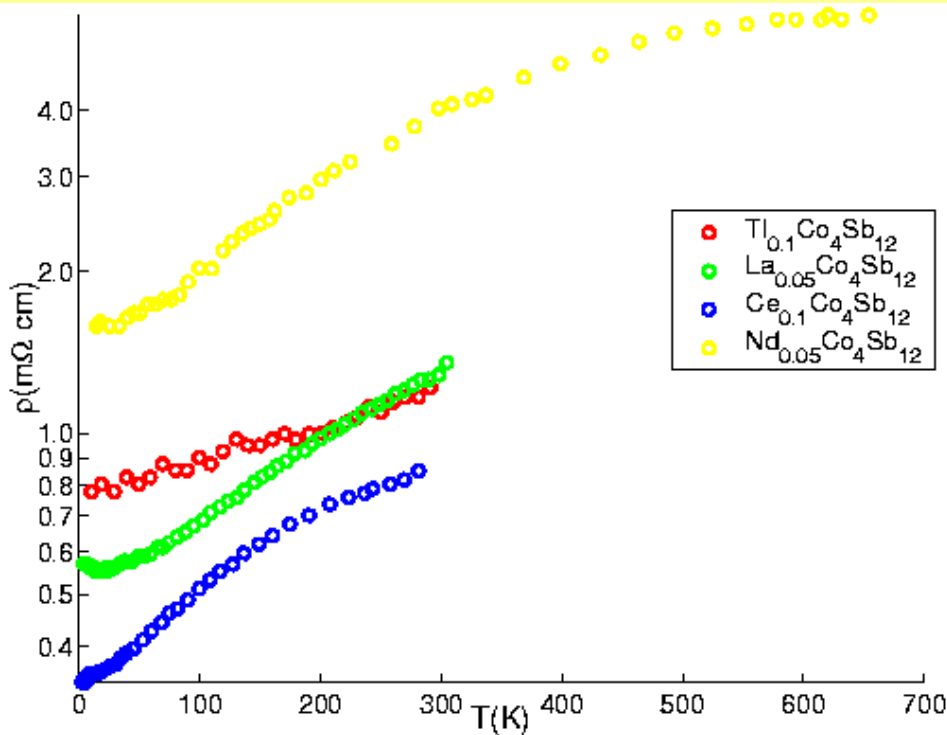
$E_F = 0.5570 \text{ Ry}, n = 0.01$



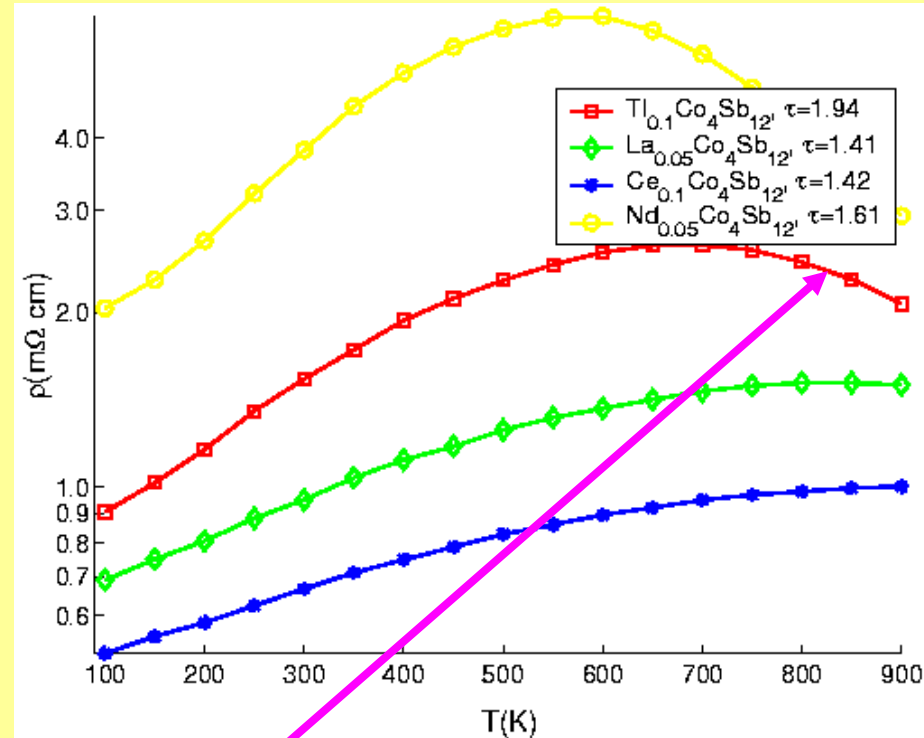
$E_F = 0.5585 \text{ Ry}, n = 0.06$

Doped CoSb_3 : electrical resistivity

Experiment (literature)



FLAPW calculations



Constant relaxation time (only one free parameter selected in order to gain the best fits to experimental resistivity curves, includes also lattice contribution)

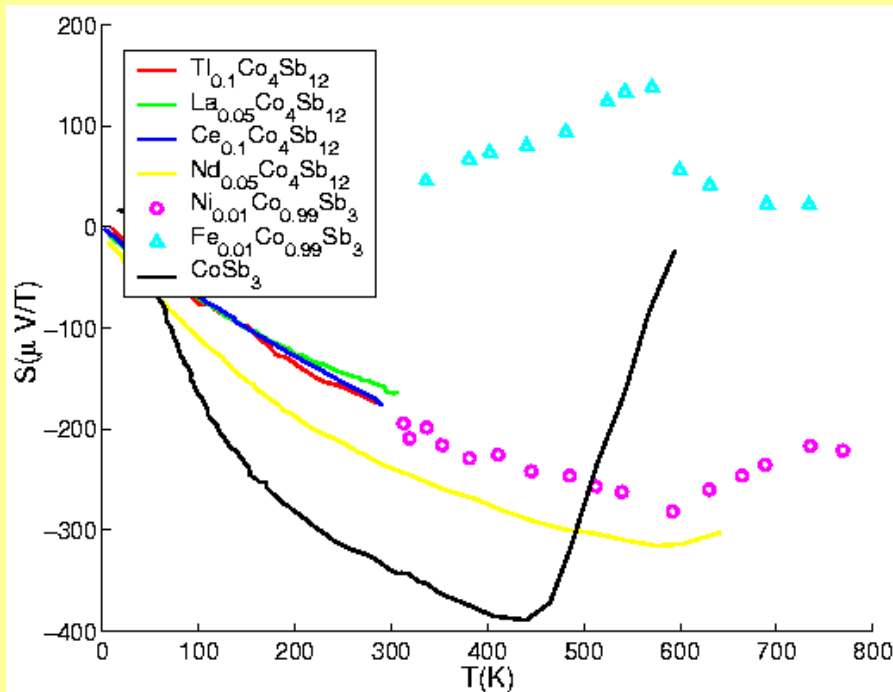
($\tau \sim 10^{-14}$ s), concentration of carriers taken from Hall measurements

(not from nominal composition !)

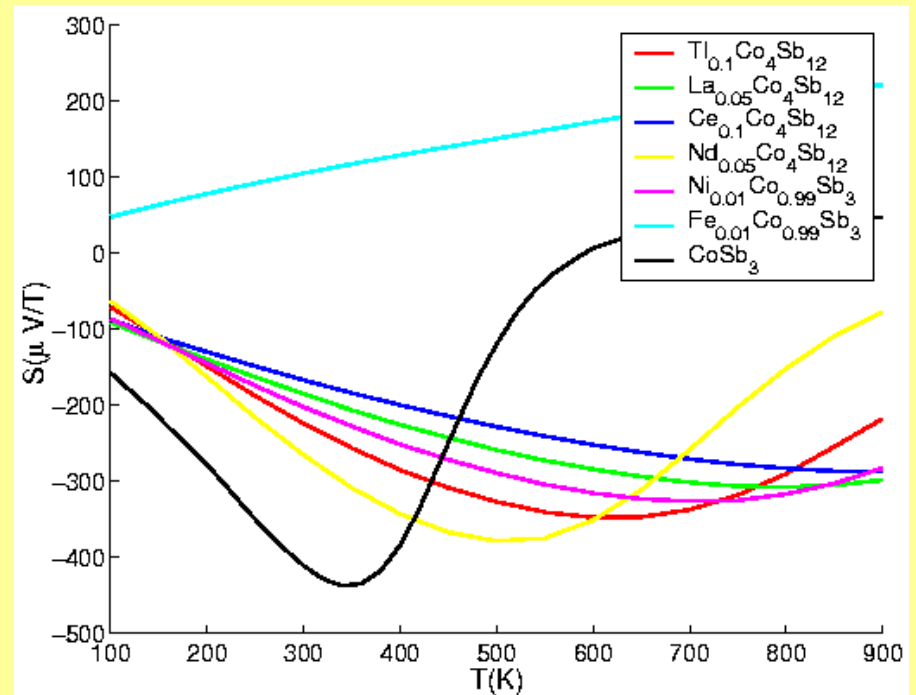
Chaput, ... JT, PRB (2005)

Doped CoSb₃ : thermopower

Experiment (literature)



FLAPW calculations



Constant relaxation time – NOT important, since Seebeck coefficient
Does not depend on this parameter – Excellent test for theory !!

$$S(T) = e(3T\sigma)^{-1} \int dE N(E) v^2(E) E \tau(E, T) [-\partial f(E)/\partial E]$$